# Calibration Method for 2-Dimensional Laser Scanner Attached on a Robot Vehicle 

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#### Abstract

The objective of this study was to develop a calibration method to get the exact position of the 2-dimensional laser scanner mounted on the front of an automated vehicle from a reference coordinate system before the automatic navigation in an orchard application. The research was limited only in calibrating a 2-dimensional laser scanner that gathers distance and angle data of the objects in front of it. The methods used in this research were Hough transform, Euler rotation theorem and LSM (least squares method). The calibration results identified the exact attachment position of the laser scanner with respect to the vehicle coordinates. Finally, field test runs for autonomous guidance with developed calibration was conducted to confirm the travel accuracy improvement. The accuracy of both lateral and heading error for calibrated sensor was higher than run of subjected calibration.


## 1. INTRODUCTION

Calibration of any sensors attached onto the vehicle or equipment is necessary to obtain environment information. After the installation of the sensor, it is necessary to check if the sensor is aligned or centered properly with respect to the reference axes. For sensors such as a video cameras, a laser range finder, an ultrasonic sensor, a 2-d laser scanner and a GPS (global positioning system) etc., the position and orientation of the sensor affects the geometric interpretation of its measurements (Pless et al., 2003).

LMS (laser measurement sensors) are a popular method for acquiring optical measurement data of the objects in any position due to their accuracy. In order to maximize the range accuracy and to have correct data acquisition, a proper calibration method has to be applied. However, calibration of sensors is a not an easy task. The determination of the fitting algorithm method alone is time-consuming not to mention the choice of the appropriate auxiliary equipment that would ensure ideal data. One thing to consider is the cost of engineering equipment to be used in calibration. Engineering costs arise from both expensive components and difficult calibration requirements (Davis et al., 2001). A laser range scanner designed for minimum calibration complexity (Davis et al., 2001) used a laser triangulation scanners method for acquiring three-dimensional geometry of the objects due to their accuracy and robustness. In said method, two-camera range scanner design was utilized to minimize calibration complexity and cost, and eliminates all actuated components from the calibrated geometry. In this research essential equipment were used to calibrate the laser scanner such as the RTK-GPS (real-time kinematic global positioning system), a

FOG (fibre optic gyroscope), and total station. Nowadays, these sensors are getting inexpensive due to popular demand and due to its efficiency in yielding optimal calibration results. Usually, the choice of the engineering equipment to use for the scanner calibration is subject on the institutions' availability of the resources.

In this research, the developed method for the calibration of laser scanner attachment position did not utilize a calibration platform compared to other methods. Posture estimation for autonomous weeding robots navigation in nursery tree plantations (Khot et al., 2005) used a calibration platform to calibrate the attachment position of the sensor. This calibration platform consists of a fabricated steel track where the calibration method is performed for the prototype robot vehicle. The advantage of using prototype robot vehicle is that the calibration platform model is not big enough to construct. But in this research, it is not advisable to make a calibration platform because the robot tractor is too big and the construction cost is expensive. A new calibration method was developed and introduced in this research using a unique technique. The unique technique used in this research is the use of the perpendicular wall. This perpendicular wall served as the reference line for the laser scanner calibration.

The main thrust of the study is to develop a calibration method to obtain the actual laser scanner attachment position which will soon be used to correct the data outputs in an autonomous navigation of the robot tractor. The attachment position of the laser scanner is called offset position values. These offset position values of the laser scanner are important to know because it will determine if the sensor attachment is properly aligned or centered with respect to reference axes.

The developed calibration method for obtaining the laser scanner attachment position used three essential sensors, FOG which served as the heading sensor. The function is to obtain the relative heading direction of the robot tractor. A RTKGPS receiver was used as the positioning sensor to get the absolute position of the robot tractor. And, a total station was used to obtain the relative position ( $x, y$ and $z$ axes) of the perpendicular wall. A total station is an optical instrument used in modern surveying as well as by police, crime scene investigators, private accident reconstructionist and insurance companies to take measurements of scenes (Wikipedia, The Free Encyclopedia). The perpendicular wall is wall perpendicular to the GPS antenna which is mounted on the top of the cabin of the robot tractors' centre of gravity and the laser scanner which is attached on the front of the robot tractor, served as the reference line to obtain the exact attachment position of the laser scanner with respect to the reference axes. The methods used in this research were Hough transform to recognize the perpendicular wall as straight line, Euler rotation theorem to transform the perpendicular wall relative coordinates into UTM (universal transverse Mercator) coordinates, LSM (least square method) to get the scanning offset error of the laser scanner which is the laser scanner exact attachment position.

