



**NTNU – Trondheim**  
Norwegian University of  
Science and Technology

Department of chemical engineering

## **Examination paper for TKP4105 (Separation Technology)**

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**Examination date:            16.12.15**

**Examination time (from-to): 09:00 – 13:00**

**Permitted examination support material: No printed or handwritten material  
permitted. Simple calculator code D accepted.**

**Other information: Attachments to be turned inn with answers**

**Language: English**

**Number of pages:            5**

**Number of pages enclosed: 2**

**mm-paper may be needed for problem 1**

**Checked by:**

12/12-2016      Roge Johnsen  
Date                              Signature

## Problem 1 (Ekstraksjon, 25%)

(Use the sheet in Attachment 1 to solve this problem or use mm-sheet)

We have 1 kg/s of a feed with 26.5 weight-% acetic acid and 73.5% water ( $L_0$ ) which is difficult to separate using distillation. Instead we want use extraction with kg/s isopropyl ether ( $V_0$ ).

(a) Use the data in the table to complete the drawing of the triangle diagram (write on legends on the axes, tie lines, two-phase region) for the system water – acetic acid – isopropyl ether (see separate sheet at the end which you can tear off and hand in with your solution)

(b) Draw a flowsheet of single-stage extraction. What are the amounts and compositions of the two products ( $L_1$  and  $V_1$ )?

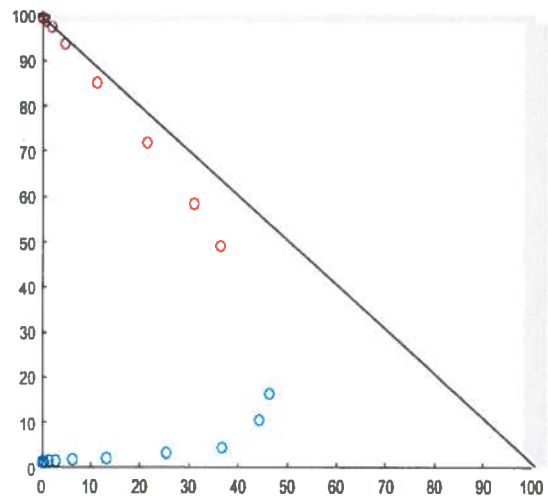
(c) Draw a flowsheet of 5-stage countercurrent extraction. We want an aqueous product ( $L_5$ ) with 1% acetic acid. What is the definition of  $\Delta$  and where is the  $\Delta$ -point located for this separation (approximately)? Is the separation possible when we use 1 kg/s isopropyl ether and use 5 stages (see also the next question)?

(d) What is the minimum amount ( $V_{0,min}$ ) of isopropyl ether required when we want the aqueous product to contain 1% acetic acid (with an infinite number of equilibrium stages)?

**A.3-24 Acetic Acid–Water–Isopropyl Ether System, Liquid–Liquid Equilibria at 293 K or 20°C**

Acetic Acid	Water Layer (wt %)		Isopropyl Ether Layer (wt %)		
	Water	Isopropyl Ether	Acetic Acid	Water	Isopropyl Ether
0	98.8	1.2	0	0.6	99.4
0.69	98.1	1.2	0.18	0.5	99.3
1.41	97.1	1.5	0.37	0.7	98.9
2.89	95.5	1.6	0.79	0.8	98.4
6.42	91.7	1.9	1.93	1.0	97.1
13.30	84.4	2.3	4.82	1.9	93.3
25.50	71.1	3.4	11.40	3.9	84.7
36.70	58.9	4.4	21.60	6.9	71.5
44.30	45.1	10.6	31.10	10.8	58.1
46.40	37.1	16.5	36.20	15.1	48.7

Source: *Trans. A.I.Ch.E.*, 36, 601, 628 (1940). With permission.



## Problem 2 Drying (30%)

- Explain with a sketch of the system what we mean when we say 1) the drying process is adiabatic, and 2) what is understood by wet bulb temperature
- A typical drying curve is given in the figure below where drying rate ( $R$ ) is a function of free water ( $X$ ).

