

## Innovated Food Design Visualized in the Nonlinear Analysis of Multi-functional Water Species Based on the Specified Physicochemical Parameters

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### Abstract

An innovated food design was challengingly studied in the course of the nonlinear analysis of multi-functional water species by using a drying process of Japanese squid at 30 ~ 60°C. An optimal design of the drying process requested was effectively visualized by using four physicochemical parameters as a function of the three multi-functional water species. The three water species were clearly distinguished as species-A<sub>1</sub> (weakly restricted-water species), species-A<sub>2</sub> (strongly restricted-water species) and species-A<sub>2</sub>' (unfrozen-water species), all of which were exactly characterized by the four physicochemical parameters. The four parameters were individually evaluated as effective diffusivity ( $De$ ), activation energy of  $De$  ( $E_D$ ), correlation time ( $\tau_C$ ) derived by a proton NMR technique, and bacterial growth rate coefficient ( $m$ ). Species-A<sub>1</sub> was described by a higher  $De$ , lower  $E_D$ , lower  $\tau_C$ , and higher  $m$ . Species-A<sub>2</sub> was characterized by widely distributed values of  $De$ ,  $E_D$ , and  $\tau_C$ , and  $m=0$ . Species-A<sub>2</sub>' was suddenly recognized in the course of temperature decrease at -15°C, accompanying a hysteresis of the Arrhenius plot of  $1/\tau_C$  and new activation energy for the rotation rate of water molecule. All the dehydration curves obtained were sufficiently simulated by a proposed water tank model.

keywords: Three water species, bacterial growth coefficient, effective moisture diffusivity ( $De$ ), activation energy of  $De$ , hysteresis of correlation time

### Nomenclature

$A_I - A_{III}$	constants designated by Eqs. (10)-(12) ( - )
$De$	effective moisture diffusion coefficient (m <sup>2</sup> /h)
$De^0$	frequency factor of moisture diffusivity (m <sup>2</sup> /h)
$E_D$	activation energy of moisture diffusivity (kJ/mol)
$E\tau_C$	activation energy of water molecule rotation (kJ/mol)
$f_s$	proportion of strongly restricted-water (=1 - $f_w$ ) ( - )
$f_w$	proportion of weakly restricted-water ( - )

$k_S$	dehydration constant for strongly restricted-water ( $h^{-1}$ )
$k_W$	dehydration constant for weakly restricted-water ( $h^{-1}$ )
$I$	nuclear spin quantum number of water proton (=0.5) (--)
$L_a$	half distance of a-axis of the rectangular sample (m)
$L_b$	half distance of b-axis of the rectangular sample (m)
$L_c$	half distance of c-axis of the rectangular sample (m)
$m$	bacterial growth rate coefficient ( $h^{-1}$ )
$r$	proton-proton distance of water molecule (=0.16nm)
$T$	squid sample temperature for the proton NMR technique ( $^{\circ}C$ )
$T_2$	spin-spin relaxation time of water proton (s)
$T_D$	drying temperature ( $^{\circ}C$ )
$t$	drying time (h)
$W$	moisture content at the drying time $t$ (%-d.b.)
$W_0$	initial moisture content at the time of PUP operated (%-d.b.)
$W_D$	initial moisture content of drying flesh sample (%-d.b.)
$W_e$	equilibrium moisture content (%-d.b.)
$W_{R1}$	moisture content ratio of region I at $W_0 > 120\%$ -d.b. (%-d.b.)
$W_{R2}$	moisture content ratio of region II at $W_0 < 120\%$ -d.b. (%-d.b.)

#### Greek letters

$\beta_1 - \beta_3$	constants ( $h^{-1}$ )
$\beta'_1 - \beta'_3$	constants ( $m^{-2}$ )
$\pi$	the ratio of the circumference of a circle to its diameter (=3.14)
$\gamma$	gyromagnetic ratio of proton (=2.675 $\times 10^8$ rad $\cdot T^{-1} \cdot s^{-1}$ )
$\tau_C$	correlation time of water proton (s)
$\hbar$	modified Plank's constant (=6.63 $\times 10^{-34}$ J $\cdot s$ )
$\omega_0$	resonance frequency (=3.14 $\times 10^9$ s $^{-1}$ )

