

# OTU-CFB boiler control design with the dynamic relative gain array and partial relative gain

## SUPPORTING INFORMATION

*Matias Hultgren<sup>\*,†,‡</sup>, Enso Ikonen<sup>†</sup>, Jenő Kovács<sup>†</sup>*

<sup>†</sup>Systems Engineering, University of Oulu, POB 4300, FI-90014 Oulun yliopisto, Finland.

E-mail: <sup>\*,†</sup>[hultgrenmatias@gmail.com](mailto:hultgrenmatias@gmail.com), <sup>†</sup>[enso.ikonen@oulu.fi](mailto:enso.ikonen@oulu.fi), <sup>†</sup>[jeno.kovacs@oulu.fi](mailto:jeno.kovacs@oulu.fi).

### Contents

**Table S1.** Steady-state gain effects in the OTU-CFB, normalized with the input maxima.

**Table S2.** The steady-state RGA matrix of the case 2 system, 5 input MVs and 5 output CVs.

**Table S3.** The steady-state RGA matrix of the case 3 system, 6 input MVs and 6 output CVs.

**Table S4.** The steady-state RGA matrix of the case 4 system, 8 input MVs and 8 output CVs.

**Table S5.** Time domain behavior of the main MVs from the APROS dynamic model. Results are normalized for each CV with respect to the largest MV (smaller percentage, shorter time).

---

<sup>\*</sup>Outotec, Kuparitie 10, PO Box 69, FI-28101 Pori, Finland, [matias.hultgren@outotec.com](mailto:matias.hultgren@outotec.com).

**Table S1.** Steady-state gain effects in the OTU-CFB, normalized with the input maxima.

	T.valve	FW	Fuel	Prim air	Sec air	Tot DSH	DSH 1	DSH 2	DSH 3	RHvalve	Firing power	Boiler load
<b>Steam p</b>	-1.0	0.04	0.2	-0.1	-0.1	0.04	0.04	0.03	0.03	0.1	0.2	0.2
<b>Steam T</b>	-0.2	-1.0	1.0	-0.4	-0.4	-1.0	-1.0	-1.0	-1.0	0.8	1.0	0.02
<b>Evap. T</b>	-0.4	-0.2	0.3	-0.2	-0.1	-0.1	-0.1	-0.1	-0.1	0.3	0.3	0.1
<b>FG O<sub>2</sub></b>	0.0	0.0	-0.0002	0.001	0.002	0.0	0.0	0.0	0.0	0.0	0.0	0.0
<b>FG T</b>	-0.1	-0.3	0.6	-1.0	-1.0	-0.2	-0.2	-0.2	-0.2	0.1	0.4	0.1
<b>SH2 T</b>	-0.3	-0.8	0.8	-0.3	0.04	-0.5	-0.8	-0.4	-0.3	0.8	0.8	0.02
<b>SH3 T</b>	-0.2	-1.0	1.0	-0.6	-0.2	-0.8	-1.0	-1.0	-0.4	0.9	1.0	-0.02
<b>RH T</b>	-0.1	-0.7	0.8	0.002	-0.3	-0.7	-0.7	-0.7	-0.6	-1.0	0.8	0.1
<b>Tot MW<sub>e</sub></b>	0.01	0.1	1.0	-0.2	-0.4	0.1	0.1	0.1	0.1	-0.3	1.0	1.0

**Table S2.** The steady-state RGA matrix of the case 2 system, 5 input MVs and 5 output CVs.

RGA	MV →	T.valve	DSH1	DSH2	DSH3	Boiler load
CV ↓	INDEX	1	2	3	4	5
<b>Steam p</b>	<b>1</b>	0.989	0.025	-0.011	-0.002	-0.002
<b>Steam T</b>	<b>2</b>	0.0006	-0.661	0.008	1.651	0.001
<b>SH2 T</b>	<b>3</b>	0.005	1.797	-0.796	-0.007	0.0007
<b>SH3 T</b>	<b>4</b>	0.002	-0.153	1.800	-0.649	-0.0001
<b>Tot MW<sub>e</sub></b>	<b>5</b>	0.003	-0.008	-0.001	0.006	1.000

**Table S3.** The steady-state RGA matrix of the case 3 system, 6 input MVs and 6 output CVs.

RGA	MV →	T.valve	FW	Fuel	Prim air	Sec air	Tot DSH
CV ↓	INDEX	1	2	3	4	5	6
<b>Steam p</b>	<b>1</b>	0.983	0.127	-0.012	0.025	-0.014	-0.109
<b>Steam T</b>	<b>2</b>	0.008	-0.643	0.055	-0.210	0.119	1.671
<b>Evap T</b>	<b>3</b>	0.017	1.806	0.040	-0.186	0.078	-0.756
<b>FG O<sub>2</sub></b>	<b>4</b>	0.000	0.000	-0.058	-1.205	2.263	0.000
<b>FG T</b>	<b>5</b>	-0.012	-0.349	0.028	2.664	-1.507	0.176
<b>Tot MW<sub>e</sub></b>	<b>6</b>	0.003	0.059	0.947	-0.088	0.062	0.018

**Table S4.** The steady-state RGA matrix of the case 4 system, 8 input MVs and 8 output CVs.

RGA	MV →	T.valve	FW	Sec air	DSH1	DSH2	DSH3	RHvalve	Firing
CV ↓	INDEX	1	2	3	4	5	6	7	8
<b>Steam p</b>	<b>1</b>	1.049	0.122	0.000	-0.118	-0.018	0.005	-0.025	-0.015
<b>Steam T</b>	<b>2</b>	-0.014	-1.102	-0.0002	-0.065	0.175	1.629	0.270	0.108
<b>Evap T</b>	<b>3</b>	-0.050	1.764	0.0002	-0.832	-0.052	0.051	0.077	0.042
<b>FG O<sub>2</sub></b>	<b>4</b>	0.000	0.000	1.001	0.0002	-0.0001	0.000	0.000	-0.001
<b>SH2 T</b>	<b>5</b>	0.001	-0.212	0.000	1.934	-0.785	-0.01	0.043	0.028
<b>SH3 T</b>	<b>6</b>	0.0005	-0.147	-0.0001	-0.053	1.819	-0.651	0.026	0.006
<b>RH T</b>	<b>7</b>	0.01	0.490	0.0001	0.130	-0.136	-0.031	0.629	-0.091
<b>Tot MW<sub>e</sub></b>	<b>8</b>	0.004	0.086	-0.001	0.004	-0.002	0.006	-0.020	0.924

**Table S5.** Time domain behavior of the main MVs from the APROS dynamic model. Results are normalized for each CV with respect to the largest MV (smaller percentage, shorter time).

Normalized times	Turbine valve			Firing power			Feedwater flow		
	Rise time	Settling time	Time delay	Rise time	Settling time	Time delay	Rise time	Settling time	Time delay
<b>Main steam p</b>	5	26	0	100	100	67	0.4	89	100
<b>Total MW<sub>e</sub></b>	0.01	33	0	100	100	0	0.1	90	0
<b>Main steam T</b>	100	100	0	74	82	60	83	94	100
<b>Evaporator T</b>	17	60	0	100	100	100	96	95	50