Explain how the drying takes place in the three different regions; B-C, C-D, D-E

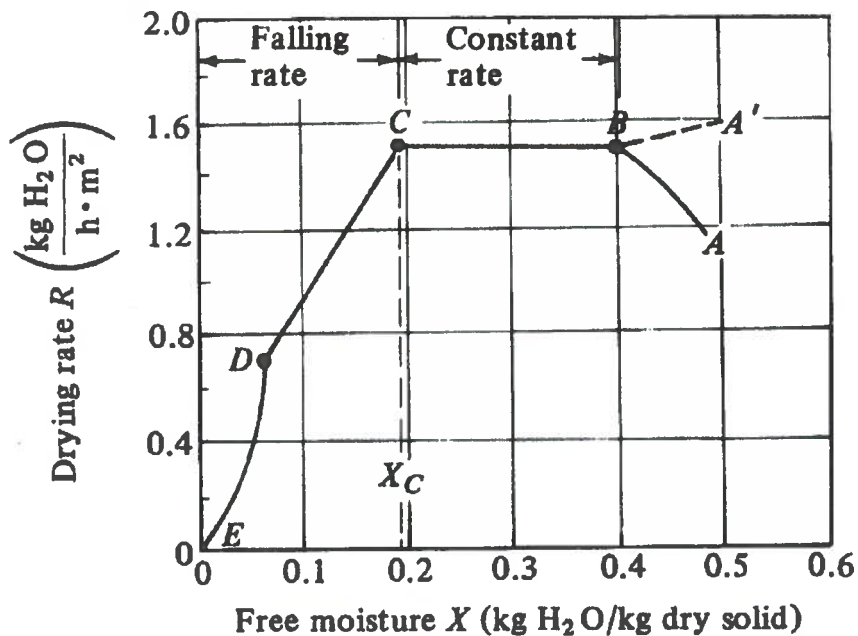
- The general drying equation is given below. Find from this the equations for time at constant drying rate and for falling drying rate.
- Air of temperature  $65^\circ\text{C}$  (dry bulb temperature) has a dew point of  $30^\circ\text{C}$ . We will use this air to dry some granulate (dog food). How much water ( $H$ ) does this air contain at start? What is the percentage humidity?
- We dry adiabatic till 90% humidity in the air at exit. What is now the temperature of the air?

Show in the attached humidity chart how you find the answers for d) and e) – the diagram shall be turned in with your answers.

- We will use a tray dryer with area  $2\text{ m}^2$ , and we will produce  $10\text{ kg}$  of the granulate. The granulate contains at start  $0.4\text{ kg H}_2\text{O/kg}$  dried material. We will use the given diagram below, but assuming that the line C-E is straight and goes through origo. Find the time it will take to dry the granulates down to  $0.05\text{ kg H}_2\text{O/kg}$  dried material which is the humidity content at equilibrium ( $X^*$ ). The critical water content ( $X_c$ ) is  $0.18\text{ kg H}_2\text{O/kg}$  dry material.

Given: 
$$R = -\frac{L_s}{A} \frac{dX}{dt}$$

Where  $L_s = \text{kg dry material}$ ,  $A = \text{drying area (m}^2\text{)}$ ,  $t = \text{drying time (h)}$



### Problem 3 Membrane gas separation (20%)

- (a) Make a sketch of a membrane with in- and out streams, and write the symbols on your sketch with respect to what is measured where. Use the same symbols as given in the equation below.
- (b) Oxygen enriched air is used in several applications. Two examples are breathing machine at a hospital, another example is for more efficient combustion.

A hollow fibre membrane with selective thickness of 1  $\mu\text{m}$ , is producing oxygen enriched air.