## 1. Introduction

For optimal design of food to store it for a long time, an appropriate drying process and freezing process are strongly requested. In the two processes, as is well known, moisture distributed in the food matrix is one of the most important substrates which sensitively regulate to quality of food. The state of the moisture is multi-functionally and dynamically varied depending on a kind of foods and moisture content of foods. A large number of researchers have studied the moisture states in the foods indicating variety of the states such as gaseous water (Waananen and Okos, 1996), free water (Rockland and Nishi, 1980; Caurie, 1971), weekly restricted water, strongly restricted water, unfrozen water, multilayered water and bound water (Rockland and Nishi, 1980). Konishi and Kobayashi (1999; 2001(a); 2001(b)) demonstrated two different moisture content regions of food (regions I and II) in which variety of water species was distributed such as mobile liquid-water and gaseous water, by using a drying operation of a fish past sausage used as a model food. The two species were clearly distinguished at a specified moisture content of 100%-d.b., indicating the mobile water to be weekly restricted water species at  $W_0 > 100\%$ -d.b.(region I) and the gaseous water to be available at  $W_0 < 100\%$ -d.b.(region II). The effective diffusivity ( $De$ ) of the two species demonstrated a

characteristically different behavior as a function of moisture content of the sausage.  $De$  of the mobile water was fallen in the range of  $1.3 \times 10^{-6} \sim 2.1 \times 10^{-6} \text{ m}^2/\text{h}$  and the gaseous water gave  $De = 1.3 \times 10^{-6} \text{ m}^2/\text{h}$  at  $T_D = 35^\circ\text{C}$ . The activation energies ( $E_D$ ) of the effective moisture diffusivity for the two species were also evaluated as 16.5kJ/mol for the mobile water and 9.6kJ/mol for the gaseous water. From these evidences obtained, one can recognize that the dried foods are effectively used to examine a variety of multifunctional water species and characterized by the two parameters,  $De$  and  $E_D$ .

To quantitatively distinguish the multifunctional water species distributed in food body matrix, proton NMR method has commonly been used and demonstrated interesting evidences. Yano, Tanaka, Suzuki and Kanzaki (2003) demonstrated, using two  $^1\text{H}$ -NMR relaxation methods, two different characteristic behavior of water species depending on the two different freezing temperature regions,  $-1 \sim -5^\circ\text{C}$ (region-A) and  $-13 \sim -28^\circ\text{C}$ (region-B), by employing a bamboo shoot, potatoes, and a cod. In the region-A, the amount of the mobile water was a rate determining factor for the freezing behavior whereas, in region-B, the mobility of water molecule was an important factor. The results obtained strongly suggest that the moisture state is sensitively changed depending on the freezing temperature region. One may recognize that the proton NMR method is a useful tool to evaluate the moisture state in food, and the correlation time ( $\tau_C$ ) derived from the NMR method is an important parameter.

In the course of food design process, as is well known, bacterial growth brings difficult problems to keep the food in a good quality. The bacterial growth rate is strongly influenced by moisture content and the state of water molecule (Heiss and Eichner, 1971), suggesting that the state of water species strongly contributes to the bacterial growth rate coefficient ( $m$ ) in food.

For the design of food quality in the course of drying operation, computer simulation technique can effectively be used to evaluate dehydration curves obtained. Overhults, White, Hamilton and Ross (1973) simulated the dehydration response curves for a soybean drying process at  $37.8 \sim 104.4^\circ\text{C}$  using an exponential equation developed by Page (1949). Shepherd and Bhadwaj (1988) examined a single-term diffusion model to describe the thin layer drying characteristics of the whole pigeon pea. Ezeike and Otten (1991) proposed a two-term exponential model for the drying of unshelled melon seeds. In our previous papers (Konishi and Kobayashi, 2001(a) and 2001(b); Konishi, Horiuchi and Kobayashi, 2001(a) and 2001(b)), a water tank model was proposed as a mathematical model to describe the dehydration curves of a fish past sausage. The generalized application of the models proposed to various kinds of foods is, however, still unclear.

The objectives of this study are, employing a Japanese squid as a model food, (1) to distinguish the multifunctional water species by using specified physicochemical parameters as effective diffusivity ( $De$ ) and activation energy of the diffusivity ( $E_D$ ), (2) to apply a proton NMR method for the evaluation of the multifunctional water species using correlation time ( $\tau_C$ ), (3) to demonstrate a further discrimination of the

multifunctional water species by using the bacterial growth rate coefficient ( $m$ ), and (4) to simulate the dehydration curves obtained using the water tank model.

## 2. Experimental Procedure

For a model sample, a Japanese common squid (50mm square and  $8\pm 1.5$ mm in thickness, initial moisture content of 300 ~ 360%-d.b. (dry base,  $W_D$ )) was used. Through all the drying operation, drying air with a flow rate of 0.7m/s was introduced into a drying room passing through a rectifiable compartment with regulating the humidity. The drying temperature was electrically controlled within  $\pm 2^\circ\text{C}$  at given temperatures. The sample was placed in a stainless steel net basket (10 meshes) that was mechanically hung from a strain gage transducer in the dryer. During the drying process, a poultice-up process (designated as PUP) was operated to keep the moisture distribution in the squid sample uniform. For the PUP, the samples were stored in an incubator for 36h, the temperature of which was regulated at  $2^\circ\text{C}$ . The PUP was operated at a given moisture content ( $W_0$ ) in the range of 15 ~ 360%-d.b. The sample weight was continuously recorded by the output of a strain-gage transducer using a data-logger. Thirty, 40, and  $50^\circ\text{C}$  were chosen as the drying temperatures ( $T_D$ ). In the present drying conditions, it was previously reconfirmed that all the drying operations for the squid were within a falling-rate period.

