

# Model-Driven PID Control System, its properties and multivariable application

Takashi Shigemasa, Masanori Yukitomo,  
Power and Industrial Systems Research and Development Center ,  
Toshiba Corporation  
Toshiba IT & Control Systems Corporation

# Outline

---

Introduction

Model Driven PID Control System

structure and properties

Multivariable Model Driven PID Control System

structure and simulations

Conclusions

# Introduction

PID control system: widely used as a basic control technology,  
however, is not always easy tuning and has control limitation for long  
dead-time processes.

What is a simple, widely applicable process controller with easy to tune?

Based on the motif, we developed Model Driven PID Control System by extending the Model Driven control concept proposed by Kimura.

Firstly, Model Driven PID Control System, its structure, properties.

Secondary, the Model Driven PID Control System for multivariable processes on regulatory control level and simulation results.

# Model Driven PID Control System

---

Model Driven Control Concept

Model Driven PID control system

Structure and Properties

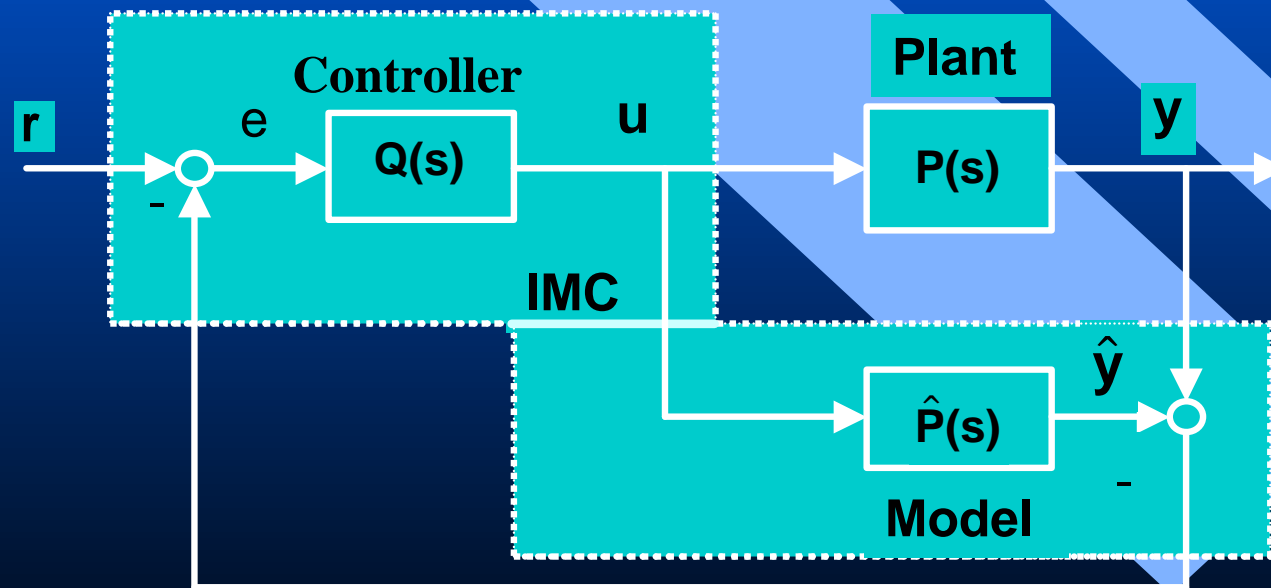
# Model-Driven Control Concept

## Definition:

Kimura(CDC2000Sydney)

A control system architecture which uses a model of the plant as a principal component of Controller is called a model-driven control.

## IMC Architecture Morari, Zafirou, 1989



## Features of MDC

Simple Structure

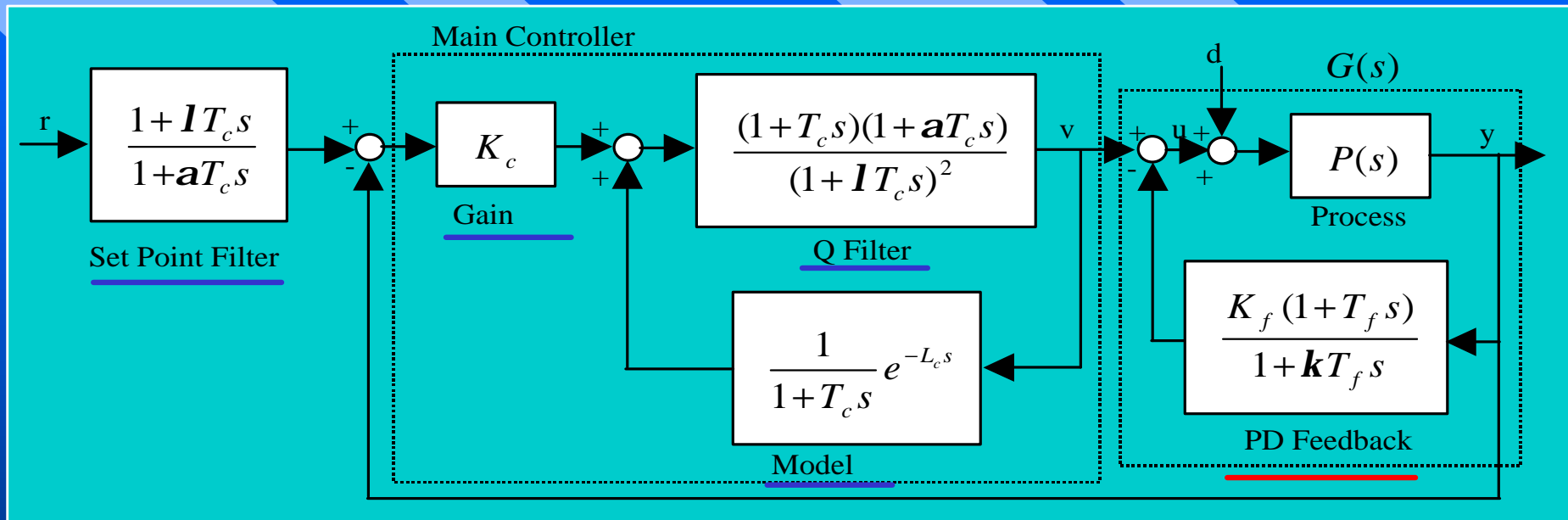
Easy Tuning

Proven Stability

and robustness

iff  $P(s)$  is stable

# Structure of Model Driven PID Control System



- PD Feedback

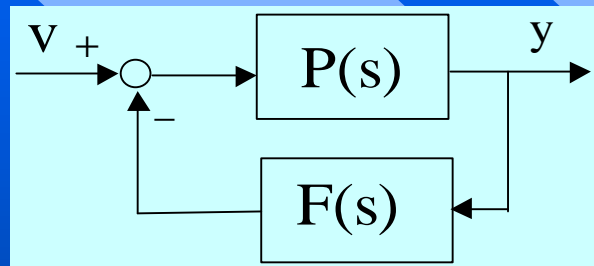
- Main control ;