Permeability of  $\text{O}_2$  ( $P_{\text{O}_2}$ ) is  $1.109 \cdot 10^{-6} [\text{m}^3(\text{STP})\text{m}] / (\text{m}^2 \text{bar h})$ , and selectivity of  $\text{O}_2/\text{N}_2$  is  $\alpha = 5$ . Pressure on feed side is 2 bar, while permeate pressure is 0,2 bar. The membrane module is going to produce 2  $\text{m}^3(\text{STP})/\text{h}$  of 45vol%  $\text{O}_2$ . Permeate cut ( $\theta = q_p / q_f$ ) is 0,10. Calculate the composition of the retentate stream, the air flow into the membrane module and the necessary permeation area.

Use the “complete mixing model” (equation given below) – indicate any assumptions made.

- c) If you instead should produce high purity  $\text{N}_2$  (95 vol%), how would you choose to arrange your membrane separation? (Comment on feed pressure, pressure ratio, permeate cut and calculation procedure.) Calculation is not needed.

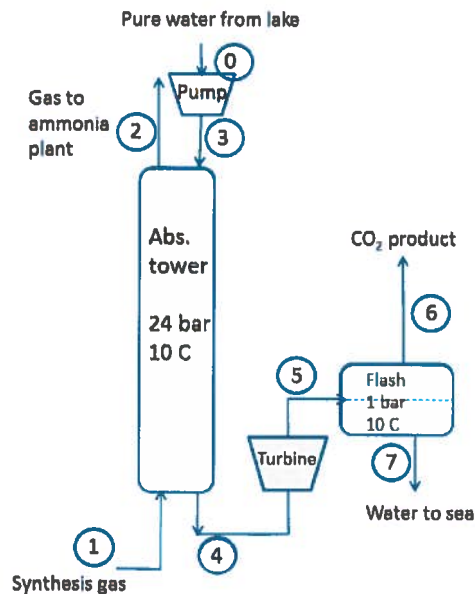
Given: Equation gas separation, complete mixing model:

$$\frac{q_A}{A_m} = \frac{q_p \cdot y_p}{A_m} = \left( \frac{P_A}{l} \right) (p_h x_0 - p_l y_p)$$

where  $q_A$  = permeate flux of component A ( $\text{m}^3(\text{STP})/\text{h}$ ),  $P_A$  is permeability (units given in the text),  $l$  = membrane thickness (m),  $A_m$  = permeation area ( $\text{m}^2$ ),  $p$  = trykk (bar),  $x_0$  and  $y_p$  mol fractions of component A

## Problem 2 (Absorption and equilibrium, 25%)

We want to look at CO<sub>2</sub>-absorption for ammonia production (this is the water wash tower («vannvask») mentioned in the lectures. The feed gas from the synthesis part of the plant is 6646 kmol/h and contains N<sub>2</sub> (approx. mol-20%), H<sub>2</sub> (approx. mol-60%), other inert gases and 17 mol-% CO<sub>2</sub> (stream 1), and we want to reduce the CO<sub>2</sub>-concentration in the gas which goes to ammonia production to 0.3 mol-% (stream 2). The water feed to the absorption column contains no CO<sub>2</sub> (stream 3).



- Henry's law is given below, and it can alternatively be written in the form  $y=mx$  where  $x$  is the mole fraction of CO<sub>2</sub> in water. Find  $m$  at 0C, 10C and 20 C when  $p=24$  bar and when  $p=1$  bar (you can make a table).
- What is the definition of the absorption factor  $A$ ? What assumptions are required for the Kremser equation? Do these assumptions hold in our case? Show that  $A$  can be written as a function of  $y_{N+1}$ ,  $y_1$ ,  $y^*_N$  og  $y^*_0$  (see formula and figure).
- Find the minimum water flow ( $L_{min}$ , stream 3) in kmol/h and in m<sup>3</sup>/h (with an infinite number of equilibrium stages).
- We use 10% more than the minimum water flow ( $L=1.1 L_{min}$ , stream 3). What is the fraction of CO<sub>2</sub>-fraksjonen in the water out ( $x_N$ , stream 4)? How many equilibrium stages ( $N$ ) are needed? You can compute  $N$  using the Kremser equation, but who also your solution in the  $xy$ -diagram (McCabe-Thiele).  
Comment: If you did not solve question (c) then use  $L=5000$  m<sup>3</sup>/h (stream 3).
- What is the composition in the gas out (stream 2) if  $N=50$ . Use the same values for  $L$  (stream 3) og  $x_N$  (stream 4) as in question (d).
- Independent question: What are the CO<sub>2</sub>-fractions ( $y,x$ ) in the streams out of the flash tank (streams 6 and 7). How much (in percent) of the original CO<sub>2</sub> ends up in the CO<sub>2</sub>-product (stream 6)?