For the readsorption of water molecule to make a variety of  $W_0$ , the dried sample was stored into a humidifier for a given time; the temperature and humidity of the humidifier were regulated at  $23.5\pm 0.5^\circ\text{C}$  and  $90\pm 5\%$  respectively. The  $W_0$  for the water-readsorbed sample was controlled by the storage time in the humidifier.

The bacterial count of the squid sample was measured by a plate culture method using Tryptone Soya Agar (Oxid) at  $30^\circ\text{C}$  for 48h after the PUP given at specified  $W_0$ .

For the characterization of moisture species in the squid, a nuclear magnetic resonance (NMR) technique was used to measure the  $^1\text{H}$ -NMR spectra and a spin-spin relaxation time ( $T_2$ ) of water proton. The squid samples which were cut into the pieces of  $2\times 2\times 10$ mm were inserted into an NMR sample tube ( $9\text{mm}\phi \times 15$ mm in length).  $^1\text{H}$ -NMR spectra were obtained by a JEOL A-500 FT-NMR spectrometer operating at 500MHz for protons. The observed frequency width was 20kHz.  $90^\circ$  pulse width was  $12.5\mu\text{s}$  and the number of pulse repetitions was 8. The proton chemical shifts were measured by using a slight amount of water containing deuterium oxide as an external reference. All the NMR measurements were performed at  $23.5\pm 0.5^\circ\text{C}$ . The spin-spin relaxation times were obtained by the CPMG method.

The value of  $T_2$  obtained is related to the correlation time ( $\tau_c$ ) by using Eq.(1).

$$\frac{1}{T_2} = \frac{\gamma^4 \cdot \hbar^2 \cdot I(I+1)}{5r^6} \left( 3\tau_c + \frac{5\tau_c}{1 + \omega_0^2 \cdot \tau_c^2} + \frac{2\tau_c}{1 + 4\omega_0^2 \cdot \tau_c^2} \right) \dots\dots\dots(1)$$

where  $T_2$  is the spin-spin relaxation time of the water proton (s),  $\gamma$  is the gyromagnetic ratio of a proton ( $=2.675\times 10^8 \text{ rad}\cdot\text{T}^{-1}\cdot\text{s}^{-1}$ ),  $\hbar$  is the modified Plank's constant ( $=6.63\times 10^{-34} \text{ J}\cdot\text{s}$ ),  $I$  is a nuclear-spin quantum number of a water proton ( $=0.5$ ),  $r$  is the

proton-proton distance of a water molecule (0.16nm),  $\omega_0$  is the resonance frequency of NMR ( $=3.14 \times 10^9 \text{ s}^{-1}$ ), and  $\tau_c$  is the correlation time of a water proton (s). Using this equation,  $\tau_c$  values at any given  $T_2$  can be evaluated.

Further detailed experimental procedures and the evaluation details of  $De$  have been presented elsewhere (Konishi, Horiuchi and Kobayashi, 2001(a); Konishi and Kobayashi, 1999(a)).

### 3. Results and Discussion

#### 3-1. Dynamic Behavior of Dehydration Curves in a Drying Process

Fig.1(A) shows a dehydration response curve (curve-(a)) obtained under a continuous drying operation for the squid ( $W_0=306\%$ -d.b.) at  $T_D=50^\circ\text{C}$ . The graphical differentiation of the curve-(a) proposes a dehydration rate and the rates evaluated at any elapsed time can be plotted as a function of the time as shown by curve- $a'$  in Fig.1(B). In the course of the curve-(a) in Fig.1(A), eight PUP operations were introduced at points (b) ~ (i) which were characterized by different moisture content as  $W_0=220 \sim 40\%$ -d.b. Each of the eight PUP operations produces a new dehydration curve and the graphical differentiation of the new curves obtained gives a newly specified dehydration rate. The dehydration rates evaluated at the eight points (b) ~ (i) in Fig.1(A) were shown by curves-(b') ~ -(i') in Fig.1(B). As can be seen from the comparison between the curve-(a') and the curves-(b') ~ -(i') in Fig.1(B), all the curves-(b') ~ -(i') gave the dehydration rates higher than the curve-(a') in Fig.1(B). One can recognize a stepwise increase of the dehydration rates. These increases are resulted from the stepwise increase in the moisture content of the squid surface layer due to the PUP operation. The acceleration degree of dehydration rate after the PUP was strongly influenced by the  $W_0$ -values at the points (b) ~ (i) located on the curve-(a) in Fig.1 (A). As has been mentioned in the previous section, the dehydration operation is limited in a falling rate period. In