Gain , second order Q-filter and normalized first order delay model with dead-time for inner loop

- Set-point filter

## Design steps

### Step 1 PD Feedback $F(s)$



$$G(s) = [1 - P(s)F(s)]^{-1} P(s)$$

$$\cong \frac{K \exp(-Ls)}{1 + Ts}$$

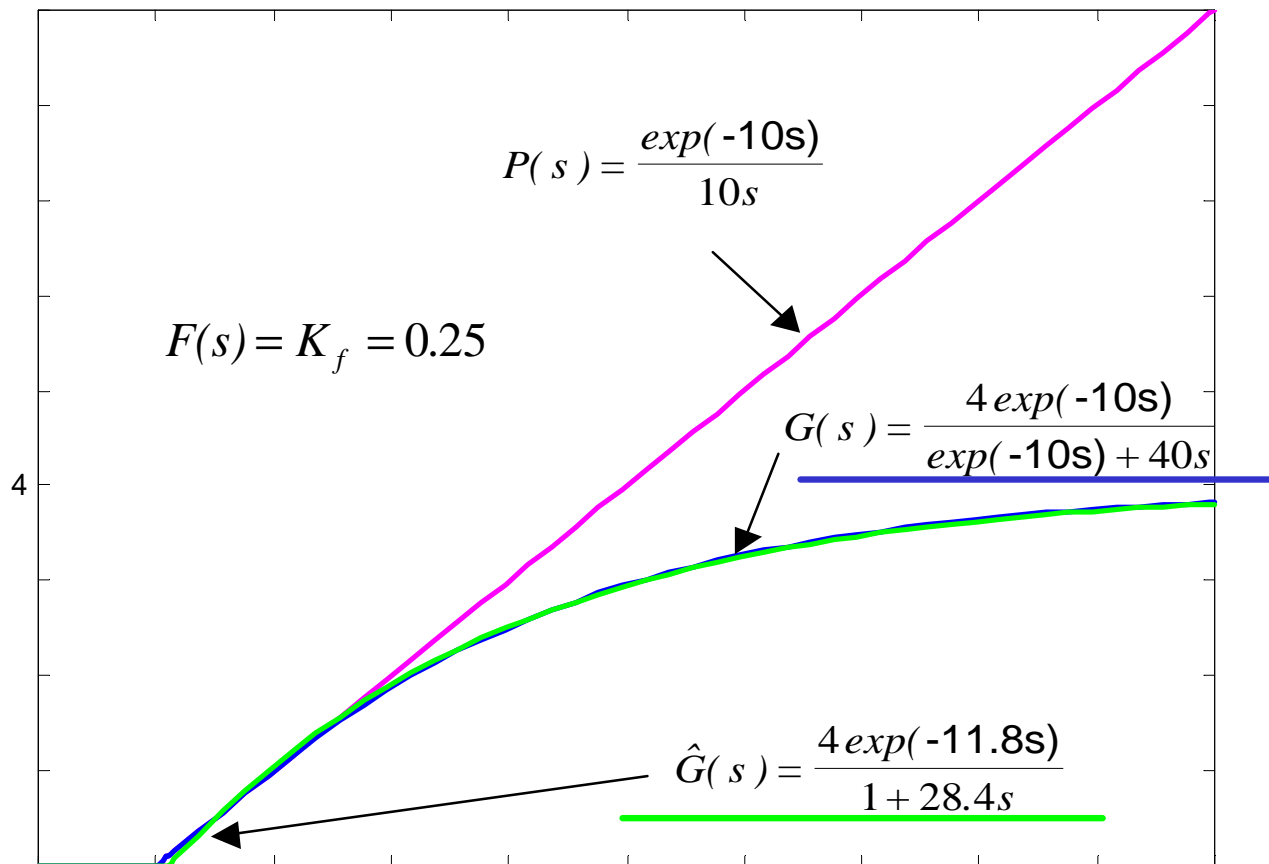
$$F(s) = \frac{K_f (1 + T_f s)}{1 + k T_f s}$$

Compensate inner loop dynamics  $G(s)$  to a first order system with dead time by using PD feedback  $F(s)$ .

Design methods  $\bar{\text{p}}$ artial model matching method, frequency region method, pole placement, simulation.

Wide applicability, for not only first order delay process with dead time but also integral process, oscillatory process and unstable process

Example: A integral process can be converted to a first order delay system with dead time





## Design steps(continued)

### Step 2: Main controller and set-point filter

- 1)  $K_c = 1/K$
- 2)  $T_c = T$
- 3)  $L_c = L$

### Step 3: TDOF property by adjusting $\alpha$ and $\beta$

$$y = \frac{\exp(-L_c s)}{1 + \beta T_c s} r + \frac{\exp(-L_c s)}{K_c (1 + T_c s)} \left[ 1 - \frac{(1 + \alpha T_c s)(1 + T_c s)}{(1 + \beta T_c s)^2} \right] d$$

