## TKP4140 Process control — Midterm Exam

12. October 2017

Student number:

- Write your student number on **every** page in the indicated space.
- Write your student answers on the enclosed pages.
- Use the last two pages for details if you have too little space.
- Do not separate the enclosed pages.

1. (30 points) Consider a tank with one inflow and one outflow, as given in Figure 1. Assume constant density,  $\rho = const$ .

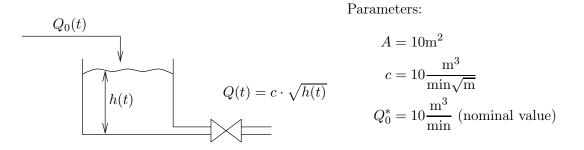


Figure 1: Tank system with volume V = Ah

(a) Formulate the dynamic mass balance and write it in the form  $\frac{dh}{dt} = \dots$ 

(b) What are the steady state values of h(t) and Q(t)?

(c) Linearize the model and introduce deviation variables.

(d) Take the Laplace transform and derive the transfer function g(s):

$$h(s) = g(s)Q_0(s)$$

(e) What is the value of the steady state gain and the time constant in g(s)?

(f) Fill in the corresponding transfer functions in the block diagram from Figure 2.

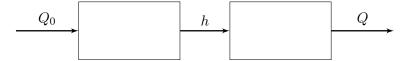


Figure 2: Block Diagram Tank System

(g) Does the block diagram from Figure 2 correspond to an open loop or a closed loop system?

2. (10 points) Given the first-order transfer function

$$g(s) = \frac{2e^{-7s}}{5s+1} \tag{1}$$

and y(s) = g(s)u(s).

Consider a step change in the input:

$$u(t) = \begin{cases} 0 & \text{for } t < 3\\ 5 & \text{for } t \ge 3 \end{cases}$$
(2)

Use the template in Fig.3 to sketch u(t) and the resulting y(t). Indicate the time constant, delay, and steady state value in your sketch.

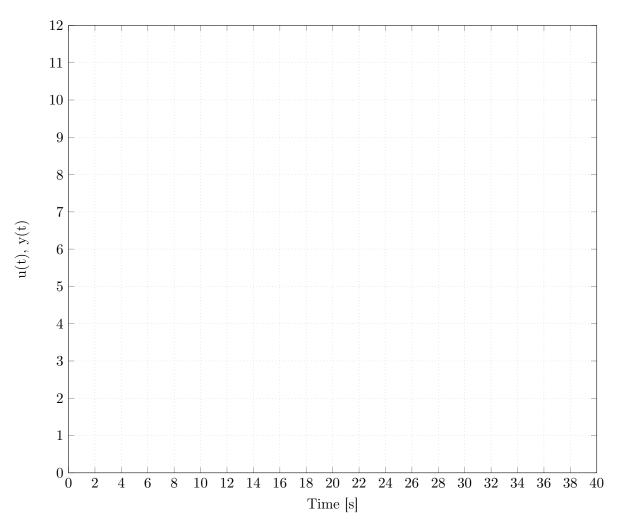


Figure 3: Step Response

3. (20 points) Consider the system in Figure 4.

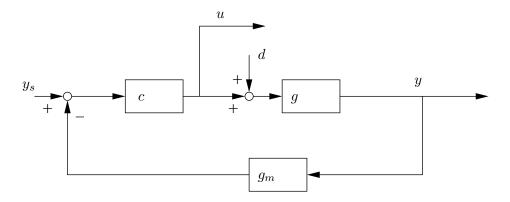


Figure 4: Block diagram

(a) Find the closed loop transfer function T(s) from  $y_s(s)$  to y(s). Use symbols  $(c(s), g(s), g_m(s))$ .

(b) Find the closed loop transfer function Q(s) from  $y_s(s)$  to u(s). Use symbols  $(c(s), g(s), g_m(s))$ .

(c) Find T(s) when: 
$$g(s) = \frac{3}{5s+1}$$
  $g_m(s) = \frac{-s+1}{s+1}$   $c(s) = 1$ 

- (d) What is the steady state gain when there is a unit step in  $y_s$ ?
- (e) Calculate the damping factor and the time constant of T(s). Hint: the denominator in the second order transfer function is  $\tau^2 s^2 + 2\tau \zeta s + 1$ .
- (f) Does the system oscillate?

Midterm Exam TKP4140

Student number: .

4. (20 points) Given

$$g_{1} = \frac{2.5}{(6s+1)}$$

$$g_{2} = \frac{2.5(s+0.8)}{(6s+1)^{2}}$$

$$g_{3} = \frac{2.5}{(9s^{2}+3s+1)}$$

$$g_{4} = \frac{2(-4s+1)}{(6s+1)^{2}}$$

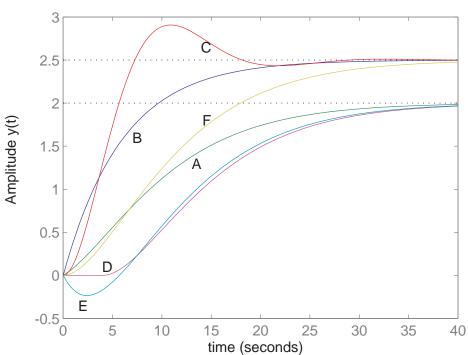
$$g_{5} = \frac{2e^{-4s}}{(6s+1)^{2}}$$

$$g_{6} = \frac{2.5}{(6s+1)^{2}}$$

Fill in the missing values in Table 1. In the case that the results in the table do not give a unique answer, comment on your choice.

## Hints:

Initial slope of response to unit step input:  $\lim_{t\to 0} y'(t) = \lim_{s\to\infty} sg(s)$ 



Step response y(t) for u(t)=1

Figure 5: Step responses

Student number:

TF	Poles	Zeros	SS gain	Initial gain	Initial slope	Conclusion
$g_1$						
$g_2$						
$g_3$						
$g_4$						
$g_5$						
$g_6$						

Table 1: Problem 4; SS: steady state; TF: transfer function

Student number: \_\_\_\_

- 5. (20 points) (a) SIMC tuning rules.
  - i. Write the SIMC PI tuning rules for a first-order plus delay process. g(s) =

ii. Write the SIMC tuning rules for cascade PID for a second-order plus delay process.

$$g(s) =$$
 $K_c = au_I = au_D =$ 

(b) By modelling and linearization, you have derived the following process transfer function

$$g(s) = \frac{3(-1.5s+1)e^{-0.5s}}{(25s+1)(3s+1)(0.8s+1)}$$
(3)

- i. Write the first-order plus delay approximation  $g_1(s)$  using the half rule.
- ii. Write the second-order plus delay approximation  $g_2(s)$  using the half rule.
- iii. Based on the approximations of  $g_1(s)$  and  $g_2(s)$  give the SIMC PI and PID settings. Use the standard choice  $\tau_c = \theta$ , where  $\theta$  is the effective delay.
- iv. Would you recommend a PI or a PID controller? Explain briefly.
- (c) What would the SIMC PI tunings be for the system in Problem 3 (given Figure 4 with the transfer function from 3(c))?

## Extra space if needed

Please indicate clearly which problem the solution belongs to.

## Extra space if needed

Please indicate clearly which problem the solution belongs to.