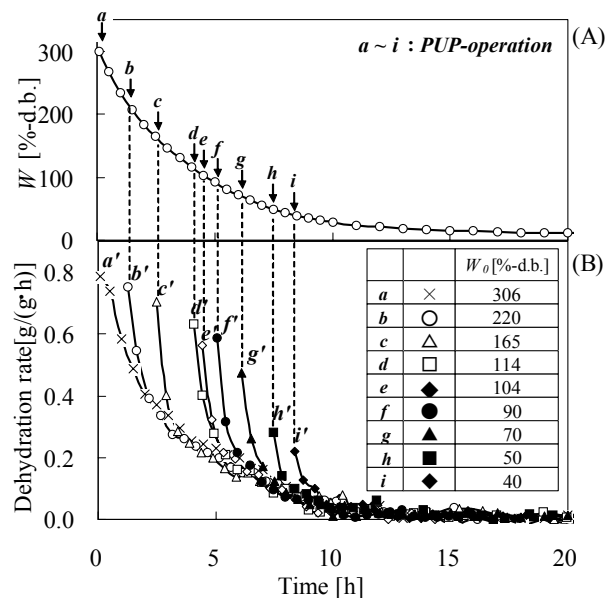


Fig.1 Acceleration behavior of drying rate derived from PUP-operation for the squid ( $T_D=50^\circ\text{C}$ )

this period, the effective moisture diffusivity ( $De$ ) can be evaluated by using Eq.2 (Jason, 1958).

$$\frac{W - We}{W_D - We} = \left(\frac{8}{\pi^2}\right)^3 \exp\left(\frac{-\pi^2 \cdot De \cdot t}{4} \cdot (L_a^{-2} + L_b^{-2} + L_c^{-2})\right) \dots\dots\dots(2)$$

where  $W$  is the moisture content at the drying time  $t$ ,  $We$  is the equilibrium moisture content,  $W_D$  is the initial moisture content of a drying fresh sample,  $t$  is the drying time, and  $L_a$ ,  $L_b$ , and  $L_c$  are the half-distances of the sample width.

At the initial points of the curves- (a') ~ -(i') in Fig.1 (B), the values of  $De$  were evaluated and plotted as a function of  $W_0$  as shown in Fig.2. The  $De$  obtained showed a characteristic behaviour exhibiting two regions as a constant value region at  $W_0 > 120\%$ d.b. (designated as region I) and a gradual increase region at  $W_0 < 120\%$ d.b. (designated as region II).

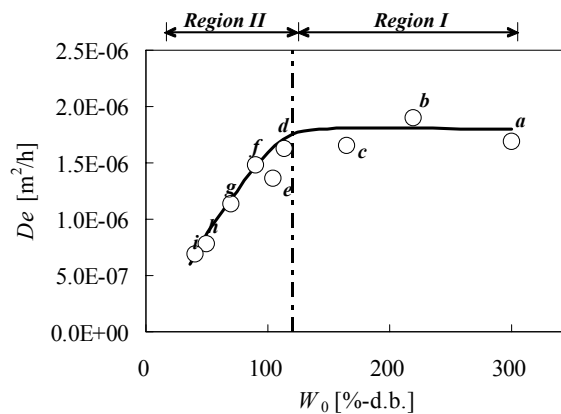


Fig.2  $De$  as a function of  $W_0$  for the squid ( $T_D=40^\circ\text{C}$ ).

From the two regions, one may recognize two different water species, water species- $A_1$  which contributes to an identical  $De$  [ $=1.8(\pm 0.2) \times 10^{-6} \text{ m}^2/\text{h}$ ] without depending on  $W_0$  in region I and water species- $A_2$  which is characterized as a gradual increase from  $De=0.6 \times 10^{-6}$  to  $De=1.7 \times 10^{-6} \text{ m}^2/\text{h}$  with increasing  $W_0$  in region II.

$De$  can be characterized by activation energy of diffusion using a simple Arrhenius-type relationship:

$$De = De^0 \exp\left[\frac{-E_D}{R \cdot (T_D + 273)}\right] \dots\dots\dots(3)$$

where  $De^0$  is frequency factor ( $\text{m}^2/\text{h}$ ),  $E_D$  is activation energy of effective moisture diffusivity ( $\text{kJ}/\text{mol}$ ),  $R$  is gas constant ( $8.314 \text{ J}/\text{K} \cdot \text{mol}$ ), and  $T_D$  is drying temperature ( $^\circ\text{C}$ ).

