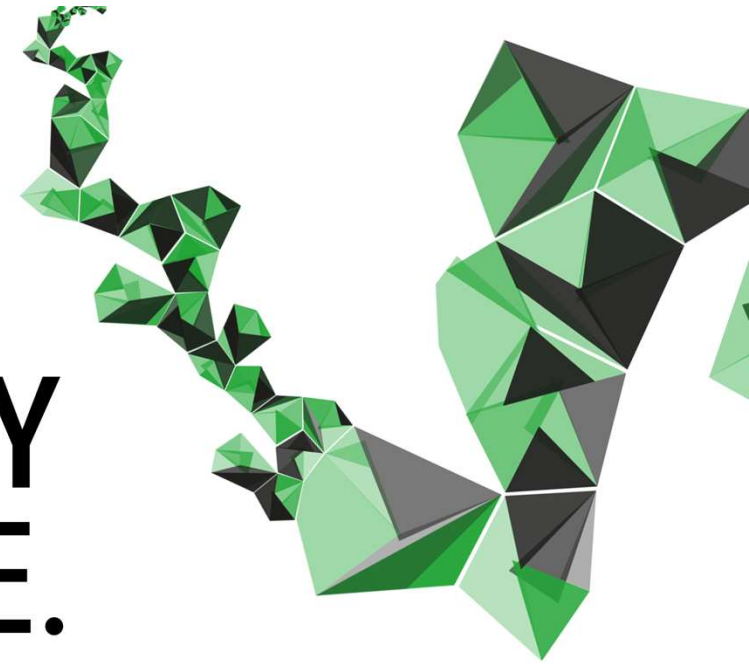


**UNIVERSITY
OF TWENTE.**



**DESIGN OF AZEOTROPIC AND EXTRACTIVE
DIVIDING-WALL COLUMNS BY MINLP METHODS**

WORKSHOP ON DIVIDED-WALL DISTILLATION IN TRONDHEIM, OCTOBER 5, 2023

IN THIS PRESENTATION:



