

## A Representation of Limiting Efficiencies for Thermochemical Cycles

*B C R Ewan, R W K Allen*

*Department of Chemical & Process Engineering, University of Sheffield,  
Mappin St, Sheffield S1 3JD, UK.*

### Introduction

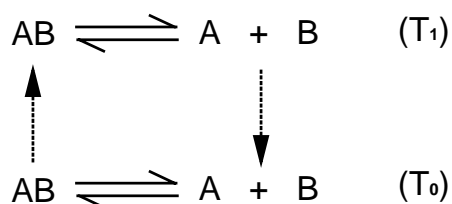
The present revival in interest in thermochemical cycles as a means of producing hydrogen has generated a number of publications which present new flowsheet variations for existing processes as well as additional cycles for consideration. In all of these, the overall process efficiency is a key parameter, although there remains some variability in the way in which this parameter is defined. Variations in process flowsheets and a lack of consistency in the way in which process efficiency is used can lead to significant uncertainties over the relative values of different cycles and suggests the adoption of a more consistent approach.

The value of a Carnot efficiency for determining the limiting efficiency of a thermal process producing work is taken for granted in power engineering and a similar approach for thermochemical cycles would aid in the assessment of the maximum efficiencies available, irrespective of the means of implementation and any subsequent flowsheet variations. The work sets out a basis for representing such a maximum possible efficiency, based on a step by step examination of each stage of the cycle in terms of its free energy change and heat requirements. The maximum thermodynamically allowed internal heat transfer is used to minimise external heat input and an overall efficiency is calculated based on the residual free energies and heat requirements, including the recombination of hydrogen and oxygen.

In this way, the thermochemical cycle is viewed as a mechanism for converting heat into work, as represented by the combination of stored chemical free energy and any additional work which the intermediate reactions can produce. The examination of the maximum theoretical efficiency of cycles in this way provides a useful starting point for any comparison between cycles and also allows identification of the strengths and weaknesses within cycles.

### Carnot efficiency equivalence

For the simplest cycle, this consists of an endothermic thermal decomposition at high temperature ( $T_1$ ) combined with a work recovery step at low temperature ( $T_0$ ).



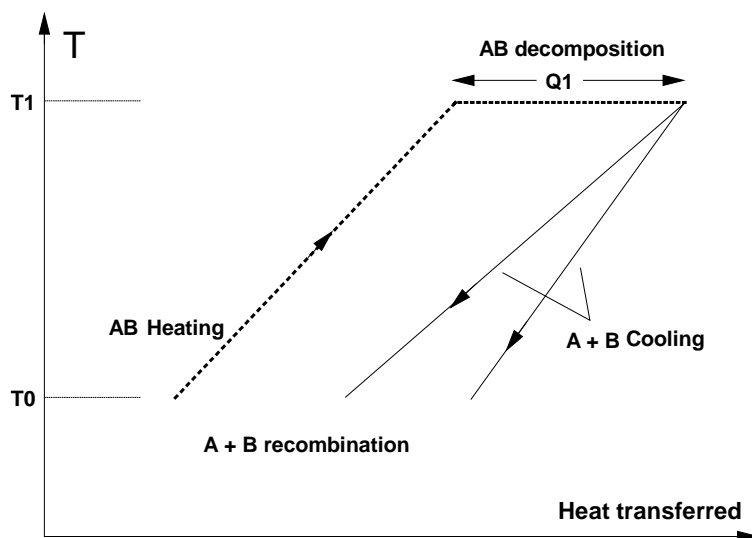
For the reactions from left to right, assuming to a first approximation that enthalpy and entropy changes are independent of temperature, the overall Gibbs free energy change for reactants and products at their reference condition, is

$$\Delta G_{\text{overall}} = (\Delta G_1 - \Delta G_0) = (T_0 - T_1) \Delta S \quad (1)$$

i.e. the cycle will provide work output ( $\Delta G_{\text{overall}} = -ve$ ) if  $\Delta S$  for the decomposition is a +ve

quantity. In this case  $\Delta G$  at the higher temperature is numerically lower, becoming zero at the decomposition temperature.

The heat balance for a simple AB decomposition can be usefully represented on a pinch diagram as shown in Figure 1. Here it assumed that the specific heats for AB heating and A + B cooling are independent of temperature.



**Figure 1.** Heating and cooling behaviour for simple AB decomposition.

The possibility for internal heat balancing is represented by two possible product cooling lines, showing both a shortfall in cooling heat with respect to the heating line and an excess of cooling heat leading to heat rejection. When standard conditions are used to represent the free energy and enthalpy changes, the work efficiency for the cycle is given by :

$$\eta = -\frac{\Delta G_{\text{overall}}}{Q} = \frac{\Delta G_0^\circ - \Delta G_1^\circ}{Q1 + \text{heat mismatch}} \quad (2)$$

where Q1 is the heat input at decomposition and 'heat mismatch' represents the heat transfer shortfall between A + B cooling and AB heating.

In the special case where the specific heat functions of products and reactants are identical, i.e.  $C_p(A+B, T) = C_p(AB, T)$ , then both the entropy changes and enthalpy changes are independent of temperature and exact heat matching results.