The Arrhenius plots of  $De$ -values obtained at  $T_D=30, 40$  and  $50^\circ\text{C}$  give a good straight line and  $E_D$ 's are evaluated at various moisture contents. The  $E_D$  obtained clearly demonstrates again two regions, identical value of  $17(\pm 0.2) \text{ kJ}/\text{mol}$  in the region I and gradual increase value from  $25$  to  $35 \text{ kJ}/\text{mol}$  with increasing  $W_0$  in the region II. Based on the results of  $De$  and  $E_D$  in the two regions, one may recognize that species- $A_1$  is mobile water with uniformed and characterized by higher  $De$ -values and lower  $E_D$ -values, and species- $A_2$  is restricted water with widely distributed  $De$ - and  $E_D$ -values.

### 3-2. Multifunctional Water Species Distinguished by the Bacterial Growth Behavior

As has been mentioned in the previous section, water species- $A_1$  effectively contributes to the moisture diffusion in region I whereas, in region II, water species- $A_2$  is available for the characteristic moisture diffusion indicating the restricted water molecule in the squid muscle. The two water species can be distinguished again by bacteria growth behavior. The bacteria observed on the squid skin were recognized mainly as staphylococcus and micrococcus. Noting the bacterial contamination of the squid skin, one can easily evaluate the bacteria growth which is sensitively influenced by both the moisture content ( $W_0$ ) and a relative humidity of supplied drying air flow (RH). Fig.3 illustrates a bacteria count as a function of  $W_0$  and RH. As one can recognize from the five curves obtained, the bacterial growth was completely limited at both  $W_0 < 120\%$ -d.b. (region II: species- $A_2$  to be available in this region) and  $RH = 30\%$  (designated as  $RH_{30}$ ). This limitation clearly demonstrates the bacterial growth to sensitively be regulated by the  $W_0$  and the RH. In other words, the water species- $A_2$  should work to prevent bacterial contamination and the  $RH_{30}$  gives a critical relative humidity to completely control the bacterial contamination even at the region of species- $A_1$  (at  $W_0 > 120\%$ -d.b.: region I). Since the bacterial count was measured as a function of time at various  $W_0$ , the bacterial growth rate coefficient ( $m$ ) can be evaluated as  $m = 0$  at  $RH = 30$ ,  $m = 0.24$  at  $RH = 55$ ,  $m = 0.34$  at  $RH = 65$ ,  $m = 0.43$  at  $RH = 75$  and  $m = 0.55h^{-1}$  at  $RH = 85\%$  within the region of species- $A_1$ . In the regions of species- $A_2$  (at  $W_0 < 120\%$ -d.b.) and  $RH < RH_{30}$ , the value of  $m$  exactly becomes zero indicating no bacterial growth. The two factors, species- $A_2$  and  $RH_{30}$ , thus can effectively be used as an operating parameter to preventing food from the bacterial contamination.

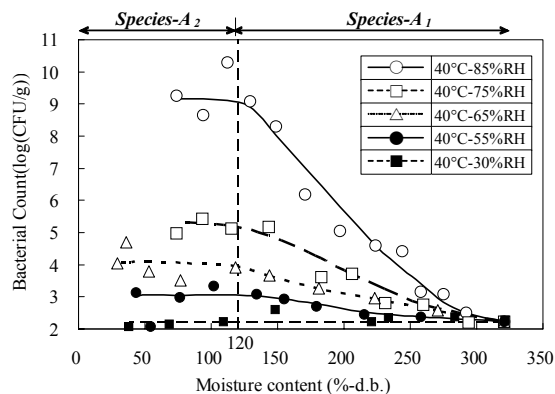


Fig.3 Bacterial count as a function of moisture content and the relative humidity.

### 3-3. Nonlinear Behavior of the Correlation Time of Water Proton

As is well known, water molecules of food are commonly restricted from the food body matrix. The degree of the restriction is strongly influenced from the matrix structure of food and the conditions of circumstances especially moisture content and temperature. To evaluate the degree of the restriction for the water species, the proton NMR method can effectively be used. In the present study, the correlation time ( $\tau_C$ ) was chosen to distinguish multifunctional water species. The value of  $\tau_C$  is dynamically varied depending on a kind of water species as species- $A_1$  to be  $4.8 \times 10^{-9}$

s and species-A<sub>2</sub> to be  $1.0 \times 10^{-8} \sim 1.2 \times 10^{-7}$  s. From the difference of the absolute value of  $\tau_c$  between the two species, one can exactly recognize species-A<sub>1</sub> to be a weekly restricted-water and species-A<sub>2</sub> to be strongly restricted-water.