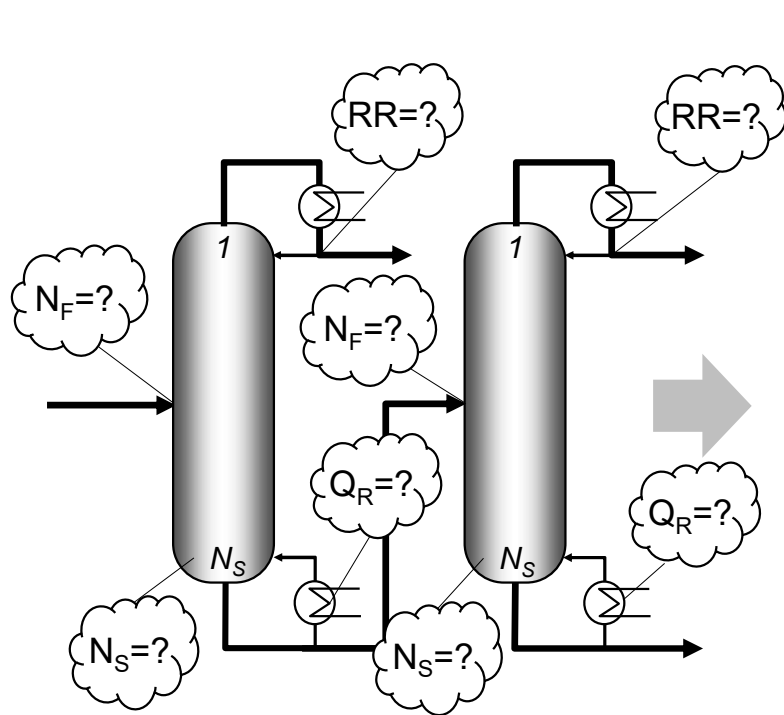
MINLP OPTIMIZATION OF
DWC COLUMNS

THERMODYNAMIC
EFFICIENCY

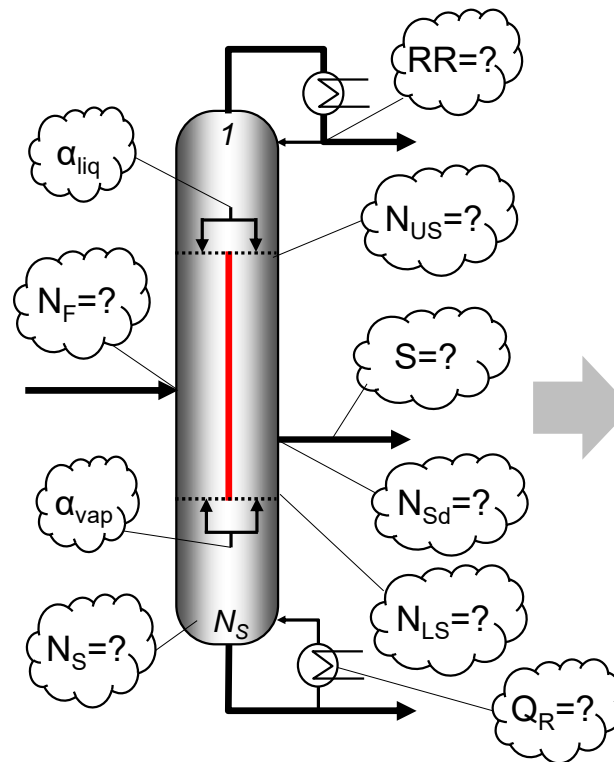
EXTRACTIVE DIVIDING-
WALL COLUMNS

AZEOTROPIC DIVIDING-
WALL COLUMNS

For a DWC, many degrees of freedom must be fixed...