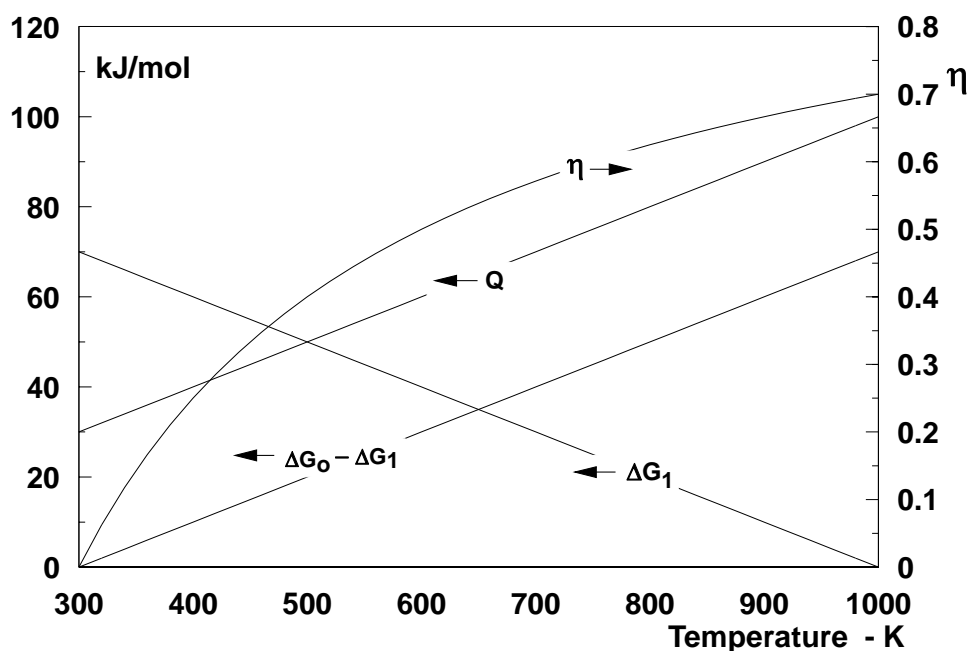
In this case,  $\Delta H_0^\circ = \Delta H_1^\circ$  and  $\Delta S_0^\circ = \Delta S_1^\circ$  and the efficiency then becomes :

$$\eta = \frac{\Delta G_0^\circ - \Delta G_1^\circ}{\Delta H_1^\circ - \Delta G_1^\circ} = \frac{\Delta H_0^\circ - T_0 \Delta S_0^\circ - \Delta H_1^\circ + T_1 \Delta S_1^\circ}{T_1 \Delta S_1^\circ} = 1 - \frac{T_0}{T_1} \quad (3)$$

For this special case heat is added only at the upper temperature  $T_1$ , and such simple cycles can provide the Carnot efficiency for converting heat into work.

Figure 2 shows the variation of the parameters of equation 3 with temperature for the hypothetical case of a system with  $\Delta H = 100$  kJ/mol and  $\Delta S = 100$  J/mol K.

As a result of the entropy and enthalpy independence with temperature, the cycle will provide the Carnot efficiency throughout the temperature range. At the decomposition temperature (1000 K),  $\Delta G_1 = 0$  and only heat is required to effect the conversion of 1 mole of reactants to products under standard conditions.



**Figure 2.** Variation of heat, work and efficiency with temperature for cycle with matched heating and cooling load.

Several decompositions of simple molecules approximate quite closely to this condition as shown for some examples in Table 1. In these cases,  $T_0 = 298$  K and  $Q$  is the greater of  $\Delta H_0^\circ$  and  $\Delta H_1^\circ$ .

**Table 1.**

Decomposition species	$\Delta H_1^\circ$	$\Delta H_0^\circ$	$\Delta G_0^\circ$	$T_1$	$\eta_{\text{Carnot}}$	$\Delta G_0^\circ / Q$
$\text{SO}_3 \rightarrow \text{SO}_2 + 0.5 \text{O}_2$	97.3	98.9	70.9	1055	0.717	0.716
$\text{H}_2\text{O} \rightarrow \text{H}_2 + 0.5 \text{O}_2$	251.2	241.8	228.5	4346	0.9311	0.909
$\text{CO}_2 \rightarrow \text{CO} + 0.5 \text{O}_2$	271.0	282.9	257.29	3340	0.911	0.908
$\text{CaCO}_3 \rightarrow \text{CaO} + \text{CO}_2$	165.8	178.2	130.5	1160	0.743	0.732

### Limiting efficiency methodology

Since thermochemical reactions form a closed set, comparison of the work efficiency for different cycles can usefully be assessed using the standard condition of 1 atm pressure for each of the steps in each cycle. For the simple cycle depicted above, the operation of the decomposition at a temperature where  $\Delta G_1^\circ = 0$ , is particularly useful since no external work is required to take the reactants to products under the standard conditions defined. As part of the objective of comparing the ability of a number of thermochemical cycles to convert heat into work, an initial approach has been taken to establish the limiting efficiency possible for these. Free energy changes for the chemical reactions are evaluated under standard conditions of 1 atm pressure for reactants and products. Since the underlying interest is in the use of heat to effect chemical changes, for reactions involving +ve values for both  $\Delta H$  and  $\Delta S$ , an operating temperature is chosen which results in  $\Delta G^\circ = 0$ , thus limiting any additional work required to bring the products to standard pressure. In some cases, the reaction temperature chosen in this way would exceed those of practical process conditions, and therefore an upper limit operating temperature of

1700 K has been imposed for all cycles. For those endothermic reactions with -ve values for  $\Delta S$ , the quoted literature value for the operating temperature has been chosen. Literature values for the operating temperature have also been chosen for any exothermic reactions in a cycle.

The main features of the analysis are described as follows :

1. The input to each cycle is water and the outputs are  $H_2$  and  $O_2$ , in all cases at standard conditions (1 atm, 298 K)
2. Reactions involving only heat inputs are carried out under equilibrium conditions and temperatures are chosen to satisfy  $\Delta G^\circ = 0$ , when possible, subject to a limit temperature of 1700 K.
3. Heat balancing is carried out between all of the heating and cooling branches of the process, with the constraint that the heat transfer temperature difference  $\Delta T$  is greater than or equal to zero.
4. Enthalpy changes are calculated using the HSC 5.1 chemistry package (1). Enthalpy and entropy values for some species have been updated in the database where necessary from published sources.
5. Efficiency is calculated through a combination of the work terms arising within the cycle and the total heat added.

The work components of the cycle are the Gibbs free energy changes for each of the fundamental steps required to complete the cycle, and are taken as :

- (a) Free energy work available from recombination, under standard conditions, of  $H_2/1/2O_2$  produced by the cycle ( $\Delta G_{298}^\circ (H_2/O_2)$ ). This is taken as -237 kJ/mol  $H_2$ .
- (b) Free energy work available from certain reactions within the set under standard conditions, characterised by -ve  $\Delta G^\circ$  values,  $\Delta G^\circ(-)$
- (c) Free energy work consumed by certain reactions within the set under standard conditions, characterised by +ve  $\Delta G^\circ$  values,  $\Delta G^\circ(+)$
- (d) Free energy work associated with the separation of reaction products. This is calculated as the negative of the mixing free energy

$$\Delta G_{sep} = -R T \sum_i n_i \ln(x_i) \quad (5)$$

where  $n_i$  and  $x_i$  are the number of moles and mole fraction of species  $i$  in the mixture respectively. This is a +ve quantity, consistent with the sign of the other work terms.