Date are given below and in the figure. State any additional assumptions you make.

Some data (you do not need all of this):

Henry's law for CO<sub>2</sub> in water: Partial pressure is  $p_{CO_2} = H x_{CO_2}$  where  $H=719$  bar at 0C,  $H=1027$  bar at 10C,  $H=1402$  bar at 20C,  $H=1835$  bar at 30C, and  $H=2300$  bar at 40C.

Vapor pressure for water:  $p^{sat}=0.012$  bar at 10C and  $p^{sat}=1$  bar at 100C.

Heat of vaporization for water at 100C: 40.7 kJ/mol

Heat capacity for water: 4.18 kJ/kg,K (liquid) and 1.87 kJ/kg,K (gas).

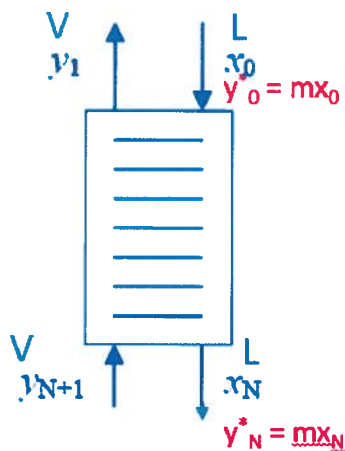
Heat capacity for CO<sub>2</sub>: 37 J/K,mol (gas)

Molecular weights [g/mol]: 44 for CO<sub>2</sub> and 18 for water

Density water: 1000 kg/m<sup>3</sup>

$R = 8.31$  J/K,mol

Kremser equations:



Book eq. (10.3-25):

$$\frac{y_{N+1} - y_1}{y_{N+1} - y_0^*} = \frac{A^{N+1} - A}{A^{N+1} - 1}$$

Alternative simpler form (Sigurd):

