Probabilistic Path Planning for Cooperative Target Tracking Using Aerial and Ground Vehicles

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Abstract— In this paper, we present a probabilistic path planning algorithm for tracking a moving ground target in urban environments using UAVs in cooperation with UGVs. The algorithm takes into account vision occlusions due to obstacles in the environments. The target state is modeled using the dynamic occupancy grid and the probability of the target location is updated using Bayesian filtering. Based on the probability of the target's current and predicted locations, the path planning algorithm is designed to generate paths for a single UAV or UGV maximizing the sum of probability of detection over a finite look-ahead. For target tracking using multiple vehicle collaboration, a decentralized planning algorithm using an auction scheme generates paths maximizing the sum of joint probability of detection over the finite look-ahead horizon. Simulation results show the proposed algorithm is successful in solving the target tracking problem in urban environments.

I. INTRODUCTION

Small unmanned air vehicles (UAVs) have recently found applications in the task of tracking moving targets on the ground. Many approaches to this topic have been presented in the last few years [1]–[4]. The main advantages of target tracking using UAVs are that they have a wide field of view and can cover large areas quickly. However, sensors mounted on UAVs are unable to localize the target on the ground accurately due to the limitations on altitude and airspeed. On the other hand, unmanned ground vehicles (UGVs) are slower with limited field of view, but they are capable of getting closer to targets and resolving their relative locations with greater accuracy [5]. In addition, in a pursuit-evasion scenario, a ground vehicle has the ability to "capture" a target, whereas an aerial vehicle can only observe and inform. Accordingly, the complimentary strength of air and ground based sensors motivates the cooperative use of both UAVs and UGVs for target tracking.

Some approaches to the target tracking problem using both UAVs and UGVs have been proposed. Reference [6] describes an information based approach to UAV/UGV cooperative tracking. This approach works well when the targets are static, and when the environment is relatively free of occlusions, allowing the efficient use of log-likelihood filters, but it is ill-suited to tracking evasive targets in complicated urban environments. Air and ground vehicle cooperation in

a probabilistic pursuit-evasion framework is considered in reference [7]. But this approach does not consider sensor data fusion, complex terrain, or planning for occluded vision. Reference [8] presents a control scheme that guides a team of UGVs into a formation to effectively "corral" targets into a specific region, while a team of UAVs fly over the formation to detect targets. The approach assumes large teams of air and ground robots, and does not consider the effect of occlusions, non-navigable terrain, and data fusion.

This paper presents a probabilistic path planning algorithm for tracking a moving target in urban environments using both UAVs and UGVs. Urban terrain complicates the tracking problems because the large number of buildings and other obstacles occlude the line of sight between the sensors and the target. The main contribution of the proposed planning algorithm is to take into account the occlusions due to obstacles. We model the target state using a dynamic occupancy grid and use a second-order Markov chain model to represent the target motion. The probability of the target location is updated using Bayesian filtering. For designing the planning algorithm, we define the probability of detection given the locations of the sensor and the target using a Gaussian function of the distance between the sensor and the target. To include the effect of occlusions, the probability of detection for the configurations where occlusions exist is assigned as zero. Based on the probability of detection of the target's current and predicted future locations, we design the path planning algorithm for independent target tracking by a single vehicle (UAV or UGV). The algorithm generates optimal paths maximizing the sum of probability of detection over a finite look-ahead horizon. Optimal paths are found using dynamic programming. For cooperative target tracking using multiple UAVs and UGVs, we define the joint probability of detection and design a decentralized suboptimal approach relying on an auction algorithm to generate optimal paths maximizing the sum of joint probability of detection over the finite look-ahead horizon. The advantage of this approach is that it results in linear computational growth as the number of vehicles increases.

This paper is organized as follows. Section II describes the target state modeling and estimation using a dynamic occupancy grid. In Section III, the path planning algorithm for target tracking using a single UAV or UGV is introduced. Section IV introduces the path planning algorithm for cooperative target tracking using multiple UAVs and UGVs. Simulation results are shown in Section V.

