

# Recipes for Data Rectification of Life Cycle Inventories

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# Life cycle inventory

contents	unit	amount	contents	unit	amount
Coal	lb	68.1	BOD	lb	1.9E-05
Electricity	kWh	813.0	Chlorine	lb	3.2E-04
Natural gas	lb	202.0	Dissolved Solids	lb	4.3
Residual oil	gallons	3.8	Lead	lb	9.4E-07
salt	lb	1670.0	Mercury	lb	5.4E-04
			Mercury	lb	1.5E-06
			Nickel	lb	9.4E-07
			Particulates	lb	4.6E-04
			Solid waste	lb	3.1E+00
			Sulfides	lb	1.5E-04
			Sulfur oxides	lb	1.0E-03
			Zinc	lb	9.4E-07
			Chlorine/Caustic Soda Production	lb	1000.0
			Chlorine	lb	893.0
			Hydrogen	lb	16.9
<b>Total</b>		<b>1943.9</b>			<b>1917.3</b>

(NREL NaOH LCI)

## Data inconsistency

- **Commensurability**
  - BOD cannot be added directly to output material
  - In certain LCI, energy consumption is represented by kJ, kWh, etc.
- **Discrepancy**
  - Conservative law of mass is not satisfied
- **Aggregated chemical species**
  - Dissolved solids, particulate and sulfides contains several chemical components

# Possible problems from inconsistency

- **Data discrepancy**
  - **Missing flows** in resource consumptions and waste emissions make impact analysis of chemical species ignored.
  - LCA results may be not correct from the **incorrect measured values**
  - Decision making by LCA is not correct if using discrepant LCI.
  - **Data rectification** can be applied to deal with the data discrepancy
- **Incommensurability and Aggregated species**
  - make data rectification difficult or practically impossible

# Data rectification of LCI and process engineering

	<b>LCI</b>	<b>Process engineering</b>
<b>Redundancy</b>	<b>Nonredundant</b>	<b>A few redundancy</b>
<b>Infrastructure</b>	<b>Blackbox</b>	<b>Detail flowsheets</b>
<b>Time horizon</b>	<b>One point</b>	<b>Yearly, monthly, daily, hourly, etc.</b>
<b>Aggregated species</b>	<b>Particulate, NO<sub>x</sub>, SO<sub>x</sub>, etc.</b>	<b>None</b>
<b>Reaction model for (trace) waste</b>	<b>Important</b>	<b>Not so important</b>
<b>Included process</b>	<b>Several processes</b>	<b>One process</b>
<b>Data source</b>	<b>Multiscale</b>	<b>One scale</b>

# Objectives

- **Propose methodology to deal with data discrepancy of LCI**
  - Multiscale characteristics of LCI data is used for rectification
  - Reducing procedure of the large number of models due to several included processes is shown
  - Nonredundancy of LCI data is solved by atomic balance

# Data rectification in process engineering

- **Gross error detection and identification**

- Global test:  $\gamma = \mathbf{r}^T \mathbf{V}^{-1} \mathbf{r} \sim \chi_v^2$
- Nodal test  $z_{r,i} = r_i / \sqrt{V_{ii}} \sim N_i(0,1)$
- Measurement test  $z_{d,j} = |y_j - x_j| / \sqrt{W_{jj}} \sim N(0,1)$

- **Data reconciliation**

$$\min_{\mathbf{x}} f = \boldsymbol{\varepsilon}^T \boldsymbol{\Sigma}^{-1} \boldsymbol{\varepsilon}$$

*s.t.*

$$\mathbf{h}(\mathbf{x}) = \mathbf{0}$$

$$\mathbf{g}(\mathbf{x}) \leq \mathbf{0}$$

where  $\mathbf{y} = \mathbf{x} + \boldsymbol{\varepsilon}$

# Data rectification in process engineering

- **Simultaneous gross error compensation and reconciliation**

$$\min_{\mathbf{x}, \delta, \mathbf{B}} f = \boldsymbol{\varepsilon}^T \boldsymbol{\Sigma}^{-1} \boldsymbol{\varepsilon}$$