$$\frac{y_{N+1} - y_N^*}{y_1 - y_0^*} = A^N$$

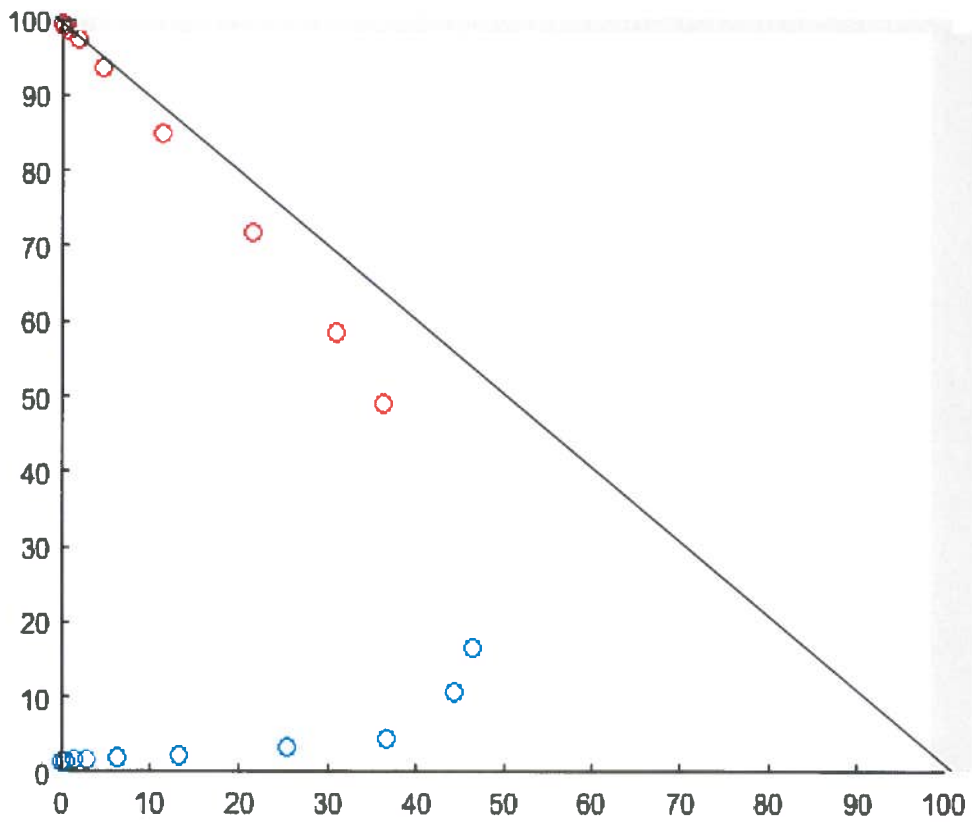
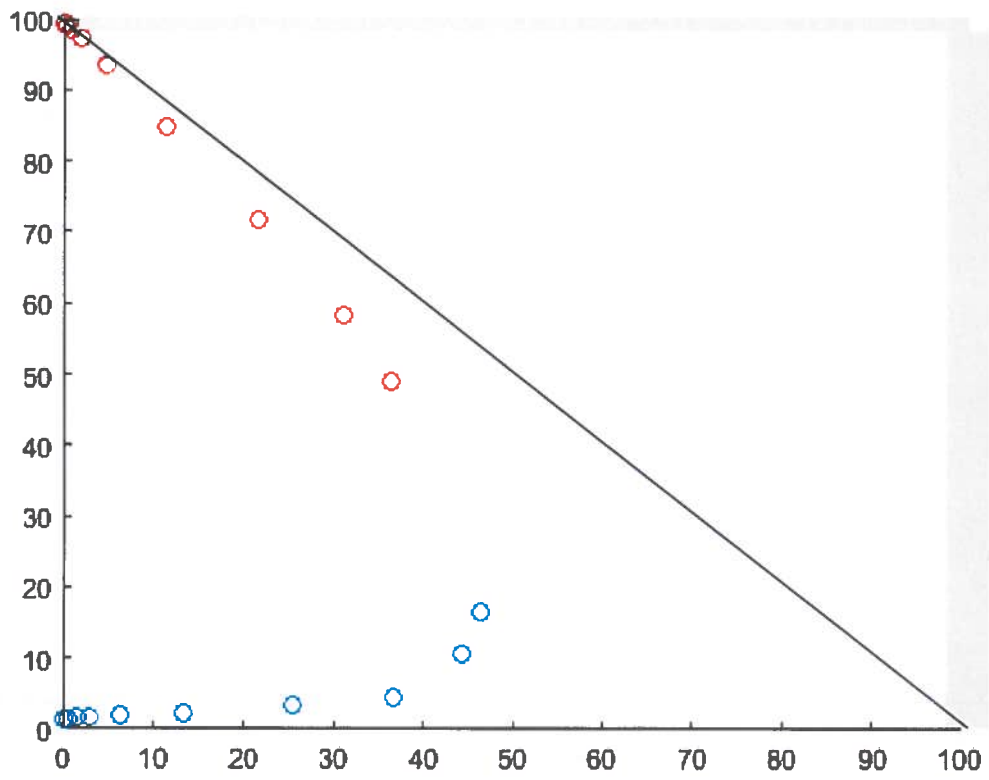
Get:

$$N = \ln \frac{y_{N+1} - y_N^*}{y_1 - y_0^*} / \ln A$$

Note. Can write:

$$A = \frac{y_{N+1} - y_1}{y_N^* - y_0^*}$$

- = in equilibrium with other phase  
(could be imaginary composition, like  $y_0^*$ )