## 2. RESEARCH COMPONENTS

This research used a $56-\mathrm{kW}$ standard tractor, which was modified into a robot tractor. The robot tractor controlled steering, transmission (forward, neutral and backward), PTO (power take-off), engine speed, brake system and three-point hitches (up and down). The LMS 291 is the laser scanner to be calibrated, (SICK AG, Division Auto Indent). Figure 1a shows the LMS 291 and scanning basic principles. The figure shows the scanning angle direction is counter clockwise and area monitoring which means that an infringement of a field, e.g. by an object, leads to a switching signal at an output. The sensor was set to 80 m distance range, 1 deg angle resolution and 13 ms response time. Figure 1 b shows the laser scanner attachment position in front of the robot tractor. It has a distance error of $+/-5 \mathrm{~cm}$. The advantages of using the laser scanner as the navigation sensor are rapid scanning times thus measurement objects can move at high speeds, no special target-object reflective properties necessary, no reflectors and no marking of the measurement objects necessary, backgrounds and surroundings do not have any influence on the measurements, measurement data is available in real time and can be used for further processing and completely weatherproof variants.

(a) Laser scanner (LMS 291) and scanning basic principles

(b) Attachment position of laser scanner

Fig. 1. Laser scanner basic principles and position attachment
The three essential sensors used to calibrate the laser scanner were the RTK-GPS receiver (MS 750 dual frequency RTK receiver, Trimble Navigation Ltd.). The MS 750 GPS receiver was preferred to use in this research because it has the highest level of accuracy and response available to receive information and it is specially designed to allow the easy integration of reliable-level positions to any guidance or control application. In the experiment run, the RTK-GPS receiver input was set to 1 Hz and the output was set to 10 Hz . It has a positioning accuracy of $+/-2 \mathrm{~cm}$. The FOG, (JG35FD, Japan Aviation Electronics Industry, Ltd.) was used as the heading sensor. This sensor obtained the heading angle necessary for the calibration method during the experiment run. The sensor drift angle accuracy is $+/-0.5 \mathrm{deg} / \mathrm{hour}$. And, the total station (APL-1, TOPCON Ltd.) used as the positioning sensor to obtain the relative position ( $x, y$, and $z$ axes) of the perpendicular wall with an accuracy of $+/-3 \mathrm{~mm}$ for fine mode and $+/-10 \mathrm{~mm}$ for course mode. The total station was set to fine mode setting. All sensors are connected to the laptop PC using RS-232 cable.

## 3. METHODS

### 3.1 Hough transform sampling

The Hough transform used in this research as the algorithm to recognize the perpendicular wall as a straight line. It was patented by Paul V. C. Hough in 1962. It used for linear or circular detection. The main advantage of using Hough transform compared to commonly used method like least squared error method of fitting lines to image data, is that even if group points varies to some extent, asking for a straight line is possible. Also, processing is collectively possible even when there are two or more straight lines in the image data. The point which has the majority of intersection served as the line equation. The disadvantage, on the other hand, is that in order to plot curves (i.e. sinusoids) for every observing point $\left(x_{i}, y_{i}\right)$ in Cartesian image space to $r-\theta$ polar Hough parameter space, the load of computational complexity is large.

Consider the normal Cartesian equation of a straight line, which is generally on an $x-y$ plane,

$$
\begin{equation*}
y=m x+c \tag{1}
\end{equation*}
$$

where $m$ is the slope and $c$ is the $y$-intercept. Consider some points of the image data where a straight line can be obtained from its edge. Transform the points into $r$ - $\theta$ normal representation of a line in Hough space (only points where the line pass through) which was shown in Fig. 2a. The shortest distance from the origin can be obtained equivalent to (2) (Gonzales \& Wood et al., 1993).

$$
\begin{equation*}
r=x \cos \theta+y \sin \theta \tag{2}
\end{equation*}
$$

In Eqn (2), the line is defined in terms of $r$ and $\boldsymbol{\theta}$, where $r$ is shortest distance from origin to line and $\theta$ is the orientation angle with respect to the $x$-axis. For any point $(x, y)$ on this line, $r$ and $\theta$ has a constant value. Equation (2) can be considered a relation between the coordinates $(x, y)$ of some points in the edge image, and the value of the parameters $(r-\theta)$ which defines the equation of the line. The points in Cartesian space correspond to a sine wave $r$ - $\theta$ polar in Hough parameter space shown in Fig. 2b. In Fig. 2b, the points where the majority of these sinusoids intersect serve as the equation of the line. The value of distance $r$ is equivalent to 0.1 unit and the angle $\theta$ is equivalent to -40 deg . The equation of the line is $y=1.1978 x+0.1392$.