In representing an efficiency ( $\eta$ ) for the cycle, all free energy components providing output work,  $\Delta G^\circ(-)$  and  $\Delta G_{298}^\circ (H_2/O_2)$ , and consuming input work,  $\Delta G^\circ(+)$  and  $\Delta G_{sep}$ , are considered equivalent.

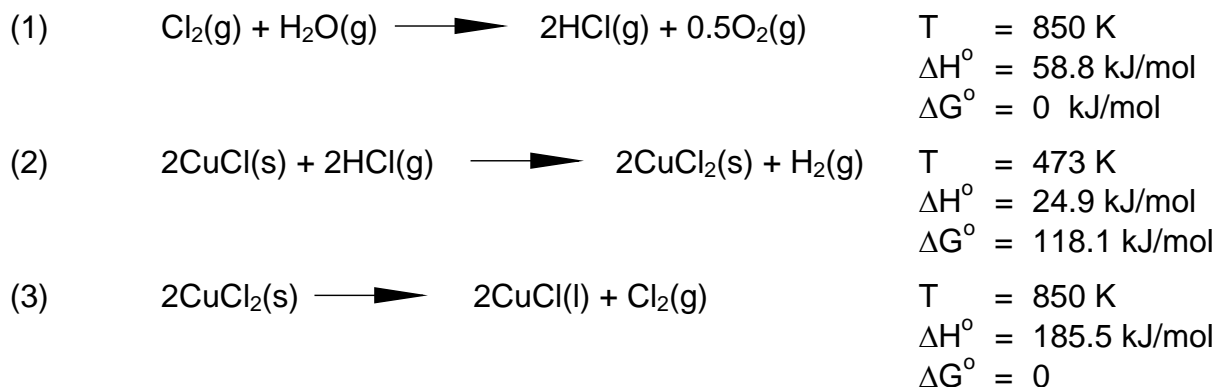
The efficiency thus becomes defined by :

$$\eta = - \frac{[\Delta G_{298}^\circ (H_2/O_2) + \sum \Delta G^\circ(-) + \sum \Delta G^\circ(+)] + \Delta G_{sep}}{\text{heat input}} \quad (6)$$

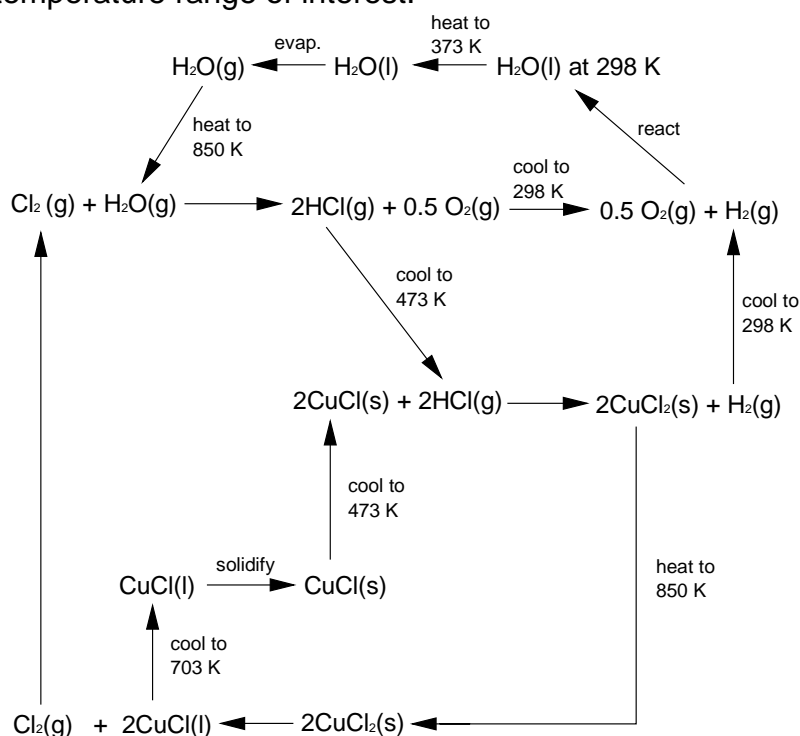
It is noted that the above definition of efficiency differs from those often used in the

thermochemical cycle literature where the HHV of hydrogen is frequently used in the numerator and any work capability of some reactions ( $\Delta G^\circ(-)$ ) is ignored. In some cases this may be a less generous definition, although it is believed that it provides some consistency with the normal calculation of a Carnot efficiency.

The representation of a cycle by a series of elementary steps is demonstrated for the case of the US Chlorine cycle (2), which involves the following three reactions :



The elementary steps required to evaluate a limiting efficiency are shown in Figure 2. Reaction (2) has a negative value for  $\Delta S$  and therefore does not provide the possibility of equilibrium under standard conditions for reactant and products, resulting in a positive  $\Delta G$  value in the temperature range of interest.



**Figure 2.** US Chlorine cycle for hydrogen production.

Table 2. summarises the individual steps representing the operation of the cycle.  $T_0$  and  $T_1$  define the starting and finishing temperatures of each step,  $\Delta G^\circ$  represents the standard Gibbs free energy change for the reactions and any work required to separate components for a further reaction step and  $Q_{\pm}$  is the heat change involved with the step (+ve when heat is added). Separation work terms are not included when reaction products exist in different phases. All of the thermochemical cycles considered are dealt with in the same way, i.e. heating, reaction, phase change and cooling.