of Operational DOF: 4
of Design DOF: 4



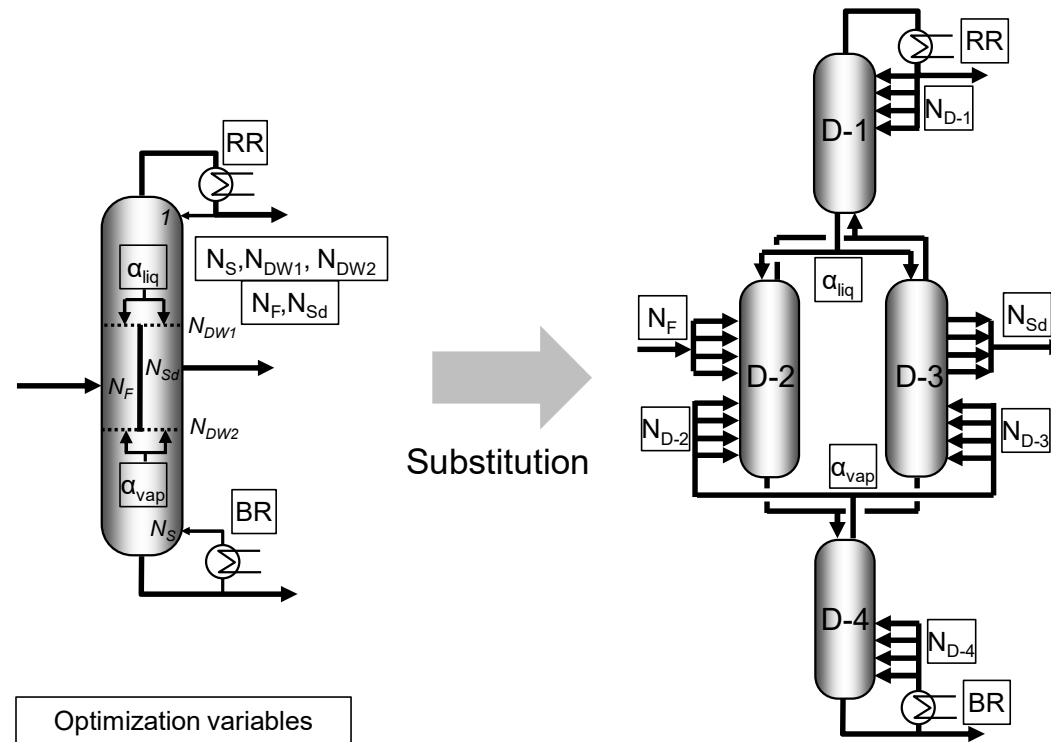
of Operational DOF: 5
of Design DOF: 5



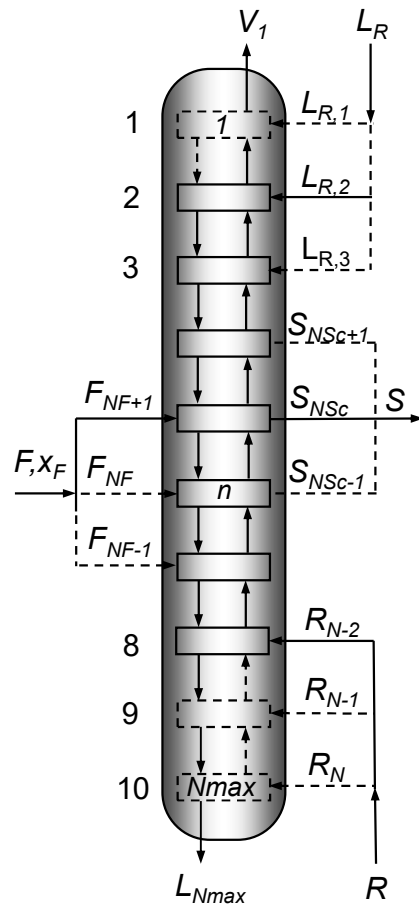
[Bayer MaterialScience: Neue TDI-Anlage in Dormagen eröffnet \(plasticker.de\)](https://www.plasticker.de)

... a suitable model structure must be chosen ...

- Thermodynamic equivalent representation of DWC by 4-section column model



... the model equations must be written ...



- MESH equations for $n = 1 \dots N_{max}$ stages:

$$V_{n+1}x_{Vn+1} + L_{n-1}x_{Ln-1} + F_n x_{Fn} + L_{Rn} x_{LRn} + R_n x_{Rn} = V_n x_{Vn} + L_n x_{Ln} + S_n x_{Sn}$$

$$x_{Vn} = K_n x_{Ln}$$

$$\sum x_{Vn} = 1 \quad \text{and} \quad \sum x_{Ln} = 1$$

$$V_{n+1}h_{Vn+1} + L_{n-1}h_{Ln-1} + F_n h_{Fn} + L_{Rn} h_{LRn} + R_n h_{Rn} = V_n h_{Vn} + L_n h_{Ln} + S_n h_{Sn}$$

- Mixed-integer and pure integer constraints:

$$F_n \leq F \cdot y_{F,n} \quad \text{and} \quad \sum y_{F,n} = 1$$

$$L_{R,n} \leq L_R \cdot y_{R,n} \quad \text{and} \quad \sum y_{LR,n} = 1$$

$$R_n \leq R \cdot y_{R,n} \quad \text{and} \quad \sum y_{R,n} = 1$$

$$S_n \leq S \cdot y_{S,n} \quad \text{and} \quad \sum y_{S,n} = 1$$

- Auxiliary model equations:

$$N_S = \sum y_{R,n} \cdot n - \sum y_{LR,n} \cdot n + 1 \quad + \text{ Pressure Drop Correlations}$$