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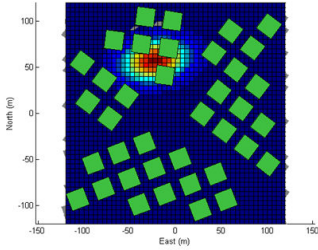
Fig. 1.   The dynamic target occupancy grid.

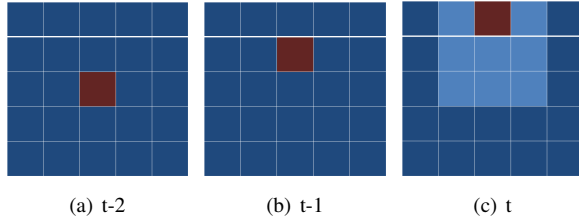| (a) t-2	(b) t-1	(c) t

Fig. 2.   The target motion model. The target moves up from time step $t-2$ to $t-1$. Accordingly, the target will be assumed to move up with a high probability P_c at time step t. The probability $1-P_c$ will be equally divided between the neighboring cells.

II. TARGET STATE MODELING AND ESTIMATION

In order to plan paths for UAV/UGV to track the target, we must estimate the target state at each time step. In this section, we describe the method for target state estimation using a dynamic occupancy grid. A discrete probabilistic model of the target motion is constructed to predict the target location using a second-order Markov chain, and is then combined with Bayes-filtered sensor measurements to update the target location.

Using a dynamic occupancy grid is a classical approach to address the problem of generating consistent maps from noisy and uncertain measurement data [9]. The basic idea is to represent the map as a spatial grid, where each occupancy cell has a random variable s associated with it. The random variable s has two states, *occupied* and *empty*, which correspond to the occupancy of that cell. We use a dynamic occupancy grid to represent changing belief about the target location. Fig. 1 shows the dynamic occupancy grid of the target location. To calculate the probability that the target will be in a given cell at time t we use data from two previous time steps, which is a second order Markov model, and assume that the target will most likely proceed in its direction, as shown in Fig. 2. In the figure, the target moves up from time step $t-2$ to $t-1$. Accordingly, the target will be assumed to move up with a high probability P_c at time t. The probability $1-P_c$ will be equally divided between the neighboring cells, as shown in Fig. 2 (c). One of the advantages of using a probabilistic model of the target motion is that several potential target paths can be captured simultaneously.

Let $x_T(t)$ represent the target state at time t and let $P(x_T(t))$ represent the posterior probability that the target is

at $x_T(t)$, which is used as the prior probability of the target location at time $t+1$. The dynamic occupancy grid approach utilizes Bayesian filtering to implement approximate posterior estimation for each grid cell. Bayesian filtering consists of two phases: prediction and update. The prediction phase uses the target motion model given by $P(x_T(t+1)|x_T(t))$, which represents the probability that the target is at $x_T(t+1)$ at time $t+1$ given its location at time t. As mentioned above, we represent the target motion model using a second order Markov chain. The predicted target probability at time $t+1$ before the new measurements are taken into account are then given by

$$\bar{P}(x_T(t+1)) = \int P(x_T(t+1)|x_T(t))P(x_T(t))dx_T(t). \quad (1)$$

When the position of the target is observed by a member of the UAV/UGV team, the occupancy grid is updated to reflect the new information. This update is the measurement phase in the Bayesian filtering. The measurement model is represented by $P(z_i|x_T)$ which is the probability of receiving the measurement z_i from the ith observation platform (UAV/UGV) given that the target is located at x_T. The posterior probability that the target is $x_T(T+1)$ at time step $t+1$ is given by

$$P(x_T(t+1)) = \eta P(z_i|x_T)\bar{P}(x_T(t+1)), \quad (2)$$

where η is a normalization factor. Eq. (1) and Eq. (2) constitute the Bayesian filtering for updating the posterior probability of the target location. We should note that if a measurement is not received at every time step, then the probability of the target location is updated using Eq. (1). The measurement update in Eq. (2) occurs when a measurement is received from any vehicle and may be applied multiple times if measurements are received from multiple platforms at the same time. At the beginning of an observation mission, when the target has not been observed by any platforms, the probability of the target location can be initialized as a uniform distribution. However, if priori information is known, then the probability map can be initialized using this information.