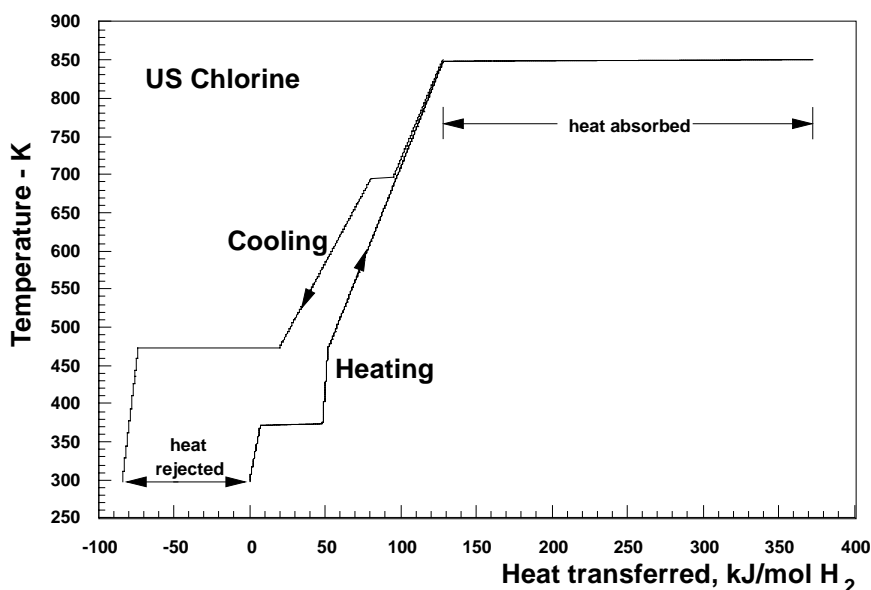
**Table 2.** Steps required to complete US Chlorine cycle.

Step No.	US Chlorine Cycle	To	T1	$\Delta G^\circ$	$Q_{\pm}$
		K	K	kJ	kJ
1	$\text{Cl}_2(\text{g}) + \text{H}_2\text{O}(\text{g}) \rightarrow 2\text{HCl}(\text{g}) + 0.5\text{O}_2(\text{g})$	850	850	0	58.8
	2HCl and 0.5O <sub>2</sub> separation at 473 K			4.92	
2	$2\text{CuCl}_2 \rightarrow 2\text{CuCl}(\text{l}) + \text{Cl}_2(\text{g})$	850	850	0	185.5
3	$2\text{CuCl}_2(\text{s}) \rightarrow 2\text{CuCl}_2(\text{s})$	473	850		62.46
4	$\text{H}_2\text{O}(\text{l}) \rightarrow \text{H}_2\text{O}(\text{l})$	298	373		7.5
5	$\text{H}_2\text{O}(\text{l}) \rightarrow \text{H}_2\text{O}(\text{g})$	373	373		40.9
6	$\text{H}_2\text{O}(\text{g}) \rightarrow \text{H}_2\text{O}(\text{g})$	373	850		17.5
7	$2\text{CuCl}(\text{l}) \rightarrow 2\text{CuCl}(\text{l})$	850	703		-17.8
8	$2\text{HCl}(\text{g}) \rightarrow 2\text{HCl}(\text{g})$	850	473		-22.54
9	$2\text{CuCl}(\text{l}) \rightarrow 2\text{CuCl}(\text{s})$	703	703		-14.2
10	$2\text{CuCl}(\text{s}) \rightarrow 2\text{CuCl}(\text{s})$	703	473		-55.7
11	$\frac{1}{2} \text{O}_2(\text{g}) \rightarrow \frac{1}{2} \text{O}_2(\text{g})$	850	298		-17.5
12	$2\text{CuCl} + 2\text{HCl}(\text{g}) \rightarrow 2\text{CuCl}_2 + \text{H}_2(\text{g})$	473	473	118.1	-93.2
13	$\text{H}_2(\text{g}) \rightarrow \text{H}_2(\text{g})$	473	298		-5.0

For each cycle it is confirmed that an overall energy balance is satisfied, i.e.,

$$\sum_i \Delta G_i^0(\text{reactions}) = \sum_i Q_i$$

This also includes the additional heat rejected at 298 K when the hydrogen and oxygen are recombined (-48.6 kJ/mol). For an efficiency calculation, it is necessary to know the overall heat input requirement and this is evaluated on the basis of the maximum possible heat transfer from the cooling side to the heating side of the process. This is most easily calculated using a pinch diagram for each of the cycles. These are constructed for the limiting case of a heat transfer temperature difference  $\Delta T = 0$  degrees, and refer to the production of 1 mol of H<sub>2</sub>. The pinch diagram for US Chlorine cycle corresponding to Table 2 is shown in Figure 3.



**Figure 3.** Pinch diagram for US Chlorine cycle.

## Examination of 10 Cycles

A selection of the preferred cycles originally proposed by Brown et al (3) have been examined in the same way and the operating conditions and thermodynamic parameters for these under standard conditions are collected together in Table 3.