... the optimization problem must be set up

- Constraints:
 - Equality constraints (model equations) \mathbf{h}
 - Inequality constraints (design specs) \mathbf{g}
 - Mixed-integer constraints $\mathbf{x} - \mathbf{M}\mathbf{y} \leq \mathbf{0}$
 - Pure integer constraints $\mathbf{y}\mathbf{E} = \mathbf{e}$
- Optimization variables:
 - Continuous variables \mathbf{d}
 - Binary (integer) variables \mathbf{y}
- Objective function $\mathbf{f}(\mathbf{x}, \mathbf{y})$:
 - $\mathbf{f}(\mathbf{x}, \mathbf{y}) = \text{Total Annual Costs (TAC)}$
 - $\mathbf{TAC} = C_{op} + 5 * C_{eqp} * 0.2$

$$Z = \min_{\mathbf{d}, \mathbf{y}} f(\mathbf{x}, \mathbf{y})$$

subject to

$$\mathbf{h}(\mathbf{x}, \mathbf{y}) = \mathbf{0}$$

$$\mathbf{g}(\mathbf{x}, \mathbf{y}) \leq \mathbf{0}$$

$$\mathbf{x} - \mathbf{M}\mathbf{y} \leq \mathbf{0}$$

$$\mathbf{y}\mathbf{E} = \mathbf{e}$$

$$\mathbf{x} \in R^{n_x}, \mathbf{y} \in \{0,1\}^{n_y}$$

Remark:

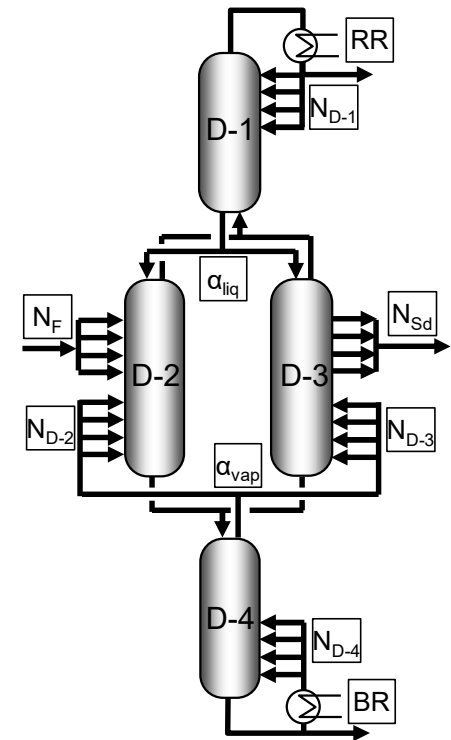
\mathbf{d} is the vector of optimization variables and a subset of all cont. \mathbf{x}

... with special attention to DWC equipment costs ...