III. PATH PLANNING FOR A SINGLE VEHICLE BASED ON PREDICTED TARGET BEHAVIOR

Given the probability of the target's current and probable future locations computed using the procedure described in the previous section, we design a path planning algorithm for tracking of the target by a single vehicle (UAV or UGV). The objective of the algorithm is to generate a parameterized path over a finite look-ahead T_L. Future paths can be parameterized in a number of different ways including a set of roll angles or a set of waypoints. To be general, let Θ_i represent the path parameterization over the time horizon $[t, t+T_L]$. We use the notation $x_i(t, \sigma, \Theta_i)$ to represent the predicted location of the ith sensor platform (UAV/UGV) at time $t+\sigma$, given its current location at time t, and the path parameterization Θ_i, where $\sigma \in [0, T_L]$.
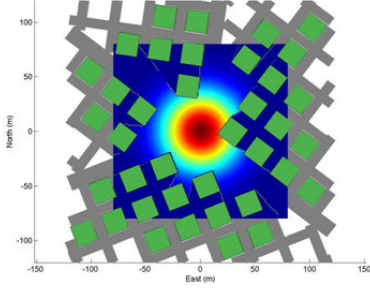
Fig. 3. The probability of detection when buildings occlude the line of sight vector. The location of the target is at (0,0) and the location of the sensor is varied.

Let D_i represent the event that the target is detected by the ith vehicle, and let $P(D_i|x_i,x_T)$ represent the probability that the target is detected by the ith vehicle when it is at x_i and the target is at x_T. We assume that the sensor is gimbaled and pointing toward the target. We represent $P(D_i|x_i,x_T)$ as a Gaussian function of the distance between the target and the sensor:

$$P(D_i|x_i,x_T) = \eta \exp(-\frac{1}{2}(x_i - x_T)^\top \Sigma^{-1}(x_i - x_T)), \quad (3)$$

where Σ is the covariance and η is a normalization factor. Please note that other non-Gaussian distribution functions can be used to represent $P(D_i|x_i,x_T)$ as well. The planning algorithm does not require the Gaussian distribution assumption and we use the Gaussian distribution only as an example. In this paper, we pay particular attention to the problem of tracking a moving target in urban and cluttered environments where occlusions due to buildings and other terrain are prevalent. We assume that an elevation map of the environment is available to the vehicles before the mission begins. To include the effect of occlusions, we also include the map as a dependence in the probability of detection where $P(D_i|x_i,x_T,m)$ is the probability that the target is detected by the ith vehicle given that the ith vehicle is at x_i, the target is at x_T, and the map is given by m. We then compute

$$P(D_i|x_i,x_T,m) = \eta \begin{cases} P(D_i|x_i,x_T) & \text{LOS is not occluded,} \\ 0 & \text{otherwise,} \end{cases}$$
$$(4)$$

where again, η is a normalization factor. Figure 3 shows an example probability of detection in an urban environment. In this example, the target location x_T is held constant at (0,0), while the vehicle location x_i is varied in one meter increments on both axes. As shown, when a building occludes the line of sight, the probability of detection is zero. Occlusions are detected by testing each line of sight vector for intersections with each building polygon in the map. Since we assume that the map is known, $P(D_i|x_i,x_T,m)$ can be precomputed for each pair of x_i and x_T and stored in memory.

Using the law of total probability, the probability that the target is detected when the ith vehicle is at x_i is

$$P(D_i|x_i) = \int P(D_i|x_i,x_T)P(x_T)dx_T. \quad (5)$$

We are interested in maximizing the probability of detection over the future time horizon $[t,t+T_L]$. Using the path parameterization discussed above, we have that the probability of detection at $\sigma \in [0,T_L]$ is given by

$$P(D_i|x_i(t,\sigma,\Theta_i)) = \quad (6)$$
$$\int P(D_i|x_i(t,\sigma,\Theta_i),x_T(t+\sigma))P(x_T(t+\sigma))dx_T(t+\sigma).$$

For optimizing the path parameterization Θ_i, we propose a return function, which measures the sum of probability of detection over the look-ahead window and is given by

$$J_i(\Theta_i) = \int_0^{T_L} P(D_i|x_i(t,\sigma,\Theta_i))d\sigma. \quad (7)$$

The myopic planning problem for a single vehicle is then to find Θ_i to maximize $J_i(\Theta_i)$. The optimum path parameters are then passed to the low level autopilot and followed for a time less than or equal to T_L.