*s.t.*

$$\mathbf{h}(\mathbf{x}) = \mathbf{0}$$

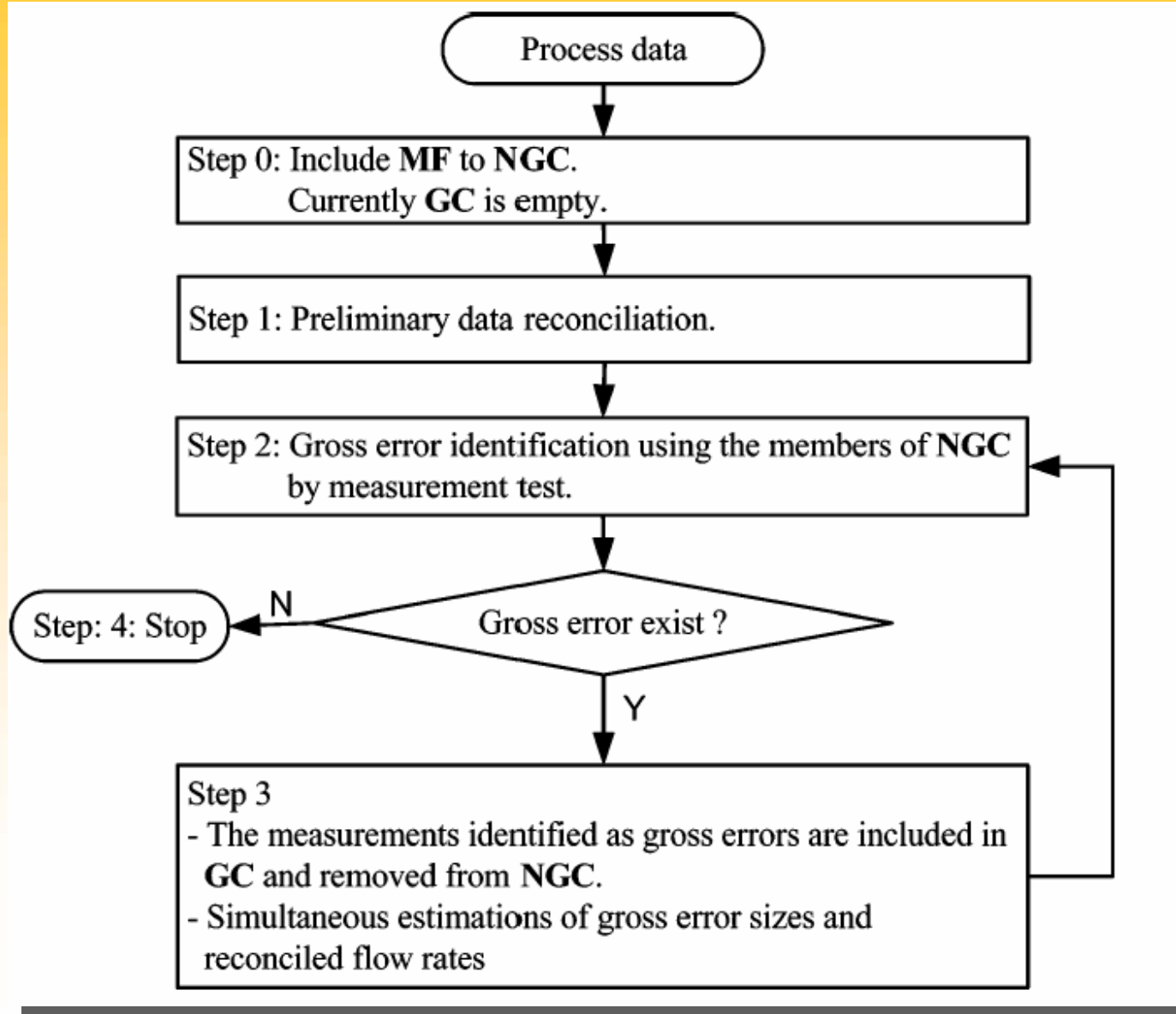
$$\mathbf{g}(\mathbf{x}) \leq \mathbf{0}$$