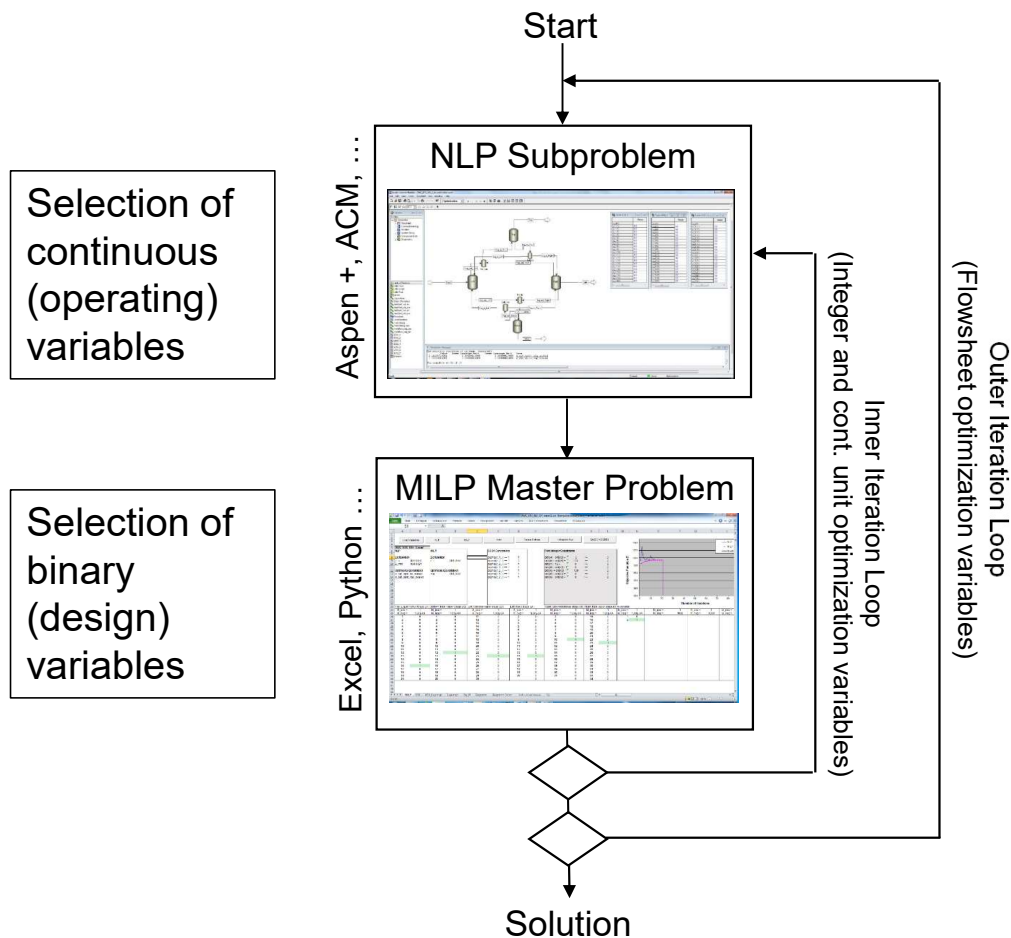
- Equipment costs of DWC consists of 4 pressure vessels with internals plus condenser and reboiler:

$$C_{eqp} = C_{eqp,D-1} + C_{eqp,D-2} + C_{eqp,D-3} + C_{eqp,D-4} + C_{eqp,Cond} + C_{eqp,Reb}$$

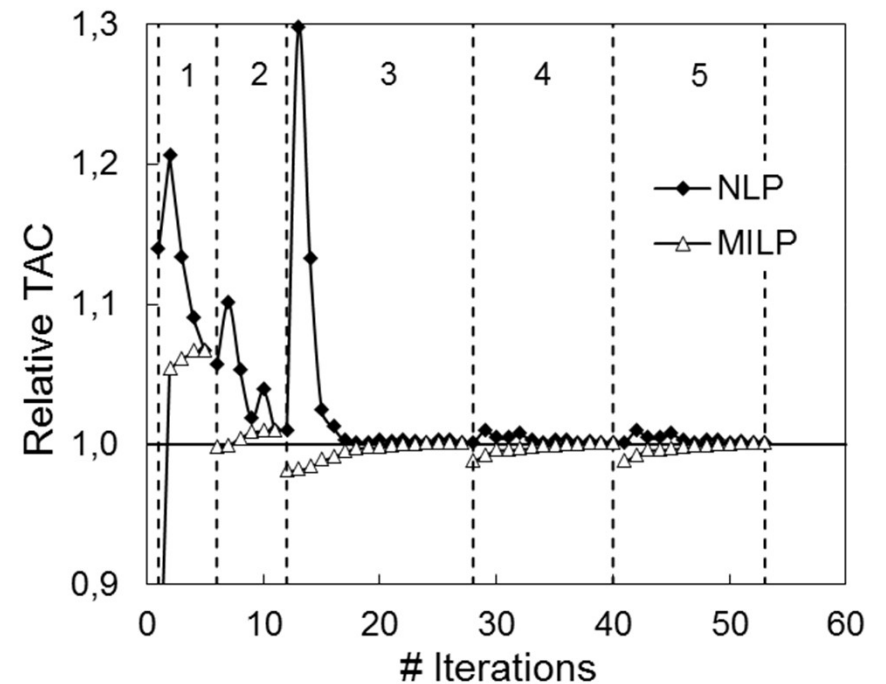
- Overestimation of DWC equipment costs, but consistent with model structure, easy to implement, and for comparative studies (probably) sufficient