For independent target tracking using a UAV, we parameterize the paths by roll angles since different roll angles generate different paths. Let $\Phi_i = [-\phi_{max},\phi_{max}]$ represent the set of roll angles, where $\pm\phi_{max}$ is the positive/negative maximal roll angle. To solve the optimization problem, we discretize Φ_i as a finite set of roll angles represented by $\Phi_{id} = \{\phi_1,\phi_2,\cdots,\phi_m\}$, where $\phi_1 = -\phi_{max}$ and $\phi_m = \phi_{max}$ and we also discretize the look-ahead window $[0,T_L]$ as $T_d = \{0,\Delta\sigma,\cdots,n\Delta\sigma\}$, $\Delta\sigma = T_L/n$, which is the n-step look-ahead horizon. Let $\Theta_i^a \in \Phi_{id}$ represent the path parameterization over the n-step look-ahead horizon. For the n-step look-ahead planning horizon, the cost function given by Eq. (7) becomes

$$J_i(\Theta_i^a) = \sum_{j=0}^n P(D_i|x_i(t,j\Delta\sigma,\Theta_i^a)). \quad (8)$$

To maximize the return function given by Eq. (8), we recursively search a tree representing a set of potential paths over the n-step look-ahead horizon. Each node in the tree represents the UAV configuration at a certain stage and it has multiple children, each of which represents the resulting configuration at the next stage corresponding to a certain roll angle.

The path planning algorithm for target tracking using a single UAV can be described as follows. When the UAV is at the configuration $x_i(t,0,\Theta_i^a)$ at time t, the algorithm has already determined an optimal path $\tau_i(t) = \{x_i(t,0,\Theta_i^a),x_i(t,\Delta\sigma,\Theta_i^a),\cdots,x_i(t,n\Delta\sigma,\Theta_i^a)\}$. The UAV is maneuvered towards $x_i(t,\Delta\sigma,\Theta_i^a)$. During that period, the algorithm first takes $x_i(t,\Delta\sigma,\Theta_i^a)$ as the tree root and the tree is pruned by only maintaining the branches with the root at $x_i(t,\Delta\sigma,\Theta_i^a)$. The tree is then extended by one stage and the new tree is searched to find a new path $\tau_i(t+\Delta\sigma)$. Once the UAV reaches $x_i(t,\Delta\sigma,\Theta_i^a)$, the new path $\tau_i(t+\Delta\sigma)$ has been generated. We repeat this process recursively so that
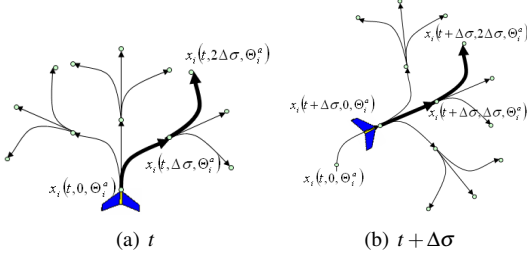
(a) t (b) $t + \Delta\sigma$

Fig. 4. A two-step look-ahead path planning tree for the UAV, where $T_d = \{0, \Delta\sigma, 2\Delta\sigma\}$ and $\Phi_{id} = \{\phi_1, \phi_2, \phi_3\}$.

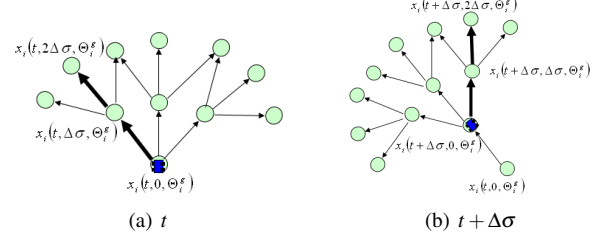(a) t (b) $t + \Delta\sigma$

Fig. 5. A two-step look-ahead path planning tree for the UGV.

found.