(a) $r$ - $\theta$ space normal representation of a line in Hough transform

(b) Points transform to sinusoids in $r-\theta$ space

### 3.2 Perpendicular wall recognition as a straight line using Hough transform

Applying the Hough transform to the data obtained by the laser scanner during the calibration experiment run, the perpendicular wall was recognized as a straight line. The perpendicular wall will serve as the base line for the laser scanner calibration. Figure 3 shows the perpendicular wall and the total station visual representation.
$r_{i, j}=d_{i} \cos \left(\phi_{j}-\theta_{i}\right) \quad(0 \leq i \leq 180,0 \leq j \leq 180)$

In (3), $r_{i, j}$ is the shortest distance between the laser scanner and the perpendicular wall, $d_{i}$ is the actual distance between the perpendicular wall and the laser scanner, $\theta_{i}$ is the relative angle of the perpendicular wall with respect to laser scanner detection, and $\phi_{j}$ is the deflection angle between the perpendicular wall and the vehicle direction. The main advantage of the $r-\theta$ is that quantization is relatively easy because not all the parameter space needs to be considered. Looking at Fig. 2b, the sinusoids all have the same period, and therefore $\theta_{i}$ can be limited to any angle range depending on the application without losing its generality. In this research, the $\theta_{i}$ limit was $0 \leq i \leq 180$ and $\phi_{j}$ limit was $0 \leq j \leq 180$.


Fig. 3. Outline on how to recognize the perpendicular wall as straight line using the Hough transform

Figure 4a shows the actual captured points of the laser scanner on the surface of the perpendicular wall. The black points represent the wall and the black line corresponds to the estimated line. Transforming the data obtained by the laser scanner into a $r-\theta$ parameterization space shown in Fig. 4b using the Hough transform, a cluster of intersections were intersected. The majority of intersections served as the equation of a line of the perpendicular wall.

Fig. 2. Basics of Hough transform

(a) Actual captured points by the laser scanner in a computer window

(b) Illustration of the captured points of the laser scanner transform to sinusoids in $r-\theta$ space

Fig. 4. Transformation of the captured points using Hough transform

### 3.3 Transformation of local coordinates to UTM coordinates

The perpendicular wall relative position ( $x, y$ and $z$ axes) was measured by the total station (surveying instrument) and then the starting edge point absolute position was measured by RTK-GPS. After determining the perpendicular wall as a straight line using the laser scanner, next is to transform the relative position into absolute position by using Euler rotation theorem. In this method, the rotation is about the $z$-axis in counter clockwise direction. Equation (4) shows the rotation matrix in $z$-axis.
$\mathbf{R}_{z(\rho)}=\left[\begin{array}{cc}\cos \rho & -\sin \rho \\ \sin \rho & \cos \rho\end{array}\right]$
In the equation, $\rho$ is the rotation angle in deg, can be obtained in the perpendicular wall angle in the UTM coordinates. Equation (5) calculated absolute position of the perpendicular wall.
$\left[\begin{array}{l}E_{s} \\ N_{s}\end{array}\right]=\mathbf{R}_{z(\rho)}\left[\begin{array}{l}x_{s} \\ y_{s}\end{array}\right]+\left[\begin{array}{c}E_{o} \\ N_{o}\end{array}\right]$

Where the $\left(E_{s}, N_{s}\right)$ is the transformed position in UTM coordinates, $\left(x_{s}, y_{s}\right)$ is the relative position of the
perpendicular wall taken by the total station, and $\left(E_{o}, N_{o}\right)$ is the starting edge point of the perpendicular wall.