$$|\delta_i| - U_i B_i \leq 0$$

$$|\delta_i| - \zeta_i U_i B_i \geq 0$$

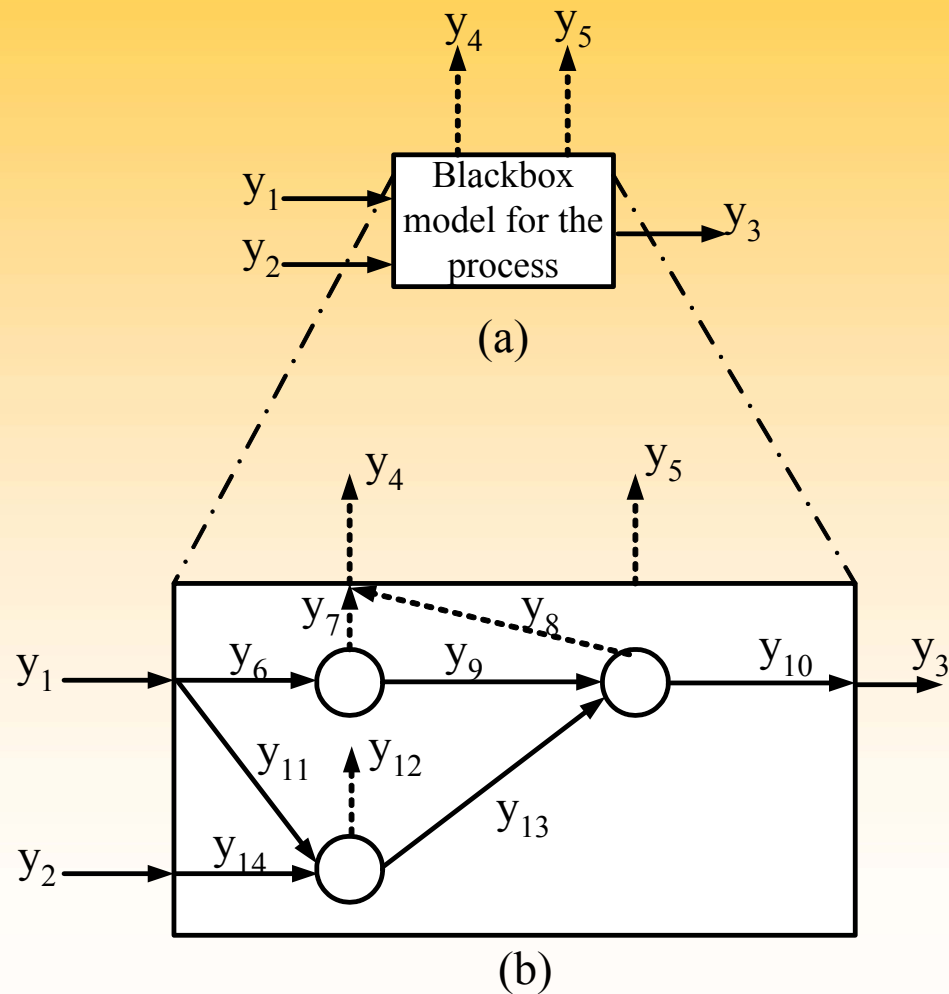
$$\text{where } \mathbf{y} = \begin{cases} \mathbf{x} + \boldsymbol{\varepsilon} + \boldsymbol{\delta} & \text{for the variable that gross error is identified} \\ \mathbf{x} + \boldsymbol{\varepsilon} & \text{for the others} \end{cases}$$

# Data rectification in process engineering





# LCI data rectification – multiple scales



## Objective functions

- Type I. Commonly exist at both scales  
e.g.,  $(y_2, y_{14})$ ,  $(y_3, y_{10})$

$$u_2 \frac{(y_2 - x_2)^2}{\sigma_2^2} + u_{14} \frac{(y_{14} - x_{14})^2}{\sigma_{14}^2}$$

$$\text{where } u_2 + u_{14} = 1$$

- Type II. Aggregated at coarse scale  
e.g.,  $(y_4, y_7, y_8)$ ,  $(y_1, y_6, y_{11})$