IV. PATH PLANNING FOR MULTIPLE VEHICLE COLLABORATION

The approach described in the previous section can easily be extended to multiple vehicles. Let I be an index set of vehicles and let $\mathbf{x}_I$ be the combined state of all vehicles whose index is in I. Let D_I represent the event that at least one vehicle in I can detect the target. The probability that at least one of vehicles detects the target given $\mathbf{x}_I$ and the target location x_T is denoted by $P(D_I|\mathbf{x}_I, x_T)$. It can be shown using standard probabilistic reasoning, that if the measurements made by each vehicle are independent, then

$$P(D_I|\mathbf{x}_I, x_T) = 1 - \prod_{i \in I} \left(1 - P(D_i|x_i, x_T)\right). \quad (10)$$

This formula is significant, because it shows that the joint probability of detection can be computed by combining the probability of detection for each vehicle. The probability that at least one of vehicles detects the target given $\mathbf{x}_I$ is denoted by

$$P(D_I|x_I) = \int P(D_I|x_I, x_T) P(x_T) dx_T. \quad (11)$$

Let Θ_I be the combined path parameters for all vehicles in the index set I. We can define the optimization criteria similar to Eq. (7) that are over the index set I, where

$$J(\Theta_I) = \int_0^{T_L} P(D_I|\mathbf{x}_I(t, \sigma, \Theta_I)) d\sigma. \quad (12)$$

The joint team optimization problem is to let I include all UAVs and UGVs on the team, and to maximize the return function $J(\Theta_I)$ at each planning instant. Unfortunately, this problem is NP-complete and so the computational time will grow exponentially in the number of UAVs and UGVs. In addition, solving the full joint optimization problem requires a centralized implementation. To mitigate these problems, we propose using a decentralized suboptimal approach that relies on an auction algorithm. To best describe our approach, we need some additional notation. Let I and K represent two index sets where $I \bigcap K = \emptyset$, and let $J(\Theta_I|\Theta_K)$ represent the return function defined by Eq. (12) but where the path parameters for the vehicles in I are free to change and the path parameters for the vehicles in K are fixed.

Consider that there are N vehicles in the groups. The decentralized algorithm that we use consists of N steps. Let

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the UAV is always maneuvered to configurations where the probability of detection is high.

Figure 4 shows a two-step look-ahead planning horizon tree, where $T_d = \{0, \Delta\sigma, 2\Delta\sigma\}$ and $\Phi_{id} = \{\phi_1, \phi_2, \phi_3\}$. When the UAV is at the configuration $x_i(t, 0, \Theta_i^a)$ at time t and the path $\tau_i(t) = \{x_i(t, 0, \Theta_i^a), x_i(t, \Delta\sigma, \Theta_i^a), x_i(t, 2\Delta\sigma, \Theta_i^a)\}$ has been found, as shown in Fig. 4(a). In Fig. 4(b), the UAV is maneuvered to $x_i(t, \Delta\sigma, \Theta_i^a)$ and the branches whose root is not at $x_i(t, \Delta\sigma, \Theta_i^a)$ are removed. The tree is then extended by one step horizon and the new tree is searched to find a new path $\tau_i(t + \Delta\sigma) = \{x_i(t + \Delta\sigma, 0, \Theta_i^a), x_i(t + \Delta\sigma, \Delta\sigma, \Theta_i^a), x_i(t + \Delta\sigma, 2\Delta\sigma, \Theta_i^a)\}$. Once the UAV reaches $x_i(t, \Delta\sigma, \Theta_i^a)$, the new path $\tau_i(t + \Delta\sigma)$ has been found. Given a tree, searching the tree and finding a path can be solved efficiently using dynamic programming [10].