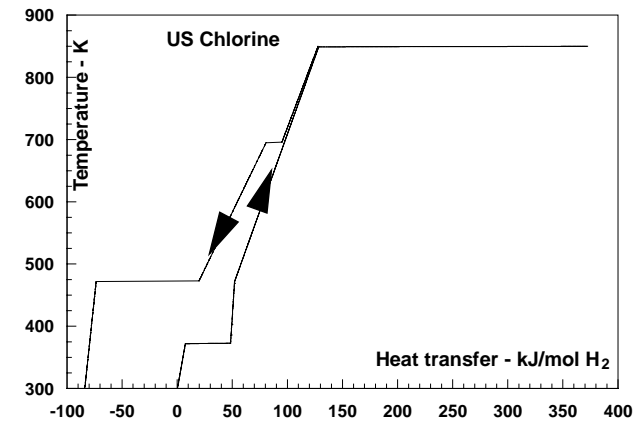
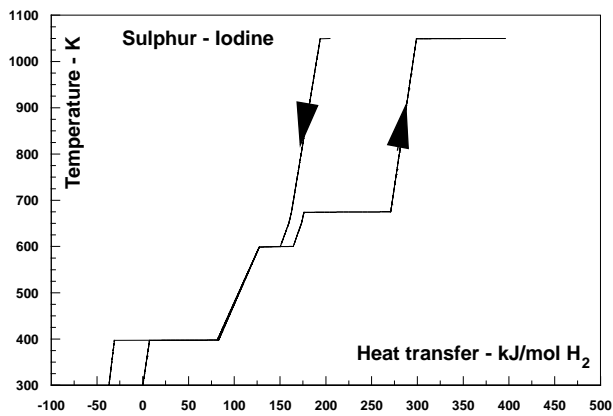
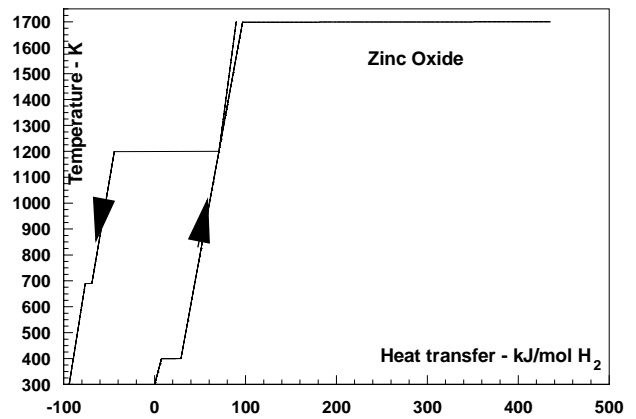
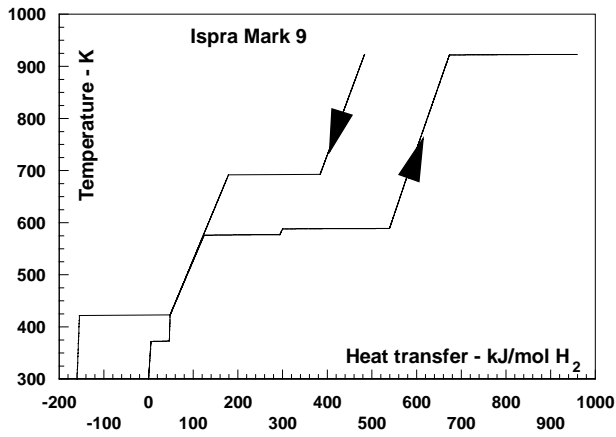
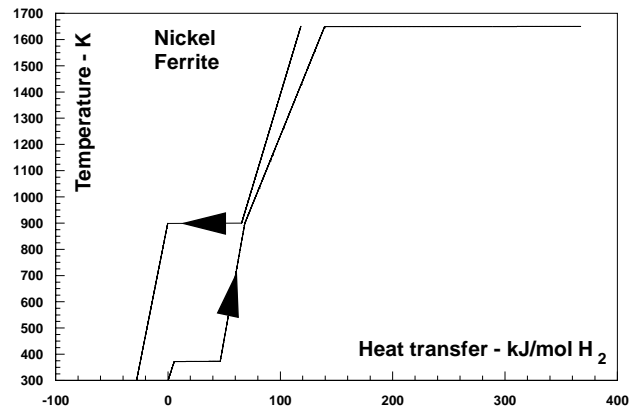
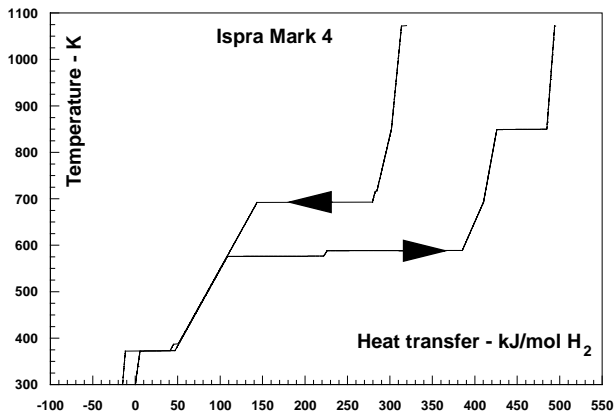
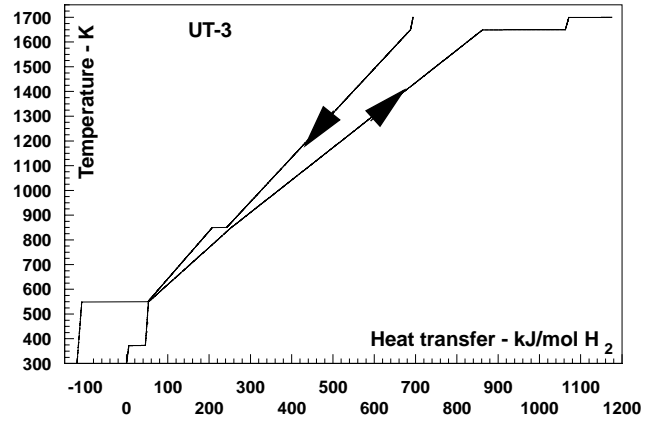
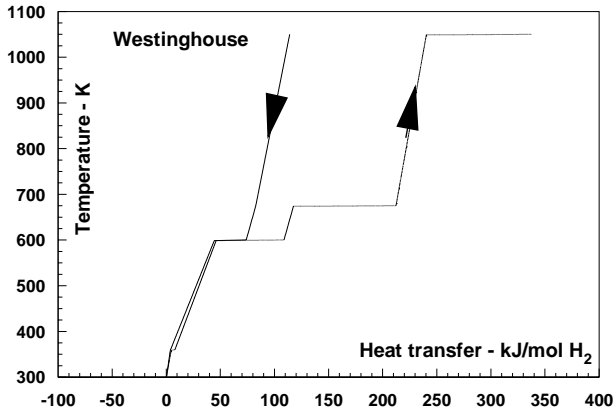
**Table 3.**