Since  $1/\tau_c$  means a rotation rate of water molecule, the value can be expressed by an Arrhenius equation. Fig.4 illustrates the Arrhenius plot of  $1/\tau_c$ . The locus of the plot gave an anomalous behavior depending on the locus of temperature decrease or temperature increase indicating a typical hysteresis. In the course of temperature decrease from 30 to -30°C, the value of  $\ln(1/\tau_c)$  steeply decreased at -10°C and, in the locus of temperature increase course from -30 to 30°C, it linearly increased up to 0°C and fell on the line of the previous curve obtained in the temperature decrease course. This hysteresis behavior was exactly reproducible, and it was reconfirmed that the reversibility of the linear relation between 0 and -25°C in the course of temperature increase was completely examined, indicating an activation energy of the rotation to be  $40(\pm 2)$ kJ/mol. One may call this water species as species-A<sub>2</sub>' different from species-A<sub>1</sub> and -A<sub>2</sub>. The species-A<sub>2</sub>' was, in the course of the temperature decrease from 30 to -30°C, suddenly recognized at the temperature range between -10 and -25°C, suggesting a happening of a self organization of unfrozen water molecule. This nonlinear behavior of the Arrhenius plot for the rotation rate of the water species was commonly observed for other foods as salmon, scallop and sardine. Species-A<sub>2</sub>' is thus recognized as the self organization of the species-A<sub>2</sub>' newly formed from species-A<sub>1</sub> and -A<sub>2</sub>. For further detailed discussion on the anomalous hysteresis behavior, more visualized experimental data based on the physicochemical analysis should be needed in future.

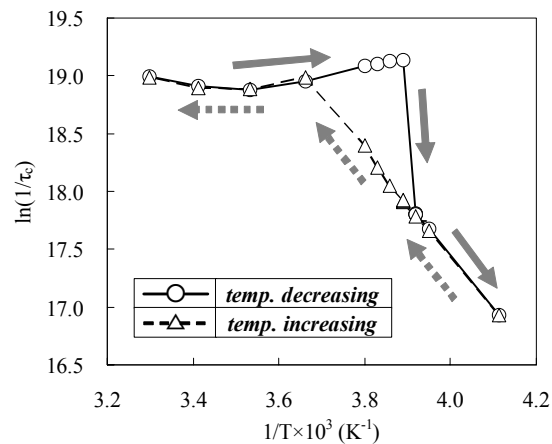


Fig.4 Hysteresis behaviour of the Arrhenius plot of  $1/\tau_c$

### 3-4. Model Description and Computer Simulation of the Dehydration Curves

As mentioned in the above section, the squid-drying period consists of a falling rate period, which indicates the dehydration rate to be limited by moisture diffusion from the internal to the surface layer. Fig.5 illustrates the experimental dehydration curves as a function of the moisture content. To simulate the dehydration curves, a water tank model (Konishi, Horiuchi and Kobayashi, 2001(b)), which was previously applied to the drying process of the fish past sausage, could be

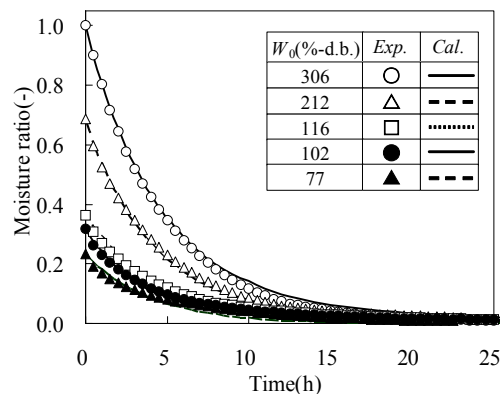


Fig.5 Comparison of the calculated curves and the experimental curves at 40°C



used. Fig.6 is a schematic of the tank model proposed. In the region I, the dehydrated moisture is separately supplied from the two water tanks consisting of weakly restricted water for the first tank (#1) and strongly restricted water for the second tank (#2), whereas, in the region II, the dehydration moisture is supplied from third tank (#3) of moisture which is same as the second tank (#2).

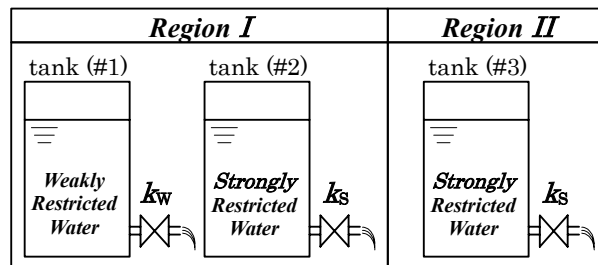


Fig.6 Schematic explanation of the tank model.