For independent target tracking using a single UGV, we decompose the roads into cells and construct a graph using those cells since the UGV can only move along the roads. Similarly, we discretize the look-ahead window $[0, T_L]$ as the n-step look-ahead horizon $T_d = \{0, \Delta\sigma, \cdots, n\Delta\sigma\}$, where $\Delta\sigma = T_L/n$. For each stage, the paths to the next stage are parameterized by the waypoints, denoted by Θ_i^g, which are the centers of the neighboring cells. The cost function to be maximized for target tracking using a single UGV is given by

$$J_i(\Theta_i^g) = \sum_{j=0}^{n} P(D_i|x_i(t, j\Delta\sigma, \Theta_i^g)). \quad (9)$$

Similarly, the n-step look-ahead planning horizon tree is constructed. The connectivity of the graph determines the extension of the tree. Figure 5 shows a two-step look-ahead planning horizon tree, where the circles represent the nodes and the tree is extended based on the connectivity of the graph. At time t, the UGV is at the configuration $x_i(t, 0, \Theta_i^g)$ and the path $\tau_i(t) = \{x_i(t, 0, \Theta_i^g), x_i(t, \Delta\sigma, \Theta_i^g), x_i(t, 2\Delta\sigma, \Theta_i^g)\}$ has been found as shown in Fig. 5(a). The UGV is maneuvered to $x_i(t, \Delta\sigma, \Theta_i^g)$ and the branches whose root is not at $x_i(t, \Delta\sigma, \Theta_i^g)$ are removed, as shown in Fig. 5(b). The tree is then extended by one stage and the new tree is searched to find a new path $\tau_i(t + \Delta\sigma)$ using dynamic programming. Once the UGV reaches $x_i(t, \Delta\sigma, \Theta_i^g)$, the new path $\tau_i(t + \Delta\sigma) = \{x_i(t + \Delta\sigma, 0, \Theta_i^g), x_i(t + \Delta\sigma, \Delta\sigma, \Theta_i^g), x_i(t + \Delta\sigma, 2\Delta\sigma, \Theta_i^g)\}$ has been

Θ_i^j represent the path parameterization for the ith vehicle at the jth step of the algorithm. The first step of the algorithm is for each vehicle to maximize $J(\Theta_i^1)$, $i = 1, \cdots, N$, and to send the optimal myopic return to the other vehicles in the network. If k_1 is the index of the vehicle such that $k_1 = \text{argmax}(J(\Theta_i^1))$, then the path of the $(k_1)^{th}$ vehicle over the look-ahead window $[0, T_L]$ is parameterized by $\Theta_{k_1}^1$, and each vehicle assigns $K = k_1$. At the second step, the remaining vehicles maximize $J(\Theta_i^2 | \Theta_K)$, $i = 1, \cdots, k_1 - 1, k_1 + 1, \cdots, N$ and send the resulting optimal value to the group. If k_2 is the index of the vehicle such that $k_2 = \text{argmax}(J(\Theta_i^2 | \Theta_K))$, then the path of the $(k_2)^{th}$ vehicle is parameterized by $\Theta_{k_2}^2$. The $(k_2)^{th}$ vehicle is added to K such that $K = \{k_1, k_2\}$. The process repeats until all vehicles $\{k_1, k_2, \cdots, k_N\}$ have been assigned path parameters $\{\Theta_{k_1}^1, \Theta_{k_2}^2, \cdots, \Theta_{k_N}^N\}$. For the N vehicles, $N - 1$ auctions will be required. Let $|\Theta_i|$ represent the cardinality of the set Θ_i. The advantage of this approach is that rather than optimizing over $|\Theta_i|^N$, the process requires N optimizations over Θ_i parameters, resulting in linear computational growth.