	Reaction set	$\Delta G^\circ$ (kJ)	$\Delta H^\circ$ (kJ)	E/T *	T (K)
Westinghouse (4)	$\text{SO}_2(\text{g}) + 2\text{H}_2\text{O}(\text{l}) \rightarrow \text{H}_2\text{SO}_4(\text{l}) + \text{H}_2(\text{g})$ $\text{H}_2\text{SO}_4(\text{g}) \rightarrow \text{H}_2\text{O}(\text{g}) + \text{SO}_3(\text{g})$ $\text{SO}_3(\text{g}) \rightarrow \text{SO}_2(\text{g}) + \frac{1}{2}\text{O}_2(\text{g})$	75.7 0 0	78.9 94.6 97.3	E T T	360 675 1050
Sulphur - Iodine (3)	$\text{SO}_2(\text{g}) + 16\text{H}_2\text{O}(\text{l}) + 9\text{I}_2(\text{l}) \rightarrow$ $\text{H}_2\text{SO}_4(\text{aq}) + 2\text{HI} \cdot 10\text{H}_2\text{O} \cdot 8\text{I}_2(\text{l})$ $\text{H}_2\text{SO}_4(\text{aq}) + [2\text{HI} \cdot 10\text{H}_2\text{O} \cdot 8\text{I}_2](\text{l}) \rightarrow$ $[\text{H}_2\text{SO}_4 + 4\text{H}_2\text{O}](\text{l}) + 2\text{HI}(\text{g}) + [10\text{H}_2\text{O} + 8\text{I}_2(\text{l})$ $\text{H}_2\text{SO}_4(\text{g}) \rightarrow \text{H}_2\text{O}(\text{g}) + \text{SO}_3(\text{g})$ $\text{SO}_3(\text{g}) \rightarrow \text{SO}_2(\text{g}) + \frac{1}{2}\text{O}_2(\text{g})$ $2\text{HI}(\text{g}) \rightarrow \text{H}_2(\text{g}) + \text{I}_2(\text{g})$	-60.8 156.5 0 0 22.7	-133.3 232 94.6 97.3 12.1	T T T T T	398 398 675 1050 650
US Chlorine (2)	$\text{Cl}_2(\text{g}) + \text{H}_2\text{O}(\text{g}) \rightarrow 2\text{HCl}(\text{g}) + \frac{1}{2}\text{O}_2(\text{g})$ $2\text{CuCl}(\text{s}) + 2\text{HCl}(\text{g}) \rightarrow 2\text{CuCl}_2(\text{s}) + \text{H}_2(\text{g})$ $2\text{CuCl}_2(\text{s}) \rightarrow 2\text{CuCl}(\text{l}) + \text{Cl}_2(\text{g})$	0 118.1 0	58.8 24.9 185.5	T T T	850 473 850
Zinc oxide (5)	$\text{ZnO}(\text{s}) \rightarrow \text{Zn}(\text{g}) + \frac{1}{2}\text{O}_2(\text{g})$ $\text{Zn}(\text{s}) + \text{H}_2\text{O}(\text{l}) \rightarrow \text{ZnO}(\text{s}) + \text{H}_2(\text{g})$	122.9 -89.1	461.8 -67.7	T T	1700 400
UT - 3 (6)	$\text{CaBr}_2(\text{s}) + \text{H}_2\text{O}(\text{g}) \rightarrow \text{CaO}(\text{s}) + 2\text{HBr}(\text{g})$ $\text{CaO}(\text{s}) + \text{Br}_2(\text{g}) \rightarrow \text{CaBr}_2(\text{s}) + 0.5\text{O}_2(\text{g})$ $\text{Fe}_3\text{O}_4(\text{s}) + 8\text{HBr}(\text{g}) \rightarrow 3\text{FeBr}_2(\text{s}) + \text{Br}_2(\text{g}) + 4\text{H}_2\text{O}(\text{g})$ $3\text{FeBr}_2 + 4\text{H}_2\text{O}(\text{g}) \rightarrow \text{Fe}_2\text{O}_3 + \text{H}_2(\text{g}) + 6\text{HBr}(\text{g})$	61.77 -39.69 -99.7 0	165.57 -74.15 -259.4 199.7	T T T T	1700 850 550 1650
Gaz de France (2)	$2\text{K}(\text{l}) + 2\text{KOH}(\text{l}) \rightarrow 2\text{K}_2\text{O}(\text{s}) + \text{H}_2(\text{g})$ $2\text{K}_2\text{O}(\text{s}) \rightarrow 2\text{K}(\text{g}) + \text{K}_2\text{O}_2(\text{l})$ $\text{K}_2\text{O}_2(\text{s}) + \text{H}_2\text{O}(\text{l}) \rightarrow 2\text{KOH}(\text{s}) + 0.5\text{O}_2(\text{g})$	260.9 210.1 -151.4	71.9 390.7 -121.5	T T T	1000 1100 400
Ispra Mark 4 (7)	$\text{Cl}_2(\text{g}) + \text{H}_2\text{O}(\text{g}) \rightarrow 2\text{HCl}(\text{g}) + 0.5\text{O}_2(\text{g})$ $2\text{FeCl}_2(\text{s}) + 2\text{HCl}(\text{g}) + \text{S}(\text{s}) \rightarrow 2\text{FeCl}_3(\text{s}) + \text{H}_2\text{S}(\text{g})$ $\text{H}_2\text{S}(\text{g}) \rightarrow \text{S}(\text{g}) + \text{H}_2(\text{g})$ $2\text{FeCl}_3(\text{g}) \rightarrow \text{Cl}_2(\text{g}) + 2\text{FeCl}_2(\text{s})$	0 107.2 189.5 -29.3	58.8 54.5 306.3 -166.0	T T T T	850 373 1073 693
Ispra Mark 7B (7)	$1.5\text{Fe}_2\text{O}_3(\text{s}) + 3\text{Cl}_2(\text{g}) \rightarrow 3\text{FeCl}_2(\text{l}) + 2.25\text{O}_2(\text{g})$ $3\text{FeCl}_2(\text{l}) + 4\text{H}_2\text{O}(\text{g}) \rightarrow \text{Fe}_3\text{O}_4(\text{s}) + 6\text{HCl}(\text{g}) + \text{H}_2(\text{g})$ $\text{Fe}_3\text{O}_4(\text{s}) + 0.25\text{O}_2(\text{g}) \rightarrow 1.5\text{Fe}_2\text{O}_3(\text{s})$ $6\text{HCl}(\text{g}) + 1.5\text{O}_2(\text{g}) \rightarrow 3\text{Cl}_2(\text{g}) + 3\text{H}_2\text{O}(\text{g})$	0 0 -73.8 -39.5	382.4 195.0 -117.6 -175.3	T T T T	1000 1175 623 673
Ispra Mark 9 (7)	$3\text{FeCl}_3(\text{g}) \rightarrow 1.5\text{Cl}_2(\text{g}) + 3\text{FeCl}_2(\text{s})$ $1.5\text{Cl}_2(\text{g}) + \text{Fe}_3\text{O}_4 + 6\text{HCl}(\text{g}) \rightarrow$ $3\text{FeCl}_3(\text{s}) + 3\text{H}_2\text{O}(\text{g}) + 0.5\text{O}_2(\text{g})$ $3\text{FeCl}_2(\text{s}) + 4\text{H}_2\text{O}(\text{g}) \rightarrow \text{Fe}_3\text{O}_4 + 6\text{HCl} + \text{H}_2(\text{g})$	-41.9 -34.8 48.3	-248.5 -237.2 334.6	T T T	693 423 923
Nickel Ferrite (8)	$0.5\text{NiMnFe}_4\text{O}_8 \rightarrow 0.5\text{NiMnFe}_4\text{O}_6 + 0.5\text{O}_2(\text{g})$ $0.5\text{NiMnFe}_4\text{O}_6 + \text{H}_2\text{O}(\text{g}) \rightarrow 0.5\text{NiMnFe}_4\text{O}_8 + \text{H}_2(\text{g})$	0 97.7	228.0 32.0	T T	1650 900