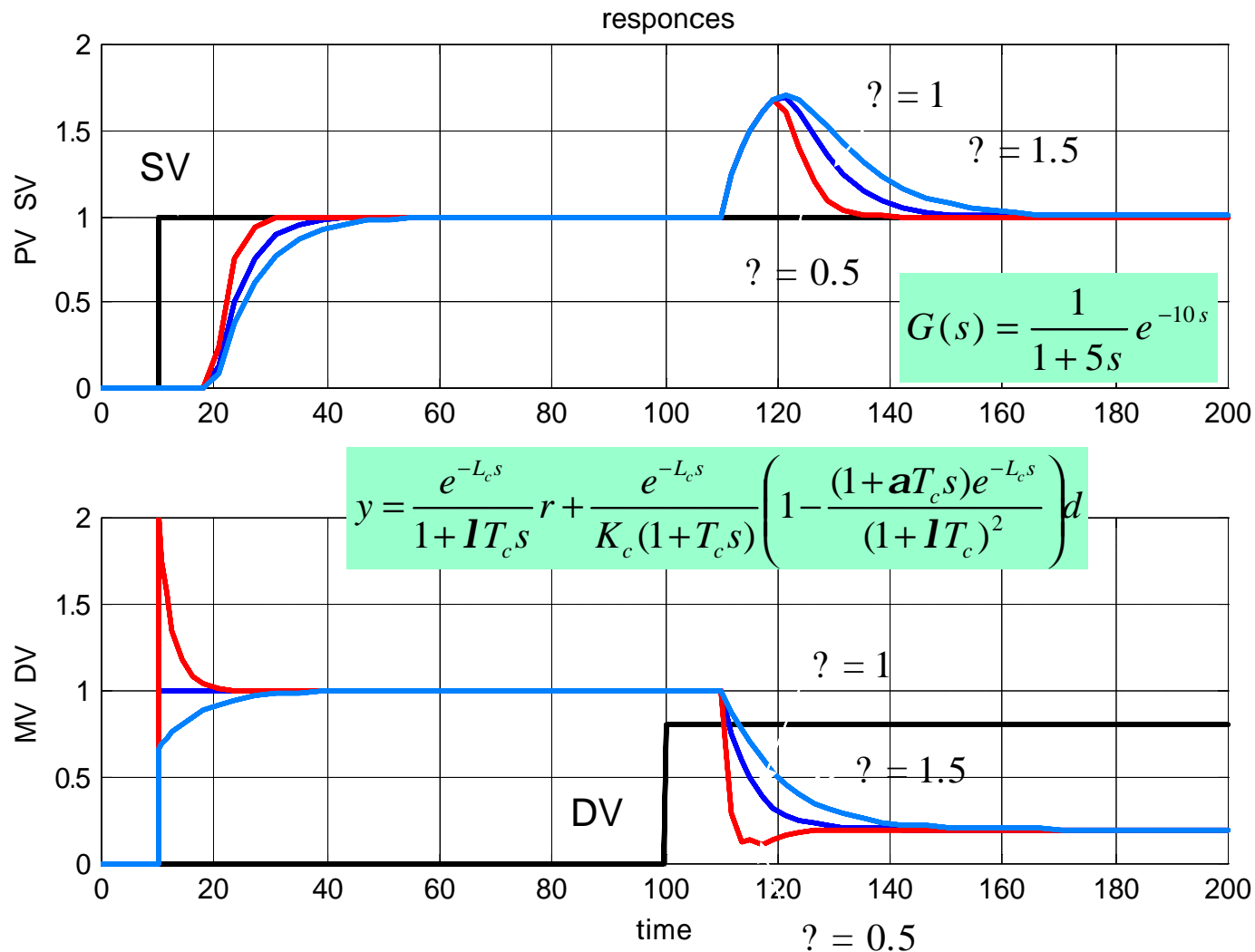
$$Q(s) = \frac{(1 + T_c s)(1 + \alpha T_c s)}{(1 + \beta T_c s)^2}$$

$\beta$  : response speed

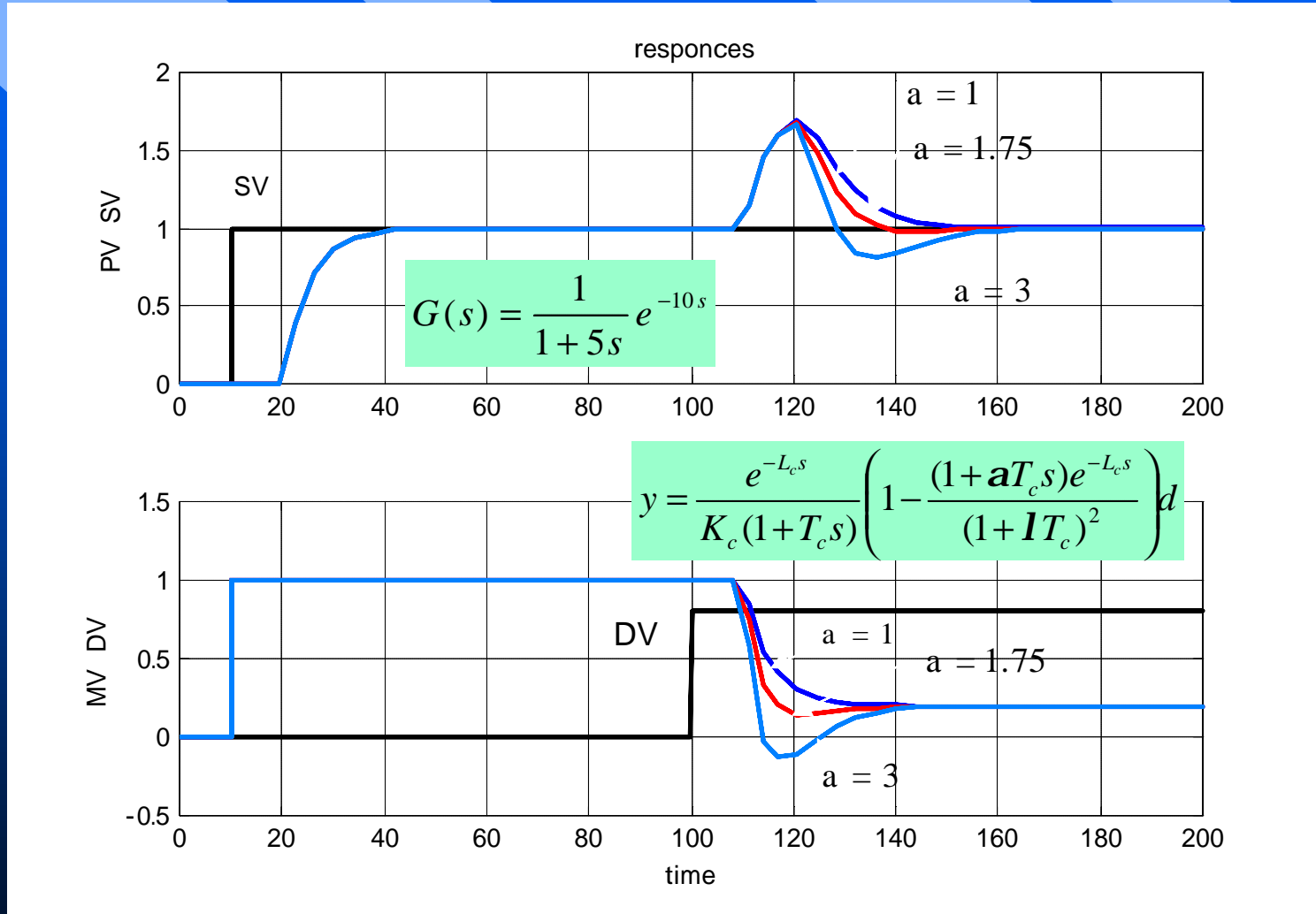
$$\frac{1 + \beta T_c s}{1 + \alpha T_c s}$$