For a mathematical description of the tank model, the following assumptions are proposed:

- (1) The dehydration process from the sample squid is adequately approximated by effluent moisture from two tanks #1 and #2 for the region I and the effluent moisture from tank #3 which is same as tank #2 for the region II.
- (2) The rates of effluent moisture from tanks #1, #2 and #3 are controlled by three dehydration constants,  $k_w$ ,  $k_s$  and  $k_s$  respectively.
- (3)  $k_w$  and  $k_s$  are described as a function of diffusion coefficients,  $De_w$  and  $De_s$ , respectively.
- (4) The temperature dependencies of  $k_w$  and  $k_s$  obey the activation energies of  $De_w$  and  $De_s$ , respectively.
- (5)  $De_w$  and  $De_s$ , which are given at the initial stage of drying with specified initial moisture content ( $W_0$ ), can effectively contribute to the characteristics mode of the dehydration curves obtained.

In the region I, the mathematical descriptions are given by the following equations:

$$\frac{-dW_{R1}}{dt} = \frac{-dW_w}{dt} + \frac{-dW_s}{dt} \dots\dots\dots(4)$$

$$\frac{-dW_w}{dt} = k_w \cdot W_w \dots\dots\dots(5)$$

$$\frac{-dW_s}{dt} = k_s \cdot W_s \dots\dots\dots(6)$$

when the drying started at the region II:

$$\frac{-dW_{R2}}{dt} = k_s \cdot W_s \dots\dots\dots(7)$$

where  $W_{R1}$  and  $W_{R2}$  are the moisture ratio for the regions I and II, respectively;  $W_w$  and  $W_s$  are the moisture ratios for the weakly restricted water (species-A<sub>1</sub>) and strongly restricted water (species-A<sub>2</sub>), respectively.

For the three tanks, boundary conditions, when  $W_0 > 120\%$ -d.b.(region I), are

$$W_S = A_I \quad \text{and} \quad W_S = A_{II} \quad \text{at} \quad t = 0$$

when  $W_0 < 120\%$ -d.b.(region II), are

$$W_S = A_{III} \quad \text{at} \quad t = 0$$

$$W_W = 0 \quad \text{and} \quad W_S = 0 \quad \text{at} \quad t = \infty$$

The solutions of Eqs.(4) and (7) become

$$\text{Region I : } W_{R1} = A_I \exp(-k_W \cdot t) + A_{II} \exp(-k_S \cdot t) \dots\dots(8)$$

$$\text{Region II : } W_{R2} = A_{III} \exp(-k_S \cdot t) \dots\dots\dots(9)$$

where  $A_I$ ,  $A_{II}$  and  $A_{III}$  are rewritten by

$$A_I = \frac{W_0 - We}{W_D - We} \cdot f_W \dots\dots\dots(10)$$

$$A_{II} = \frac{W_0 - We}{W_D - We} \cdot f_S \dots\dots\dots(11)$$

$$A_{III} = \frac{W_0 - We}{W_D - We} \dots\dots\dots(12)$$

where  $f_W$  and  $f_S$  are the proportions for the amounts of the weakly restricted and strongly restricted water, respectively. Both  $f_W$  and  $f_S$  are experimentally obtained as follows.

$$f_W = 6.1(\pm 2.8) \times 10^{-6} W_0 + 0.89(\pm 0.07) \dots\dots\dots(13)$$

$$f_S = 1 - f_W = 0.89(\pm 0.07) + 6.1(\pm 2.8) \times 10^{-6} W_0 \dots\dots\dots(14)$$

Since the drying period is the falling rate period, the drying rate is limited by moisture diffusion from the internal to the surface layer of squid. The dehydration constants in Eqs. (8) and (9) can thereby be expressed as a function of moisture diffusivity:

$$k_W = \beta_1' \cdot D e_w \dots\dots\dots(15)$$

$$k_S = \beta_2' \cdot D e_s \dots\dots\dots(16)$$

where  $\beta_1'$  and  $\beta_2'$  are constants ( $m^{-2}$ ), which are given by the drying conditions.

Using Eq.(3), the two dehydration constants can be rewritten by the assumption of the activation energies for species- $A_1$  and  $-A_2$  to be same:

$$k_W = \beta_1' \cdot D e_w = \beta_1' \cdot D e_w^0 \cdot \exp(-E_D / (R \cdot (T_D + 273))) = \beta_1 \cdot \exp(-E_D / (R \cdot (T_D + 273))) \dots\dots\dots(17)$$

$$k_S = \beta_2' \cdot D e_s = \beta_2' \cdot D e_s^0 \cdot \exp(-E_D / (R \cdot (T_D + 273))) = \beta_2 \cdot \exp(-E_D / (R \cdot (T_D + 273))) \dots\dots\dots(18)$$

where  $E_D$  is the activation energy for both species-A<sub>1</sub> and -A<sub>2</sub>.