$$u_4 \frac{(y_4 - x_7 - x_8)^2}{\sigma_4^2} + u_7 \frac{(y_7 - x_7)^2}{\sigma_7^2} + u_8 \frac{(y_8 - x_8)^2}{\sigma_8^2}$$

$$\text{where } u_4 + u_7 + u_8 = 1$$

- Type III. Exist only at fine scale  
e.g.,  $y_9, y_{12}, y_{13}$

- Type IV. Exist only at coarse scale  
e.g.,  $y_5$

# LCI data rectification – confining models

- **LCI data**

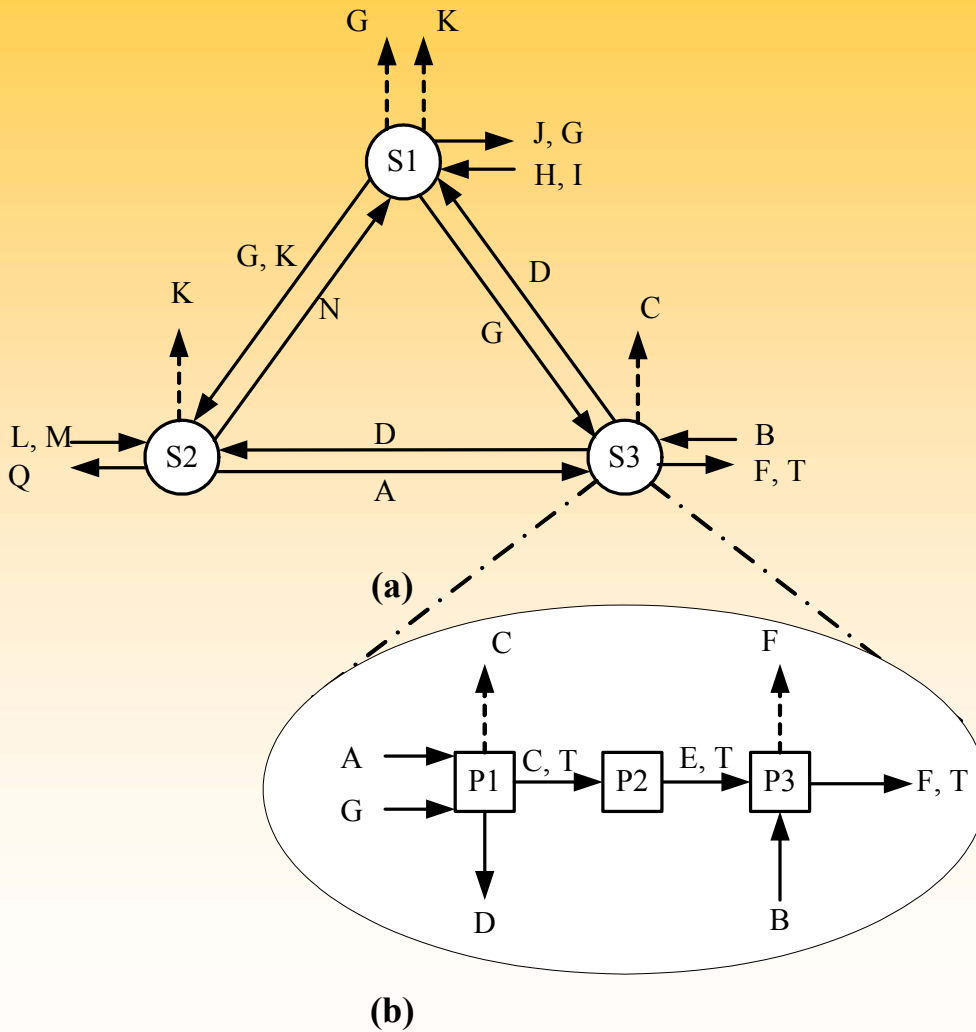
- Several processes are included for LCI data
- It is required to confine models for problem size reduction

- **Process models**

- Generally, the balance equations of total mass and component are used
- Component balances are not required for the node that does not have gross errors

- i) Implement global test by total mass balances
- ii) If (no error is detected) then  
go to step vii)  
else  
continue
- iii) Implement nodal test for each node by total mass balances
- iv) Add component balances in the descending order of nodal test statistics values
- v) Calculate the global test statistics
- vi) if ( $\Delta$ global test statistics) > (predefined criterion) then  
go to step iv)  
else  
continue
- vii) Preliminary data reconciliation
- viii) Measurement test for gross error identification
- ix) Simultaneous gross error compensation