$\alpha$  : Disturbance regulation

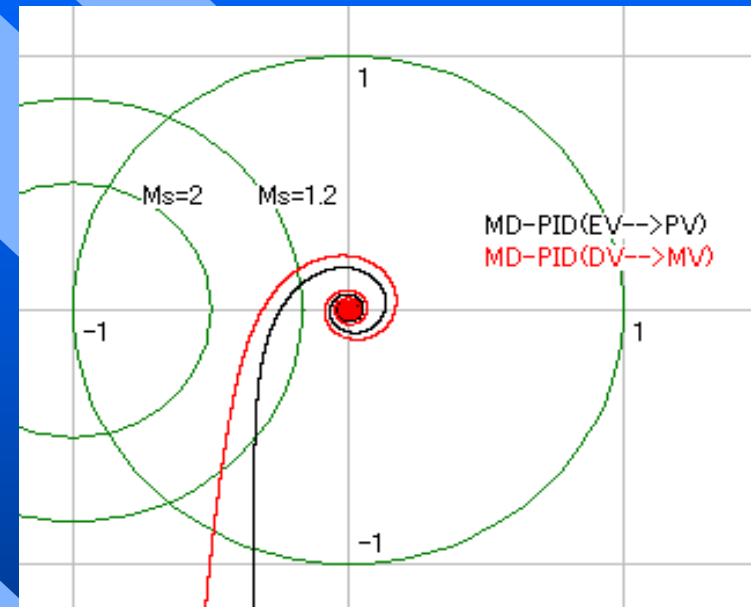
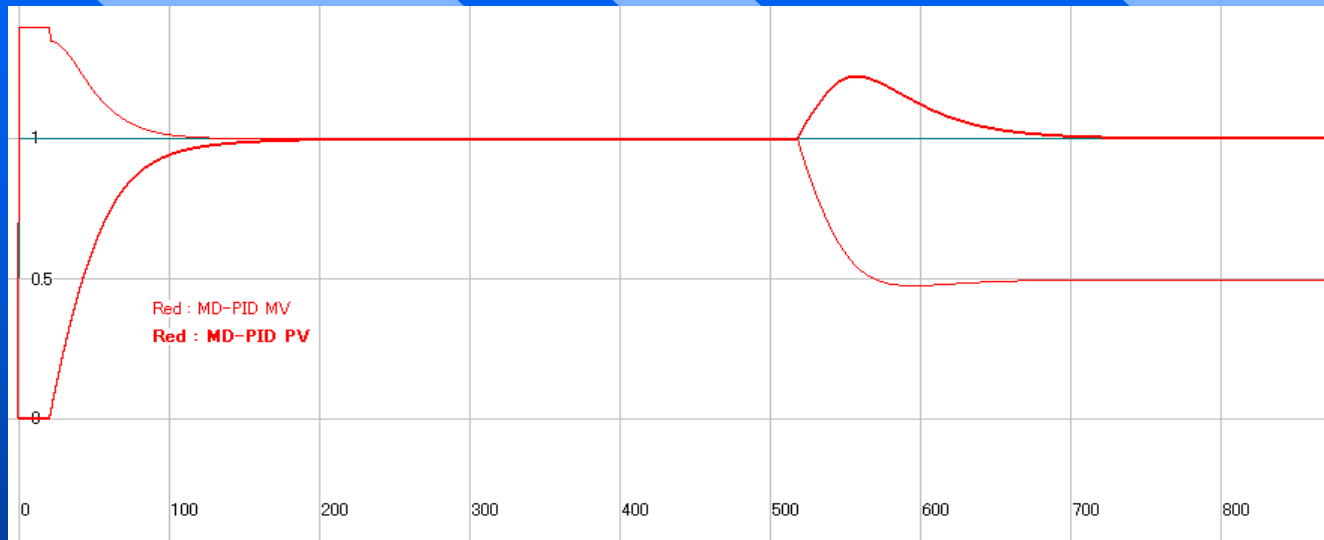
## Adjustable response speed by



## Adjustable Disturbance regulation speed by



## Robustness



$$P(s) = \frac{\exp(-20s)}{1+50s}$$

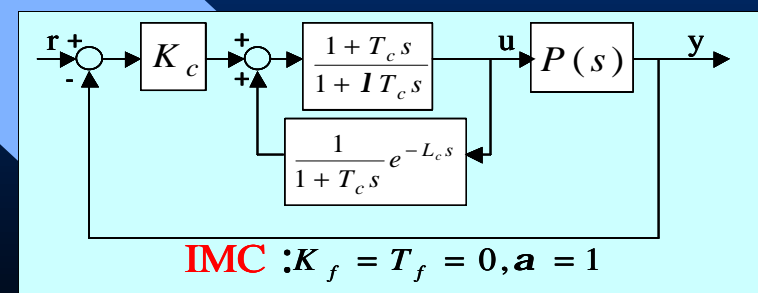
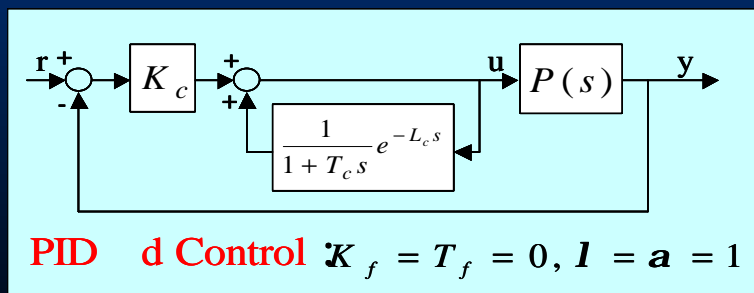
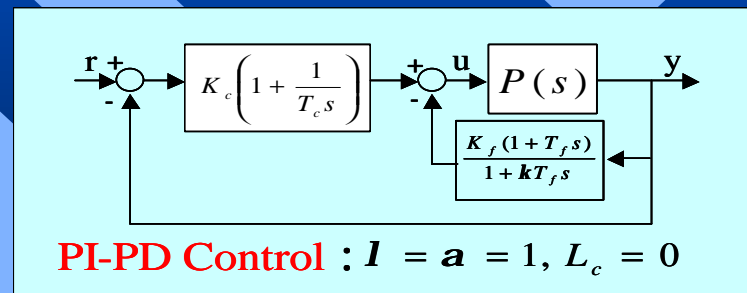
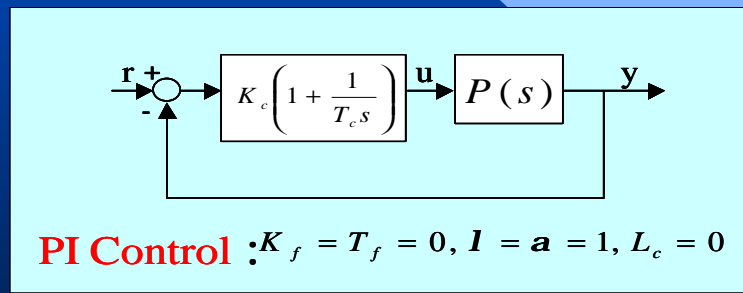
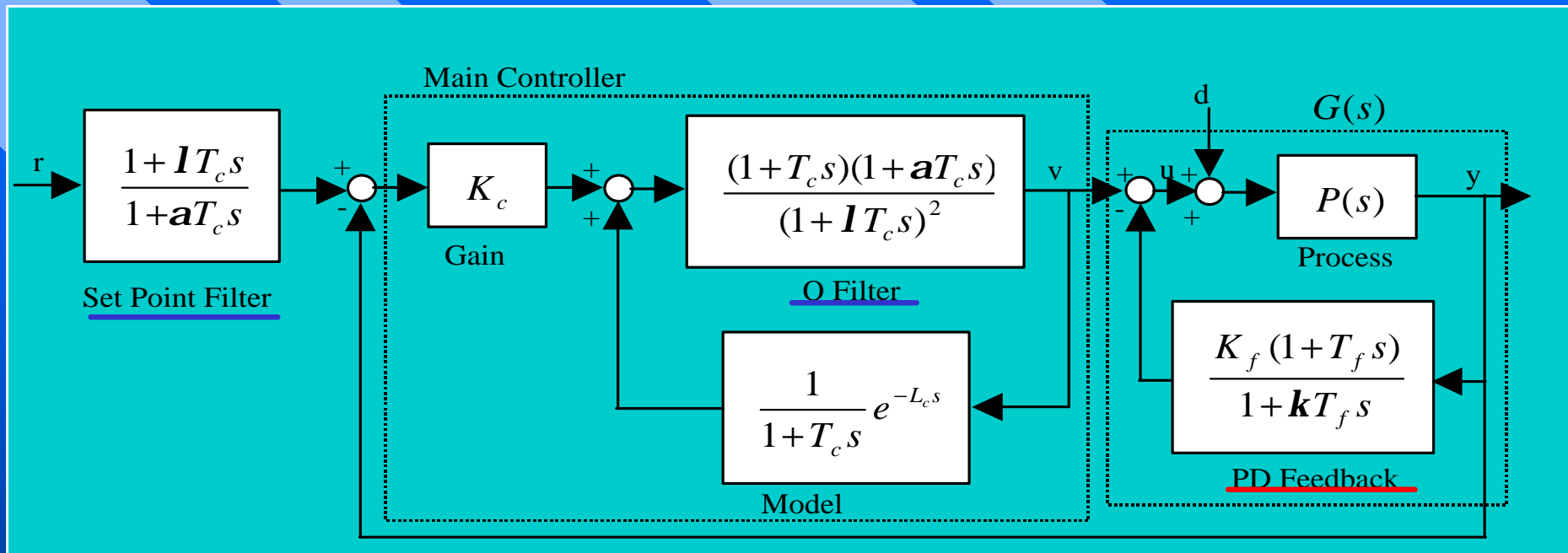
$$F(s) = 0.4$$