# Humidity Chart

# APPENDIX 2

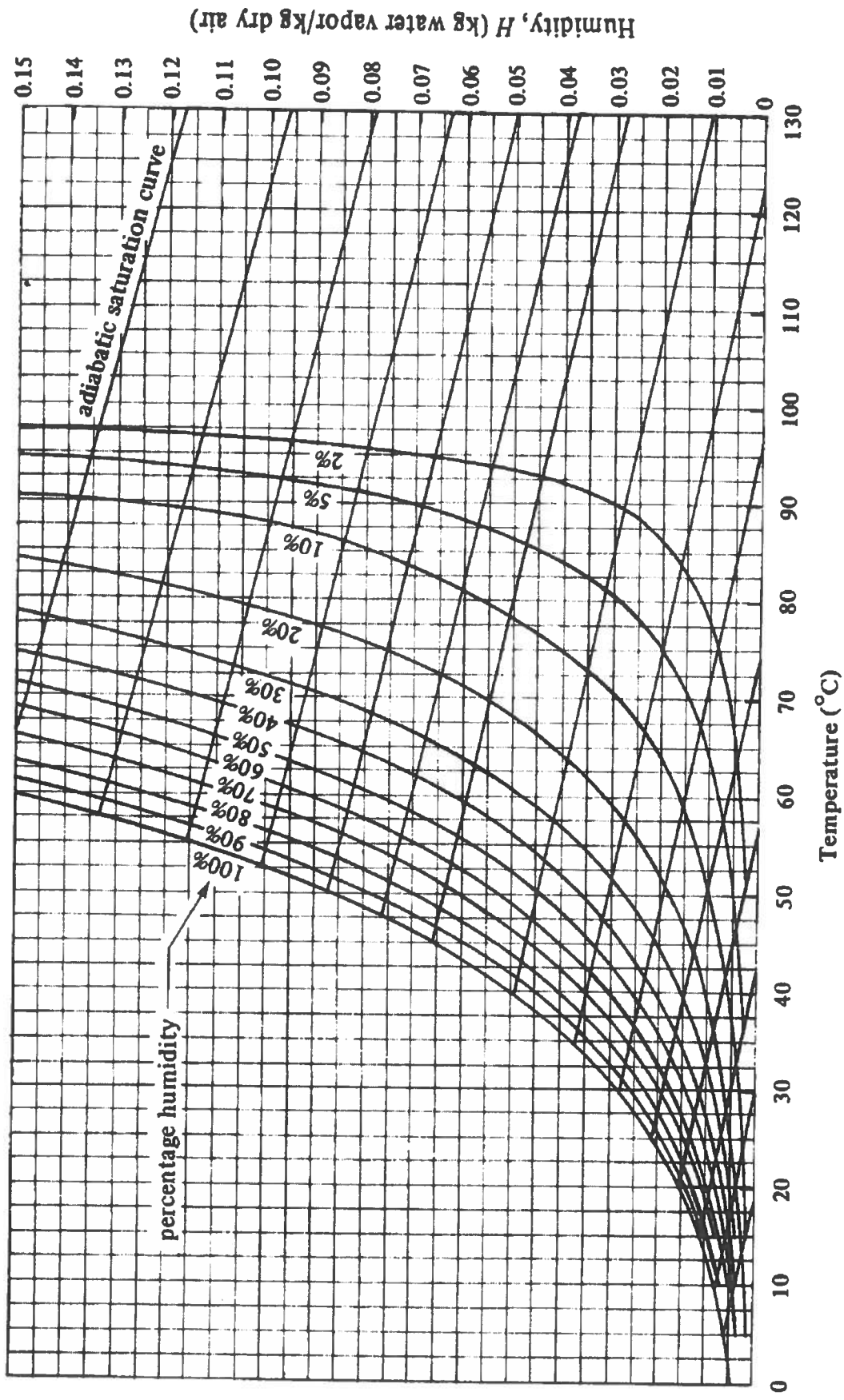


FIGURE 9.3-2. Humidity chart for mixtures of air and water vapor at a total pressure of 101.325 kPa (760 mm Hg). (From R. E. Treybal, Mass-Transfer Operations, 3rd ed. New York: McGraw-Hill Book Company, 1980. With permission.)