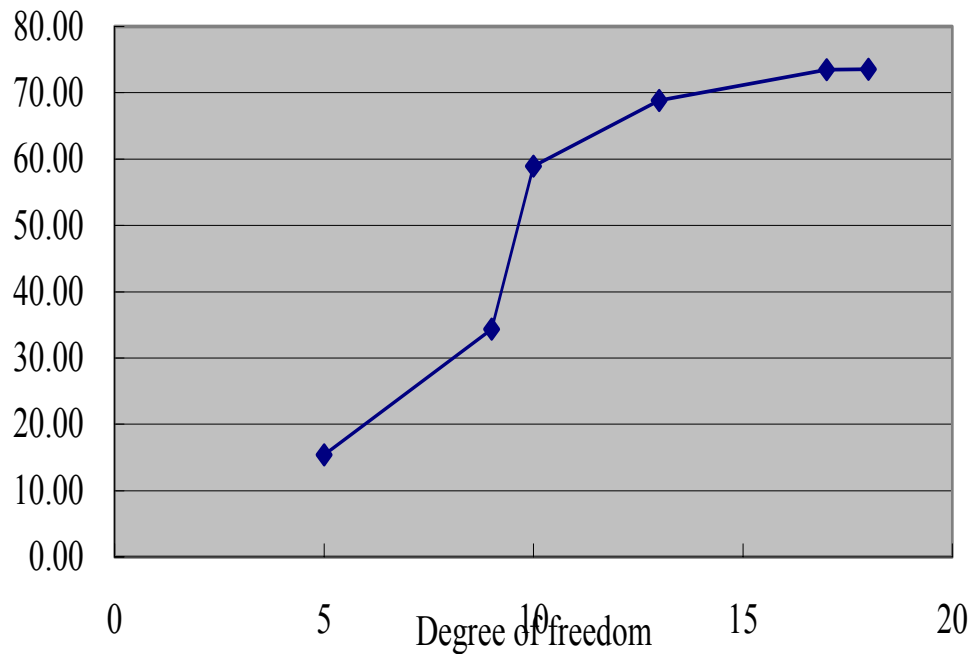
# LCI data rectification – confining models



- **The number of constraints**
  - 18 equations are required for complete component balances
- **The number of equations can be reduced by applying the proposed procedure**
- **The rectification results by the proposed algorithm are not changed significantly compared with complete constraints**

# LCI data rectification – confining models

Global test statistics



- The sums of relative errors for highest three cases are shown for comparison

	DOF= 13	DOF= 17	DOF= 18
Sum of Rel. err	0.19	0.16	0.12

# LCI data rectification – nonredundancy

- Public LCI data often neglect certain chemicals

Component	Mass, kg	
	Input	Output
Natural gas (fe	464.0	
H2O	922.0	
CH4		7.14
CO		2.50E-02
CO2(emission)		4.36E-01
NMVOG		9.28E-01
NO2		3.04E-01
SO2		1.00E-02
CO2(co-product)		1155.9
NH3		1000.0
<b>Total</b>	<b>1386.0</b>	<b>2157.6</b>

(SimaPro NH3 LCI)