$$G(s) = \frac{0.714\exp(-21s)}{1+28.7s}$$

## Nyquist curves

MD-PID(EV-->PV)  
Gain Omega = 0.09  
Gain Margin = 12.12dB  
Phase Margin = 69.94deg

MD-PID(DV-->MV)  
Gain Omega = 0.09  
Gain Margin = 10.09dB  
Phase Margin = 60.64deg



# Summary of Properties

## 1. Wide Applicability

PD feedback

$$G(s) \cong \frac{K \exp(-Ls)}{1 + Ts} \quad F(s) = \frac{K_f (1 + T_f s)}{(1 + ? T_f s)}$$

## 2. Two degree of freedom characteristics

$$K_c = 1/K \quad T_c = T \quad L_c = L$$

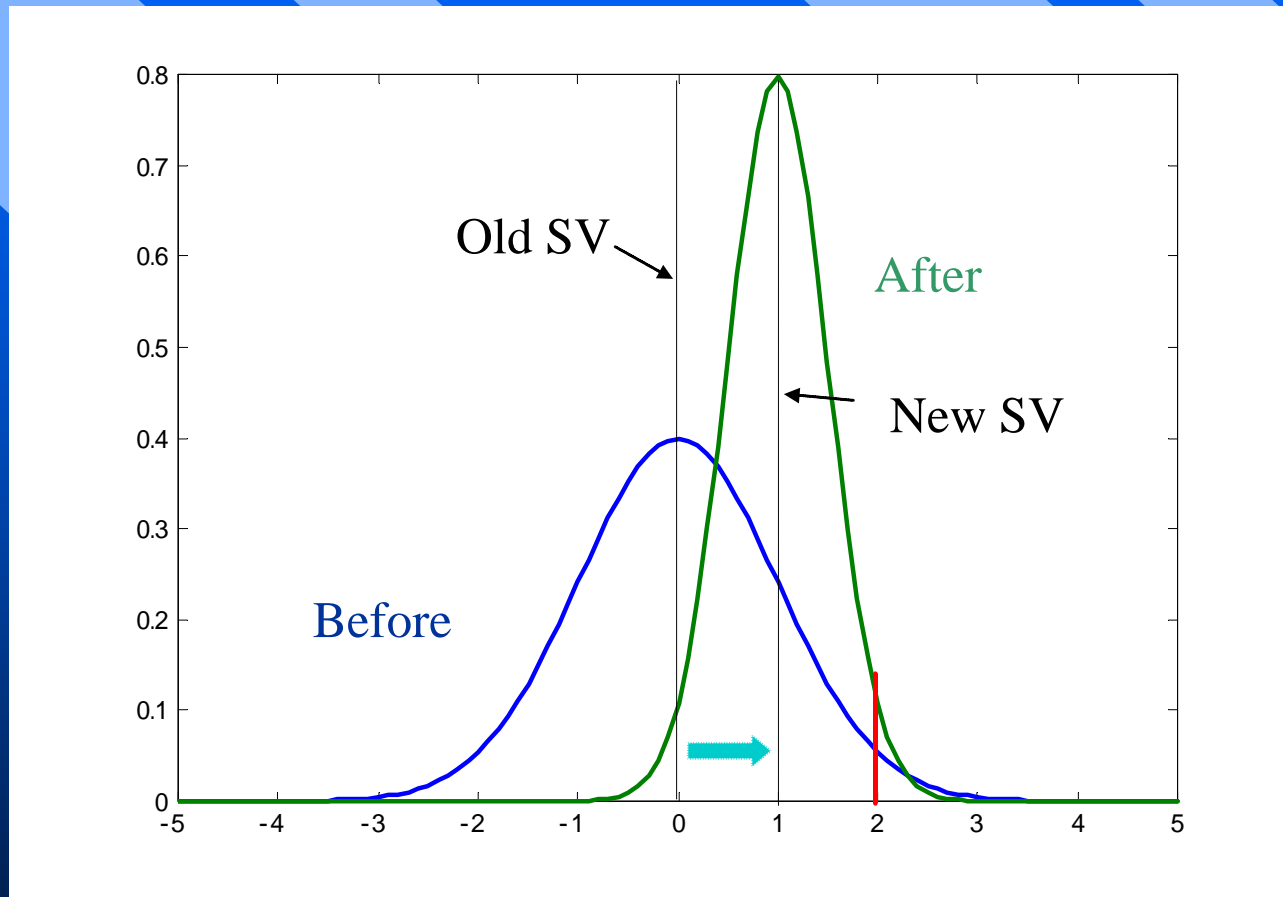
tuning; Response speed,

tuning; Disturbance regulation speed

## 3. Robustness can be examined by well-known nyquist chart

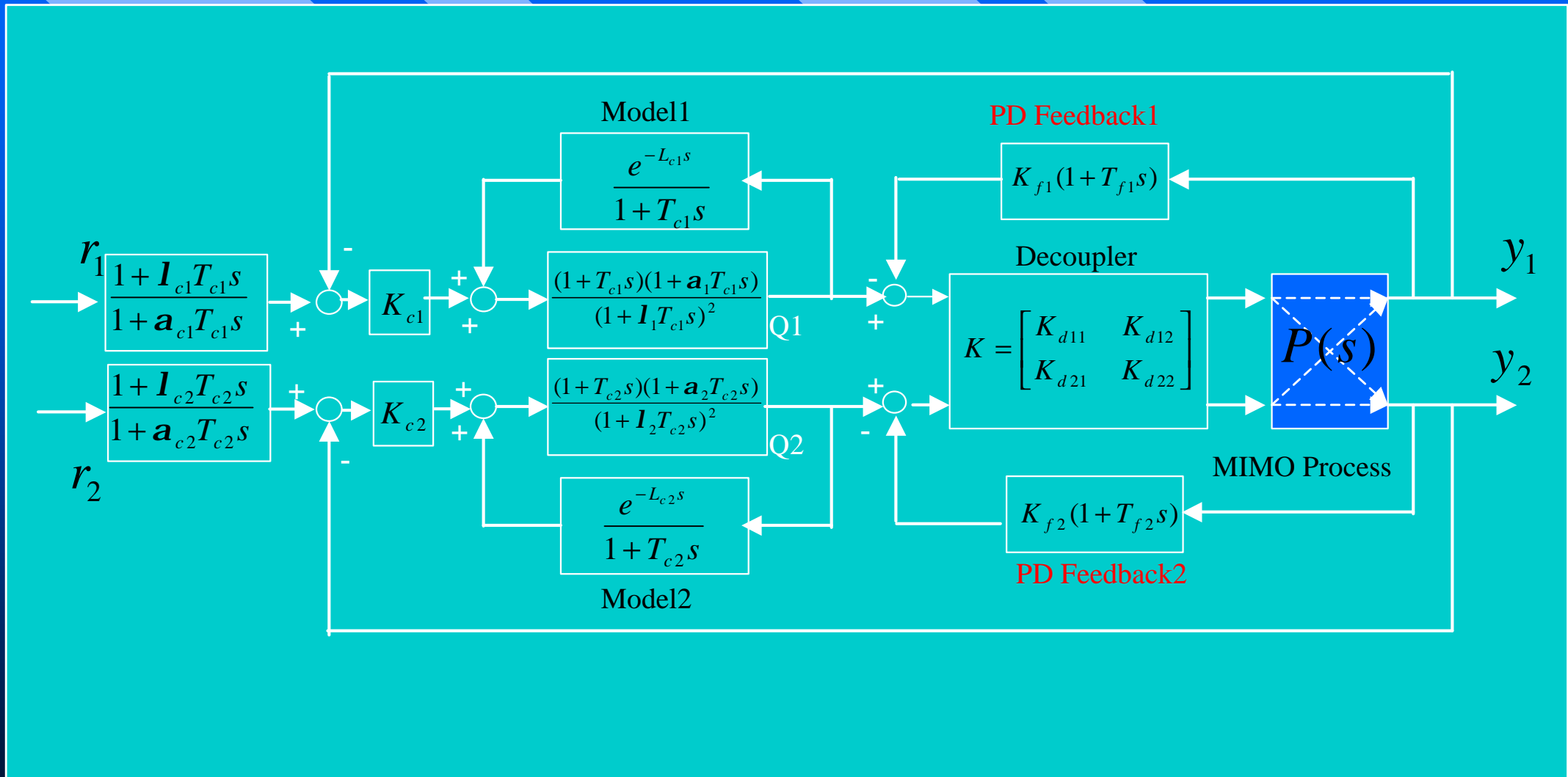