By using Eqs. (17) and (18), Eqs. (8) and (9) are rewritten by

$$W_{R1} = \left( \frac{W_0 - W_e}{W_D - W_e} \right) \cdot \left[ f_w \cdot \exp \left( -\beta_1 \cdot \exp \left( \frac{-E_D}{R \cdot (T_D + 273)} \right) \cdot t \right) + f_s \cdot \exp \left( -\beta_2 \cdot \exp \left( \frac{-E_D}{R \cdot (T_D + 273)} \right) \cdot t \right) \right] \dots\dots\dots(19)$$

$$W_{R2} = \left( \frac{W_0 - W_e}{W_D - W_e} \right) \cdot \left[ f_s \cdot \exp \left( -\beta_3 \cdot \exp \left( \frac{-E_D}{R \cdot (T_D + 273)} \right) \cdot t \right) \right] \dots\dots\dots(20)$$

Since the activation energy is experimentally evaluated as  $E_D=1.8\text{kJ/mol}$ ,  $\beta_1$ ,  $\beta_2$  and  $\beta_3$  can easily be estimated by using a simple optimization technique for fitting to the two  $W_{R1}$  and  $W_{R2}$  curves obtained after the PUP at  $W_0=306$  and 102 %-d.b. at 40°C.

$$\beta_1 = 306(\pm 90) \text{ h}^{-1}$$

$$\beta_2 = 75(\pm 22) \text{ h}^{-1}$$

$$\beta_3 = 16900(\pm 3000) \text{ h}^{-1}$$

By using these values, one can evaluate the values of  $k_w$  and  $k_s$  as 0.19-0.39 and 0.053-0.228h<sup>-1</sup>, respectively, at  $W_0=306 \sim 77\%$ -d.b. and  $T_D=35\text{-}50^\circ\text{C}$ . These values obtained fall in the range of dehydration constants reported in the previous works as 0.186-0.450h<sup>-1</sup> for pigeon pea (Shepherd and Bhardwaj, 1988) and 0.023-0.086h<sup>-1</sup> for ear corn (Sharaf-Eldeen, Blaisdell and Hamdy, 1980).

Using Eqs. (19) and (20), all the dehydration curves obtained could be simulated. The simulated curves are presented in Fig.5 by the solid and broken curves. The results clearly indicate good agreement with the experimental curves suggesting that the proposed water tank mode can usefully be applied to the squid drying process same as the fish past sausage.

#### 4. Conclusions

The four physicochemical parameters chosen for the squid,  $De$ ,  $E_D$ ,  $\tau_C$ , and  $m$ , individually characterized the three water species, -A<sub>1</sub>, -A<sub>2</sub> and -A<sub>2</sub>'. On  $De$ , it was evaluated as  $1.8 \times 10^{-6}$  for the water species-A<sub>1</sub> and  $0.6 \sim 1.7 \times 10^{-6} \text{ m}^2/\text{h}$  for species-A<sub>2</sub>. On  $E_D$ , they were 17 for species-A<sub>1</sub> and  $25 \sim 35 \text{ kJ/mol}$  for species-A<sub>2</sub>. On  $\tau_C$ , they were  $4.8 \times 10^{-9}$  for species-A<sub>1</sub> and  $1.0 \times 10^{-8} \sim 1.2 \times 10^{-7} \text{ s}$  for species-A<sub>2</sub>. On  $m$ , they were 0.24~0.55 for species-A<sub>1</sub> and 0h<sup>-1</sup> for species-A<sub>2</sub>. On the water species-A<sub>2</sub>', an

unusual histerisis behaviour for the Arrhenius plot of  $1/\tau_C$  was exactly appeared indicating two different locus's depending on the temperature decrease from 30 to -30°C or the temperature increase from -30 to 30°C. The activation energy ( $E\tau_C$ ) of the water molecule rotation rate was evaluated to be 3kJ/mol for the temperature decrease course and 40kJ/mol for the temperature increase course, indicating a self organization formed from the species-A<sub>1</sub> and -A<sub>2</sub> as unfrozen water molecule even at the temperatures lower than -10°C.

All the four parameters can individually be chosen depending on the food quality requested. The populations of species-A<sub>1</sub>, -A<sub>2</sub>, and -A<sub>2</sub>' can easily be regulated by controlling  $W_0$ ,  $T$ , and the relative humidity of supplied drying air (RH) as an operating parameter. The growth rates of staphylococcus and micrococcus for the squid sample were completely limited by the species-A<sub>2</sub> or by an RH lower than 30% (designated as critical relative humidity, RH<sub>30</sub>) at less than 10<sup>3</sup> CFU/g without depending on  $W_0$ . One could recognize that the RH<sub>30</sub> was usefully employed as an optimal operation in the drying process without bacterial contamination. All the unknown parameters to simulate the dehydration curves were reasonably evaluated for the design of optimal drying operation.

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