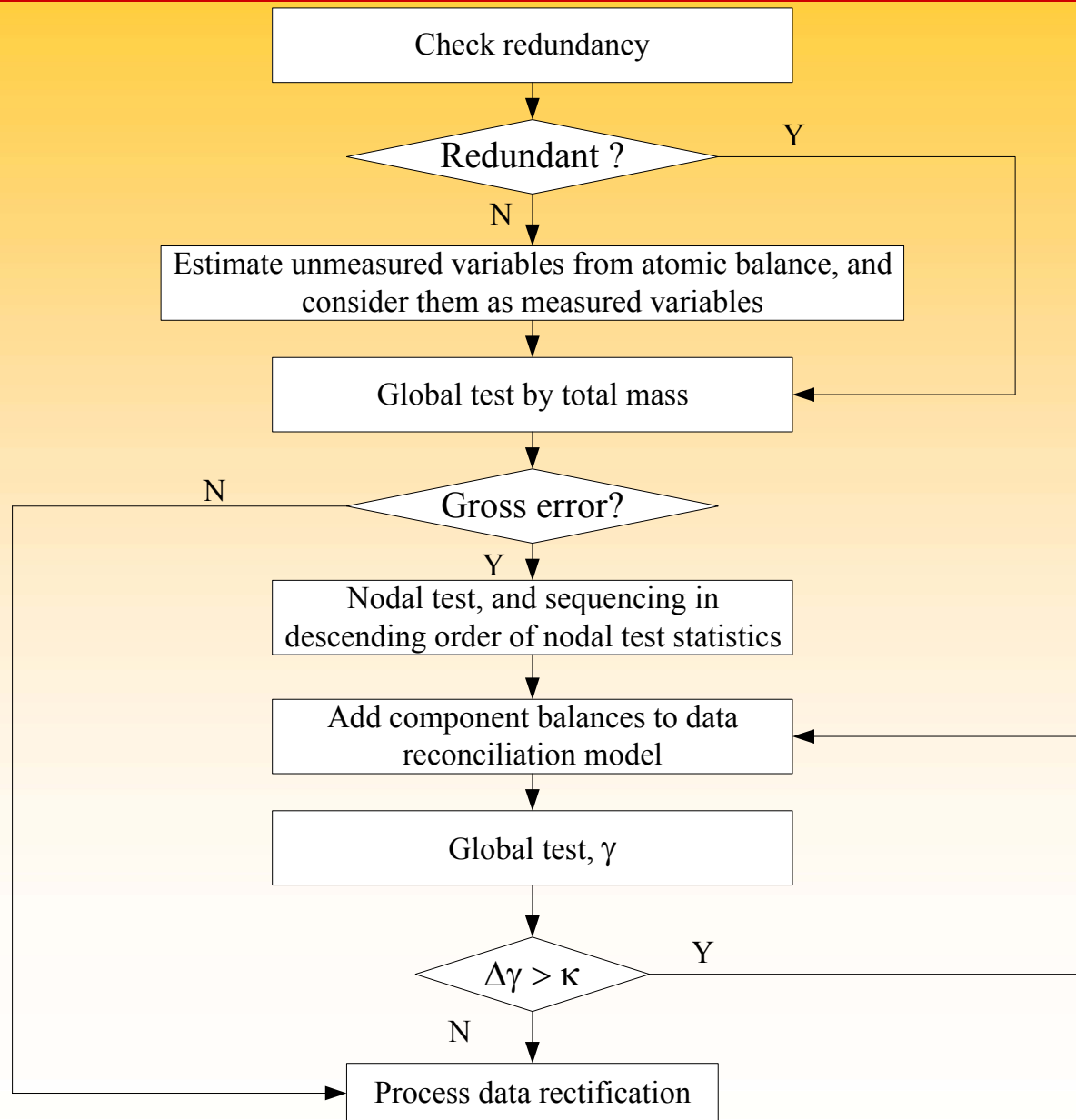
- Ammonia process consumes H2O and O2 for resources

- O2 and H2O are estimated by atomic balance

Component	Mass, kg	
	Input	Output
Natural gas	464.0	
H2O	922.0	
O2	17.8	
N2	822.4	
CH4		7.14
CO		2.50E-02
CO2(emission)		4.36E-01
NMVOG		9.28E-01
NO2		3.04E-01
SO2		1.00E-02
CO2(co-product)		1155.9
NH3		1000.0
<b>Total</b>	<b>2226.3</b>	<b>2157.6</b>

- Only if the estimated O2 and H2O are considered as measured variables, the system is redundant

# Algorithm for LCI data rectification



# Future work and conclusion

- **The methodology for LCI data rectification is proposed**
  - Multiscale data could be cooperated for data rectification
  - Large size of constraints could be reduce by confining procedure of process models
  - Nonredundancy problem is deal with atomic balance, which make system redundant
- **The proposed methodology will be applied to life cycles of LNG power plant and ammonium nitrate plant**