## 4. Upper compatibility from conventional PID control systems

## Control performance - PV distribution -



Reported reduce operator's over-riding actions and fuel cost, obtain high quality of product though some field applications.

# Multivariable Model Driven PID Control System





# Design steps

## 1 .Decoupler ( $K_{dec}$ )

$$P(s) = \begin{bmatrix} \frac{K_{11}}{1+T_{11}s} e^{-L_{11}s} & \frac{K_{12}}{1+T_{12}s} e^{-L_{12}s} \\ \frac{K_{21}}{1+T_{21}s} e^{-L_{21}s} & \frac{K_{22}}{1+T_{22}s} e^{-L_{22}s} \end{bmatrix} \Rightarrow K_{dec} = P(0)^{-1} = \begin{bmatrix} K_{11} & K_{12} \\ K_{21} & K_{22} \end{bmatrix}^{-1}$$

the control process

A decoupler

## 2 .Other MD control systems

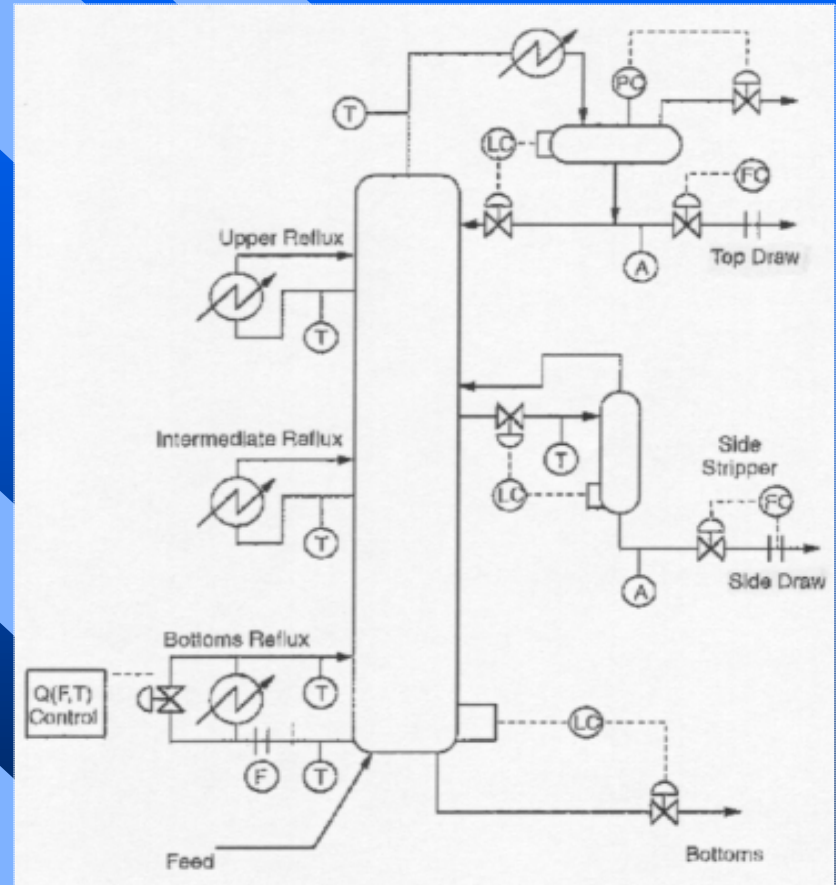
$$K_{dec} P(s) = \begin{bmatrix} \hat{P}_{11} & \hat{P}_{12} \\ \hat{P}_{21} & \hat{P}_{22} \end{bmatrix}$$