### 3.4 Determination of the offset position of the laser scanner using LSM

The next method to be explained is the determination of the offset position values of the laser scanner attached on the front of the robot tractor. The offset position values are between the laser scanner and the GPS antenna which was shown in Fig. 5. In the figure, $a$ and $b$ are the laser scanner offset values ( $x$ and $y$ axes) in m and the $\delta$ is the offset angle of the laser scanner in deg at the vehicle coordinate system, respectively. The center point of the laser scanner from perpendicular wall is denoted by $E$ in m . The value of $E$ can be computed from the data obtained by the laser scanner in distance $(d)$ and angle $(\theta)$ using Hough transform using (3). The values of the distance $(E)$ depend on the equation of the perpendicular wall obtained previously by the laser scanner recognition as a straight line. The distance from the GPS antenna to the perpendicular wall is denoted by $D$ in m . To solve the distance $(D)$, the straight line equation of the perpendicular wall is needed in UTM coordinates by using (6).
$\alpha x+\beta y+c=0$
Using the perpendicular distance relation between the perpendicular wall and GPS antenna the distance $(D)$ can be solved by (7).


Fig. 5. Calibration method outline using a perpendicular wall as the reference line for getting the laser scanner exact position
$D=\frac{a b s|\alpha x+\beta y+c|}{\sqrt{\alpha^{2}+\beta^{2}}}$

The angle $(\psi)$ between the perpendicular wall and vehicle coordinate system is given by

$$
\begin{equation*}
\psi=\eta-v \tag{8}
\end{equation*}
$$

Where $\eta$ is the angle of the vehicle direction in deg with respect to the UTM coordinate and $\boldsymbol{\nu}$ is the angle of the perpendicular wall in deg with respect to the UTM coordinate. The equation for solving the offset angle $\delta$ of the laser scanner is shown in (9).
$\delta=\kappa-\psi$
Using the Hough transform, $\kappa$ is the angle between the laser scanner's exact position in deg and the perpendicular wall, computed from the data obtained by the laser scanner during the calibration experiment run.

Since distance $(E)$ and distance $(D)$ exists on the straight line, the position of the laser scanner can be calculated using (10) in vehicle's coordinate system.
$a \cos \psi+b \sin \psi=E-D$
However, $E-D$ values have measurement errors. Through using the least squares method (Downie and Heath, 1984), the minimum errors were obtained. The error was acquired by $i$ in a straight line in $n$ value of observation as

$$
\begin{equation*}
a \cos \psi_{i}+b \sin \psi_{i}+D_{i}-E_{i}=0 \tag{11}
\end{equation*}
$$

Assigning the $F_{i}$ as
$F_{i}=D_{i}-E_{i}$
Using LSM, the minimum error $\left(E_{i}\right)$ can be calculated in (13).
$E_{i}^{2}=\left(a \cos \psi_{i}+b \sin \psi_{i}+F_{i}\right)^{2}$
Solving for the least square estimates by summing of all observation data:
$S_{\varepsilon}=\sum_{i=0}^{n} E_{i}^{2}$
Using partial derivatives, the minimum error can be calculated in (16) and (17) which are set to 0 .

$$
\begin{align*}
& \frac{\partial S_{\varepsilon}}{\partial a}=\sum_{i=0}^{n}\left(2 a \cos ^{2} \psi_{i}+2 b \cos \psi_{i} \sin \psi_{i}+2 \cos \psi_{i} F_{i}\right)=0  \tag{15}\\
& \frac{\partial S_{\varepsilon}}{\partial b}=\sum_{i=0}^{n}\left(2 b \cos \psi_{i} \sin \psi_{i}+2 a \sin ^{2} \psi_{i}+2 \sin \psi_{i} F_{i}\right)=0 \tag{16}
\end{align*}
$$

The values of the offset position of the laser scanner were $a=$ - $0.056 \mathrm{~m}, b=2.57 \mathrm{~m}$ and $\delta=2.8 \mathrm{deg}$ from the northing UTM coordinates.

## 4. RESULTS AND DISCUSSION

### 4.1 Determined offset position values of the laser scanner

Before the laser scanner was attached in front of the automated vehicle, a measurement was made to know the attachment position of the laser scanner in front of the automated tractor. The purpose of this measured position was to insure that the laser scanner was attached properly in front of the automated tractor. This attachment position of the laser scanner is a subjective calibration because the installation is only depended on the person who installed the laser scanner. In order to verify whether it was attached properly/centered to the centreline of the tractor the offset position values should be obtained. To obtain the offset position values of the laser scanner different algorithms-- Hough transform, Euler rotation theorem, and LSM were used. A unique technique was also used to obtain the offset position values. This technique was the utilization of the perpendicular wall as the reference line to develop calibration method for the laser scanner attachment position. The developed calibration method determined the offset position values of the laser scanner. These values were the exact location on the robot tractor attachment position and proved that the attachment position of the laser scanner was not properly aligned or centered with the reference coordinate. This condition justifies the need for the calibration of the laser scanner and it is very important to implement because of the effect on the evaluation accuracy on any system. In this research, the offset position values will be used in the accuracy evaluation to correct the data obtained by the laser scanner in an autonomous navigation orchard application.