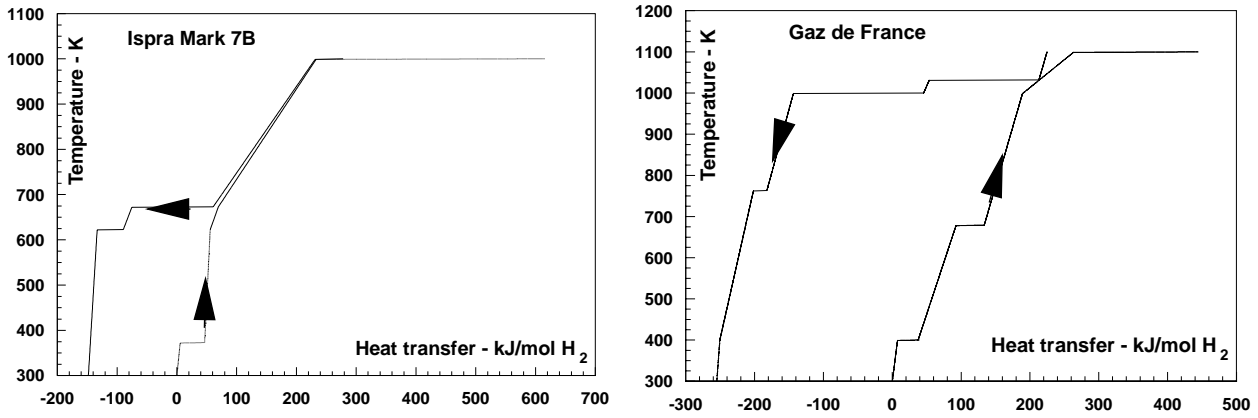
\* Refers to thermal or electrochemical step

In the same way as described for the US Chlorine cycle above, a detailed heating and cooling scheme for the cycles of Table 3 has been derived, based on the needs of individual species involved transforming from products of one reaction to reactants of another.

The heating and cooling needs of these have been presented in pinch diagram form as before and are shown in Figures 4.







**Figure 4.** Pinch diagrams for thermochemical cycles of Table 3 showing heating ( $\uparrow$ ) and cooling ( $\downarrow$ ) curves.

The definition of efficiency (Eq. 6) indicates that the maximum value for this is achieved when use is made of any available work arising from the cycle reactions, in addition to that from the  $H_2$  and  $O_2$  produced. The efficiency information in Table 4 is therefore presented in two ways, represented by  $\eta_1$  and  $\eta_2$ . These are defined by :

$$\eta_1 = - \frac{[\Delta G_{298}(H_2/O_2) + \sum \Delta G^\circ(-) + \sum \Delta G^\circ(+) + \sum \Delta G_{sep}]}{\text{heat input}} \quad (7)$$

$$\eta_2 = - \frac{[\Delta G_{298}(H_2/O_2) + \sum \Delta G^\circ(+) + \sum \Delta G_{sep}]}{\text{heat input}} \quad (8)$$

These definitions reflect the fact that additional measures need to be implemented to realise the full potential of cycles which provide additional sources of work ( $\eta_1$ ) and without these measures the lower efficiency ( $\eta_2$ ) will be the maximum available. In cases where  $\eta_1 = \eta_2$  in the table, no additional work  $\Delta G^\circ(-)$ , is available and no additional measures are required. The pinch diagrams provide the necessary information on heat demand and heat rejected, and the overall heat and work inputs and outputs for the cycles are summarised in Table 4.

**Table 4.**

Process	Heat input kJ/mol $H_2$	Heat rejection kJ/mol $H_2$	Work input kJ/mol $H_2$	$\eta_1$	$\eta_2$
Westinghouse	222.5	0	87.7	0.67	0.67
UT - 3	441.5	157.7	86.3	0.60	0.31
Ispra Mark 4	174.4	15.2	155.1	0.62	0.45
Nickel ferrite	249.3	28.0	97.7	0.56	0.56
Ispra Mark 9	393.3	183.3	76.7	0.53	0.36
Zinc oxide	341.7	94.5	136.4	0.56	0.29
Sulphur - Iodine**	192.0	37.0	179.3	0.51	0.19
US Chlorine	258.9	84.0	123.0	0.44	0.44
Ispra Mark 7B	337.7	148.0	249.1	0.30	0
Gaz de France	219.8	255.0	471.0	0	0

\*\* Thermodynamic data for the Bunsen reaction calculated from the strong acid model (9)

## Discussion

The examples shown have been chosen as they typify the behaviour of different classes of thermochemical cycles.

Those cycles which approximate most closely with the heating and cooling curves of Figure 1 are expected to have the highest efficiencies due to good heat matching.

Differences in the heating and cooling curves arise from specific heat differences, isothermal phase changes and chemical reaction heats, in particular the relative positioning of these on the temperature axis. Good heat matching behaviour is associated with similar specific heat values for reactants and products across the temperature range, or similar isothermal heat absorption and rejection behaviour, with the rejection temperature located above the absorption temperature. A number of the isothermal stages in Figure 4 are also connected with work inputs or outputs required to achieve standard conditions and these will often involve related heat changes. In some cases, work inputs appear as work outputs via the +ve enthalpy changes which result, whilst in others the work inputs appear as rejected heat due to the -ve entropy change associated with a reaction whose equilibrium lies to the left.