Designed for the diagonal element of  $K_{dec} P(s)$

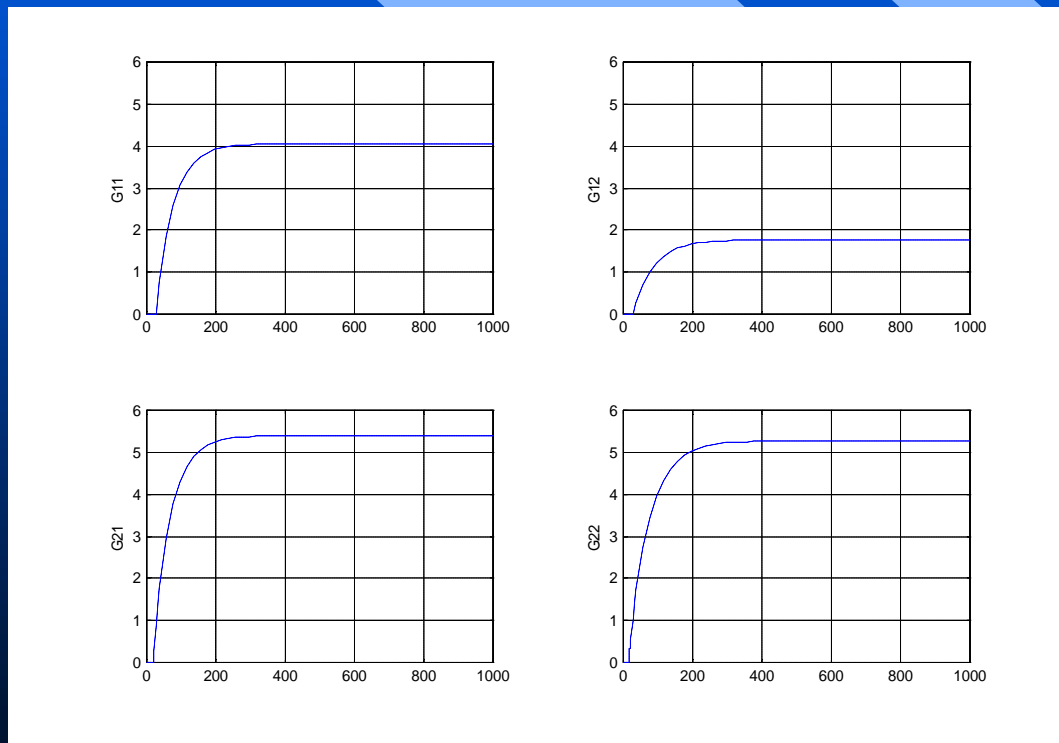
## Simulation

Controlled object : Shell heavy oil fractionator

$$P(s) = \begin{bmatrix} \frac{4.05}{1+50s} e^{-27s} & \frac{1.77}{1+60s} e^{-28s} \\ \frac{5.39}{1+50s} e^{-18s} & \frac{5.27}{1+60s} e^{-14s} \end{bmatrix}$$



IEEE Control System Magazine  
Shell heavy oil fractionator  
By Daniel E. Rivera