Hough transform has possible errors during the linear and circular detection. In this research, errors for linear detection were not considered because the errors were minimal and it wouldn't affect the accuracy of the calibration. But in circular detection, the errors should be considered.

### 4.2 Evaluation of the autonomous run outputs with developed calibration and with subjective conjecture calibration

The laser scanner attachment position in front of the automated vehicle was mounted by subjective calibration in which the attachment position was conjectured in the reference axes. In order to see the effect of the presence or the absence of the laser scanner calibration in accuracy evaluation of the autonomous navigation, a series of autonomous runs were conducted. The experiment runs were conducted in the Hokkaido University, Sapporo, Japan. The selected test site was approximately 40 m by 3 m in length and width. The area which resembled an orchard was spanned with trees in two vertical rows. Figure 6 shows the accuracy evaluation of autonomous navigation with developed calibration and with subjective calibration. In the figure, the black line represents the data with subjective calibration and the broken line represents the data with developed calibration. This research shows the effect of not calibrating the laser scanner was that the accuracy errors tend to increase and the subjective
conjecture calibration is not enough to do in attachment position of the any sensor.


(b) Heading error in autonomous run

Fig. 6. Comparison of lateral and heading errors with and without the developed calibration

The RMS (root mean squared) errors in terms of lateral and heading mean error that was calibrated using the developed method is relatively small compared to the data that was calibrated using subjective calibration. Table 1 shows the RMS mean error results with developed calibration and with subjective calibration. Also, the data that was calibrated by the developed method were the actual data taken by the laser scanner because it is aligned with the reference coordinate axes of the robot tractor.

## Table 1. Evaluated accuracy results of the autonomous run in orchard application with and without the developed calibration

| Root mean squares (RMS) mean error |  |  |
| :---: | :---: | :---: |
|  | with calibration | without calibration |
| lateral error, $m$ | 0.21 | 0.22 |
| heading error, deg | 2.7 | 3.9 |

## 5. CONCLUSION

The research developed an attachment calibration method for a 2-d laser scanner attached on the front of the robot tractor
before the orchard autonomous application. The developed calibration method determined the position of the laser scanner in robot tractor coordinates using the reference coordinate. The reference coordinate was GPS antenna location. Hough transform recognized the perpendicular wall as a straight line and also obtained the distance between the perpendicular wall and the laser scanner centerpoint, Euler rotation theorem transformed the perpendicular wall relative position to UTM coordinates, and LSM determined the minimum measurement errors in the laser scanner data acquisition which were the offset position values. And also, the utilization of the perpendicular wall was the technique help in determining the attachment position of the laser scanner. The offset position values of the laser scanner were a $=-0.056 \mathrm{~m}, \mathrm{~b}=2.57 \mathrm{~m}$ and $\delta=2.8 \mathrm{deg}$ from the tractor's $y_{0}$ axis. The developed calibration method was used to correct data obtained of the laser scanner in the autonomous navigation on orchard application.

## REFERENCES

Davis, J. and X. Chen (2001). A laser range scanner designed for minimum calibration complexity. In: Proceedings of the Third International Conference on 3D Digital Imaging and Modelling, 91-98.
Downie, N. and R. Heath (1984). Basic statistical method. Harper \& Row, Publishers, Inc., New York.
Gonzales, C. and E. Woods (1993). Digital Image Processing. Addison-Wesley Publishing, USA.
Khot, L., L. Tang, S. Blackmore and M. Norremark (2005). Posture estimation for autonomous weeding robots navigation in nursery tree plantations. In: Proceedings of the ASAE Annual Meeting. Paper number 053092.
Pless, P., Zhang, Q. 2003. Extrinsic auto-calibration of a camera and laser range finder. Department of Computer Science and Engineering, Washington University, St. Louis.
Wikipedia, The Free Encyclopedia. http://en.wikipedia.org/wiki/Total_station. January 10, 2008.