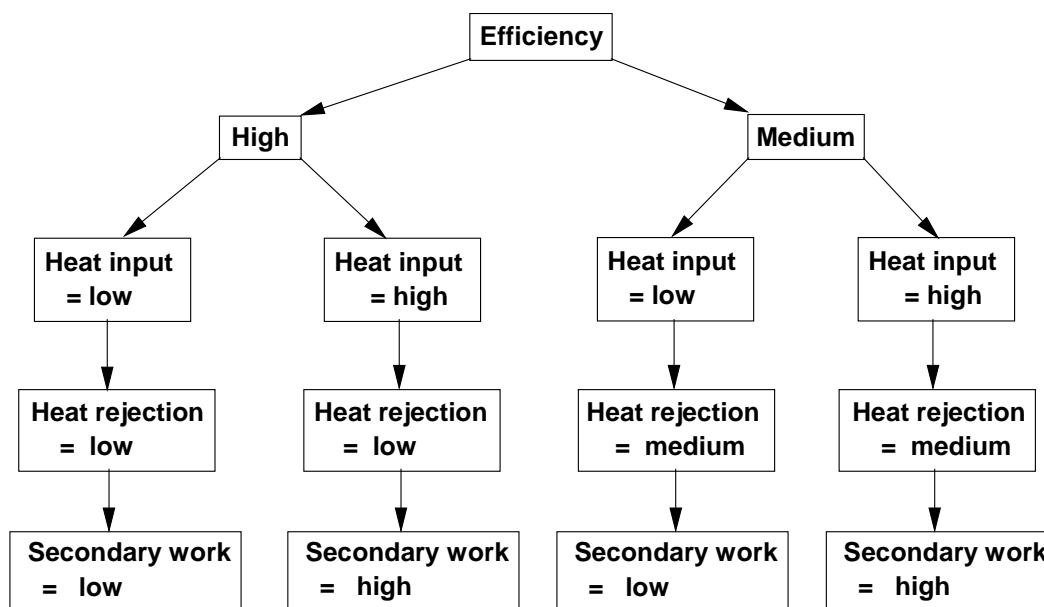
One can arbitrarily define high, medium and low values for efficiency, heat input, heat rejected and the secondary work, characterised by the  $\Delta G^\circ(-)$  terms.

The ranges for these, based on the above cycles, are shown in Table 5.

**Table 5.**

	Efficiency	Heat input (kJ)	Heat rejected (kJ)	Secondary work (kJ)
High	$\geq 0.6$	350 - 450	250 - 400	$> 100$
Medium	0.5 - 0.6	250 - 350	150 - 250	50 - 100
Low	$< 0.5$	150 - 250	0 - 100	0 - 50

The behaviour of those cycles with high and medium efficiencies is observed to follow the pattern depicted in Figure 5.



**Figure 5.**

This shows that high or medium efficiency is particularly associated with low or medium levels of heat rejection respectively. In both cases the level of heat input can be high or low. When this is high, the level of secondary work tends to be high, i.e. the additional heat input can be transformed into productive work terms without loss of overall efficiency. This normally means that work input arises from an enthalpy demand from a reaction rather than a -ve entropy change. The UT3 and Zinc oxide cycles are an example of such behaviour, which also show significant differences between  $\eta_1$  and  $\eta_2$  due to the conversion of input work, arising from an enthalpy demand, into output work.

Low efficiencies are generally characterised by medium levels of heat input, relatively high levels of heat rejection and work input, and medium - low levels of secondary work. In these cases, high levels of work input tend to give rise to high levels of heat rejection, i.e. the processes act to convert input work into heat. Such behaviour can often be traced to two dominant causes, (i) reactions with large +ve  $\Delta G$  values arising from large -ve entropy changes, which require significant work input to achieve standard conditions, giving rise to large isothermal heat rejection and (ii) serious mis-matches between the heating and cooling sides of the process due to poorly aligned phase changes. Figure 4 reveals a number of these features, the Gaz de France cycle showing both adverse features. In this particular case, for two of the reactions ( $K_2O$  decomposition and K/KOH reaction), the equilibrium lies strongly to the left requiring significant input work to meet standard conditions, with result that overall, no nett work is produced on  $H_2/O_2$  recombination. The above approach has a number of features which are useful in making comparisons between thermochemical cycles and with other heat - work processes. Some of these include :

- an evaluation, without the use of process flowsheeting, of the maximum thermal efficiency which a cycle can provide
- identification of the sources of work produced by the cycle and the feasibility of making use of all  $\Delta G^\circ(-)$  contributions to the overall work output
- the provision of a starting point for process optimisation, identifying the main geometrical needs for heat transfer
- assessment of the relative efficiencies of heat - electricity cycles and thermochemical cycles for use with hybrid cycles
- the basis for improvement of existing cycles through chemicals selection and better positioning of isothermal heat processes

## References

1. HSC Chemistry v 5.1, Outokumpu Research, Finland, 2002
2. L O Williams, Hydrogen Power, Pergamon (1980)
3. J H Norman, G E Besenbruch, L C Brown, D R O'Keefe, L C Allen, 'Thermo-chemical Water-Splitting Cycle, Bench Scale Investigations and Process Engineering', Final Report GA-A16713, may 1982, General Atomics.
4. L E Brecher, S Spewock, C J Warde, 'The Westinghouse Sulfur Cycle for the Thermochemical Decomposition of Water', *Int J Hydrogen Energy*, 2, 7 - 15, (1977)
5. A Steinfeld, 'Solar hydrogen production via a two-step water-splitting thermochemical cycle based on Zn/ZnO redox reactions', *Int J Hydrogen Energy* 27(6), 611 - 619 (2002)
6. J K Funk, R M Reinstorm, 'Energy requirements in the production of hydrogen from water', *Ind Eng Chem Proc Des Develop* 5, 336 - 342 (1966)
7. G E Beghi, 'A decade of research on thermochemical hydrogen at the joint research center, Ispra', *Int. J Hydrogen Energy* 11, 761 - 771 (1986)

8. Y Tamaura, Ainfeld, P Kuhn, K Ehrensberger, 'Production of solar hydrogen by a novel, 2-step, water-splitting thermochemical cycle', *Energy* 20(4), 325 -330, (1995)
9. H Engels, K F Knoche, 'Vapor pressures of the system HI/H<sub>2</sub>O/I<sub>2</sub> and H<sub>2</sub>, *Int J Hydrogen Energy* 12 (11), 703 - 707 1986