Step responses

# Design results

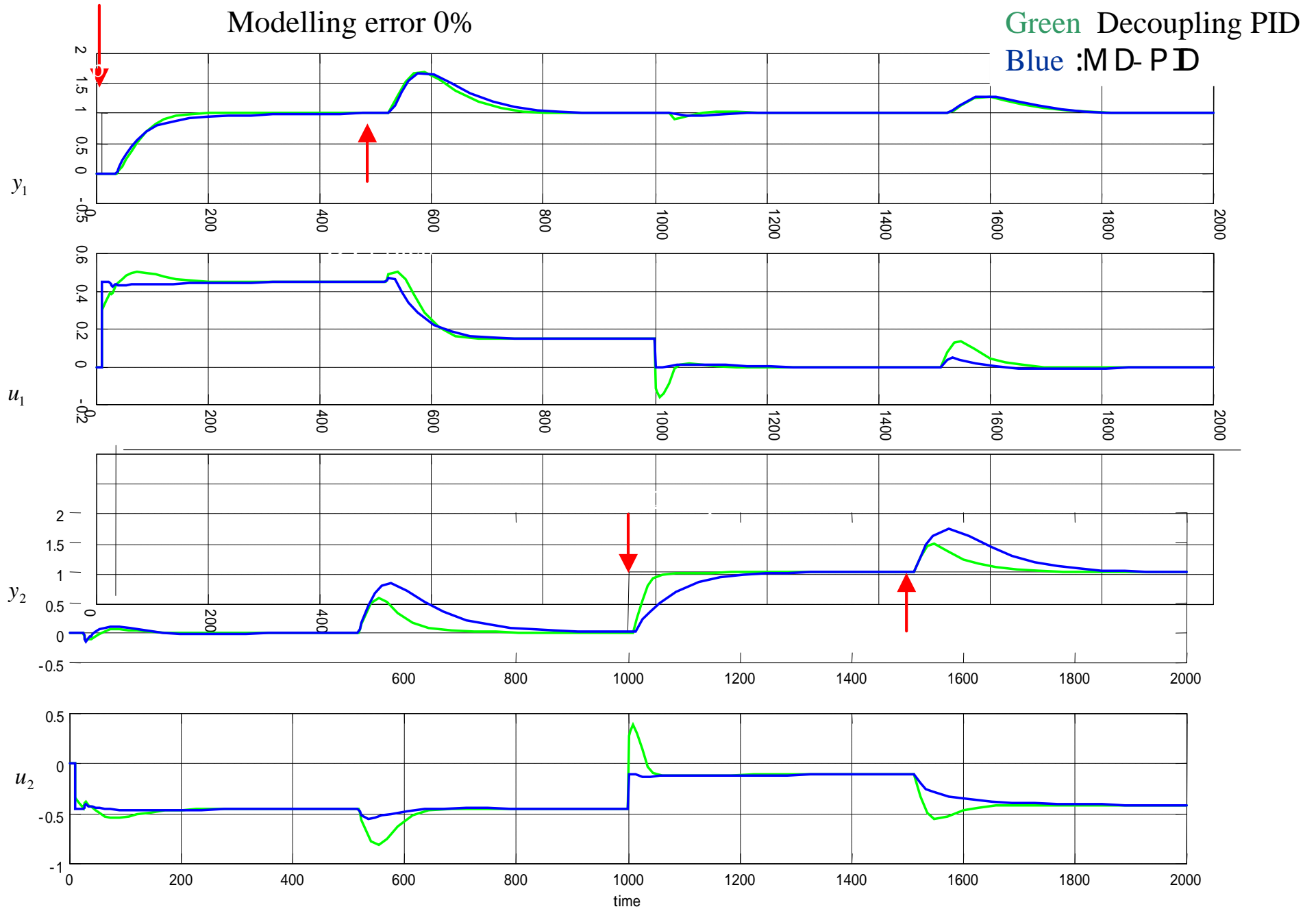
## 1 .Distributed MD PID Control

$$\text{Decoupler} = \begin{bmatrix} 0.4465 & -0.1500 \\ -0.4567 & 0.3431 \end{bmatrix}$$
$$\text{model1} = \frac{1}{1+50s} e^{-27s}, \text{model2} = \frac{1}{1+60s} e^{-14s}$$

## 2 .Decoupling PID Control

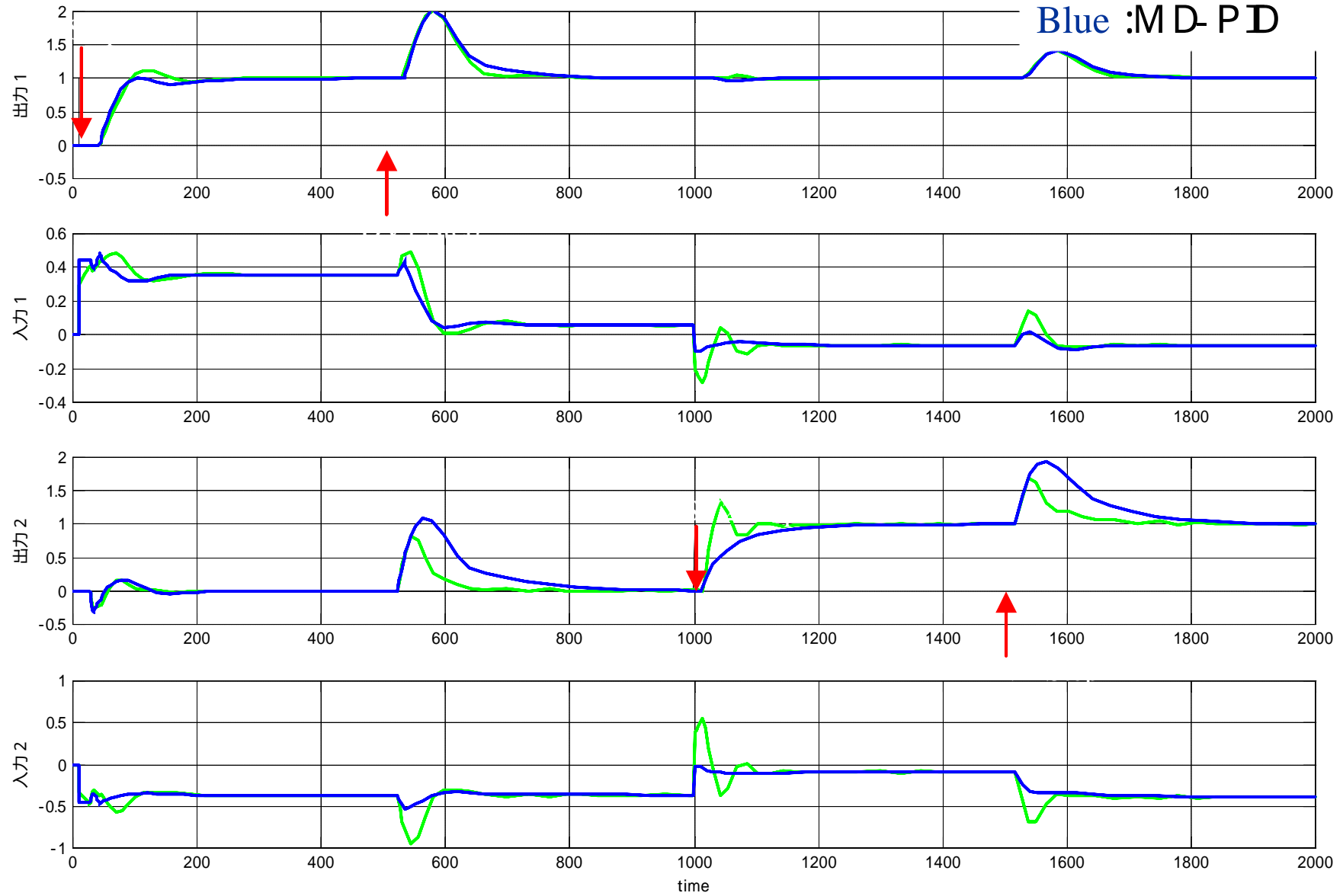
by Model-matching method by Kitamori

$$K_p = \begin{bmatrix} 0.2982 & -0.2618 \\ -0.3455 & 0.7372 \end{bmatrix}$$
$$T_I = \begin{bmatrix} 45.1015 & 47.6909 \\ 51.1015 & 58.6909 \end{bmatrix}$$



Modelling error 25%

Green Decoupling PID  
Blue :M D- P D



# Conclusions

We discussed a Model Driven PID control system, its properties and a multivariable application.

PD feedback give us wide applicability of controlled processes:

|        | Delay with dead time |           | Zero | Oscillation | Integral | Unstable |
|--------|----------------------|-----------|------|-------------|----------|----------|
|        | Small L/T            | Large L/T |      |             |          |          |
| PID    | ●                    | △         | △    | △           | △        | △        |
| MD-PID | ●                    | ○         | ○    | ○           | ○        | ○        |

MD-PID control system shows Good control performances like a TDOF control system with easy tuning.

MD- PID control system has upper compatibility from conventional PI, IMC, PID and PI-PD

Multivariable MD PID Control system shows useful results in spite of simple control structure.