V. Simulation

The algorithm was tested using a simulation environment developed in MATLAB/SIMULINK, as shown in Fig. 6, where green blocks represent the buildings. A single UAV and UGV were used to track a target cooperatively. A 49×49 occupancy grid, where the size of each cell is $5m \times 5m$, was used to model the target state. The simulator uses six state navigation equations for the aircraft and uses four state navigation equations for the ground vehicle. Three-step look-ahead horizon paths were planned for the UAV and the UGV with the sample interval $\sigma = 2s$. The set of roll angles for the UAV was $\{-30°, -15°, 0°, 15°, 30°\}$. The camera mounted on the UAV was assumed to be gimballed so that it was always pointed down and the field of view of it was $40°$. An omnidirectional camera was used for the UGV and the area it can observe was a square of $30m \times 30m$. The covariance of the detection probability was $\Sigma = 20$. The parameter P_c was set at 0.9. In the simulation, the UAV flew at an altitude of $120m$. The target is initially placed at North-East coordinate (75m, 75m) and it will move among the waypoints (75m, 75m), (75m, -75m), (-75m, -75m) and (-75m, 75m) in turn. The motion model of the target is not known by the UAV and the UGV.

Figure 6 shows the snapshots of the target occupancy grid and the paths for the UAV and the UGV for cooperatively tracking the target at different time steps. There exist 36 buildings in the environment, each of which is $40m$ high. The algorithm assumes the target is initially located at the origin. It then updates the target occupancy grid using Bayesian filtering and plans the corresponding paths such that the joint cost function is maximized. By doing so, the UAV and the UGV can eventually detect the target at time $t = 40s$, as shown in Fig. 6(c). Figure 7 shows the trajectories of
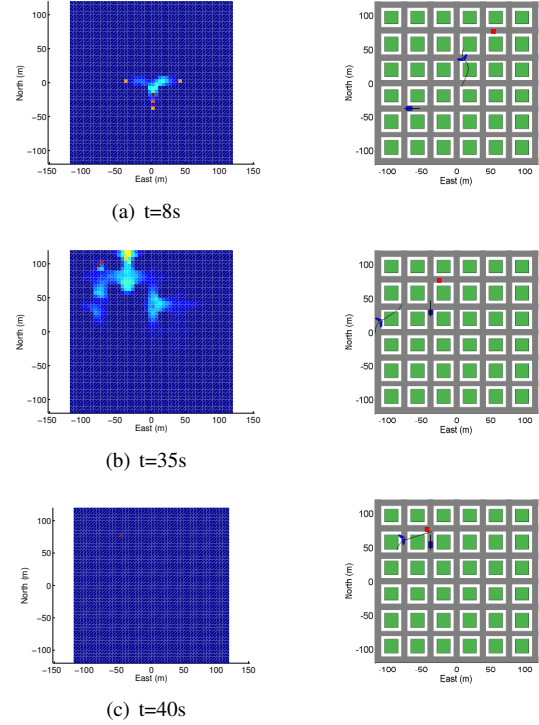

(a) t=8s

(b) t=35s

(c) t=40s

Fig. 6. The snapshots of target occupancy grid and the paths of the UAV and the UGV.

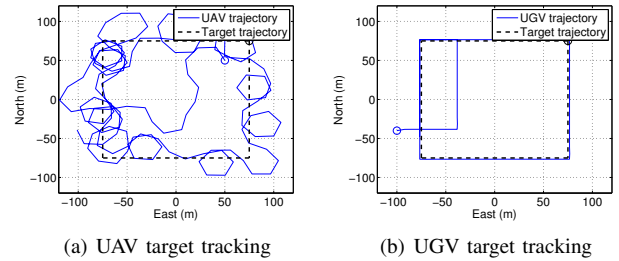(a) UAV target tracking   (b) UGV target tracking

Fig. 7. The trajectories of the target, the UAV and the UGV.

the target, the UAV and the UGV. Figure 8 shows the cost associated with the UAV, the UGV and their cooperation. Based on the figure, the cost associated with the UAV shows more oscillations than the cost associated with the UGV. This is due to the fact that the UAV must always fly along its orbits and cannot stop. The algorithm takes around $40s$ to detect the target, as shown in the green area. The UAV and the UGV then start to track the target. The straight horizontal lines in the figure show the mean of the cost associated with the UAV, the UGV and their cooperation before and after the first detection.

To show the statistical performance of the algorithm, we implemented the algorithm in the environments with different building height and density. For each environment, we executed 100 simulation runs. Each simulation run lasted $300s$ and different initial positions of the UAV and the UGV were chosen based on a uniform distribution. We evaluated
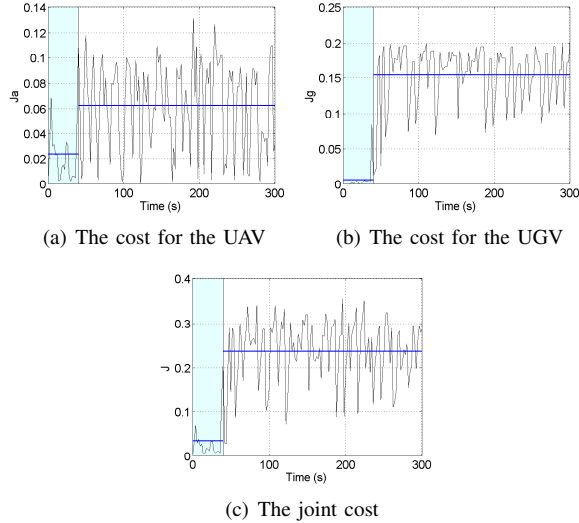
(a) The cost for the UAV   (b) The cost for the UGV

(c) The joint cost

Fig. 8.   The cost associated with the UAV, the UGV and their cooperation.

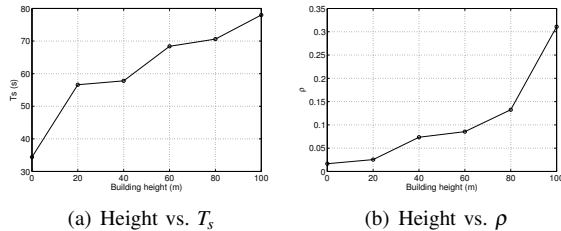(a) Height vs. T_s (b) Height vs. ρ

Fig. 9.   The change of T_s and ρ versus the building height.

two criteria: (a) the search time for the first detection denoted by T_s, and (b) the time percentage of target loss by both the UAV and the UGV (out of the field of view of both cameras or occluded by buildings) denoted by ρ. Figure 9 shows the change of average values of T_s and ρ over 100 simulations versus the height of the buildings for the environment where 36 buildings exist. Figure 10 shows the change of average values of T_s and ρ versus the density of the environment where the building height is 100m. In the simulation, we consider the environment where at most 36 buildings exist. The density of the environment is assumed to be the ratio of the number of existing buildings over 36. From the two figures, T_s and ρ increase as the height of the buildings and the density of the environment increase. This is because that more occlusions will be generated as the height and the density increase.

VI. CONCLUSIONS

We have presented a path planning algorithm for tracking a moving target in urban environments using both UAVs and UGVs. The algorithm takes into account occlusions between the sensors and the target. We use the dynamic occupancy grid to model the target state and use Bayesian filtering to update the probability of the target location. For target tracking by a single obstacle, we design the path planning algorithm to generate paths maximizing the sum
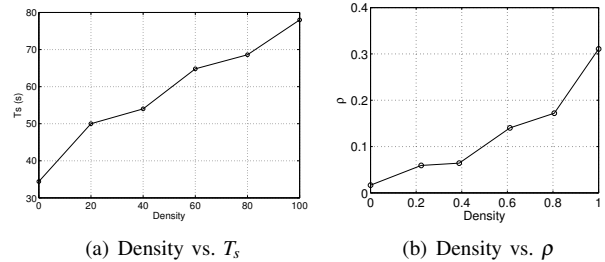

(a) Density vs. T_s (b) Density vs. ρ

Fig. 10.   The change of T_s and ρ versus the density of the environment.

of probability of detection over a finite look-ahead horizon. For target tracking using multiple vehicles, we designed the decentralized path planning algorithm relying on an auction algorithm to generate paths maximizing the sum of the joint probability of detection over the finite horizon.

In this work, we assume that the terrain map is accurately known and not changing in time. In the future, we will design schemes for tracking targets in unknown environments. We will also use higher order Markov chains to represent the target motion. Flight experiments will also be conducted to validate the planning algorithm.

VII. ACKNOWLEDGEMENT

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