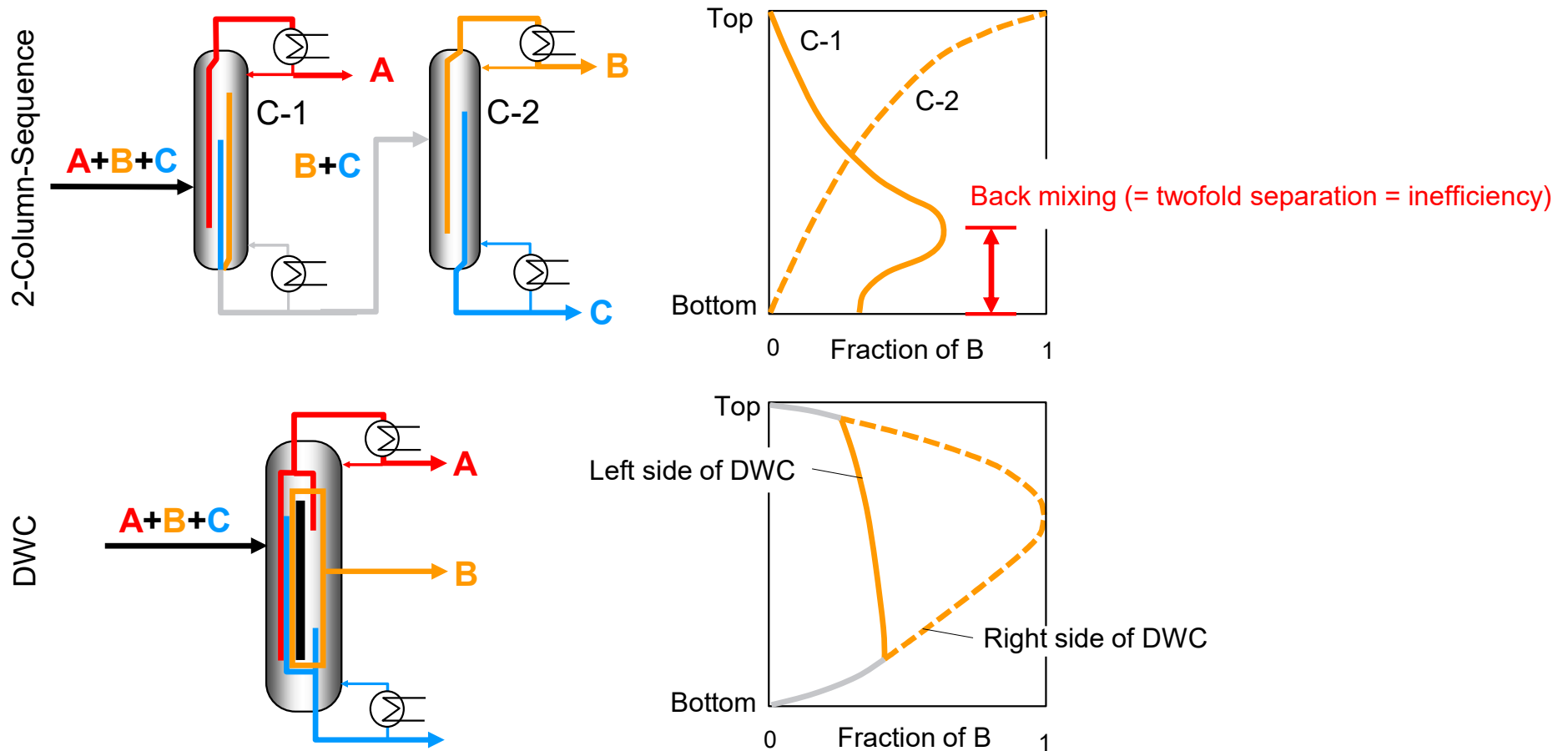
... and finally, the problem must be solved.



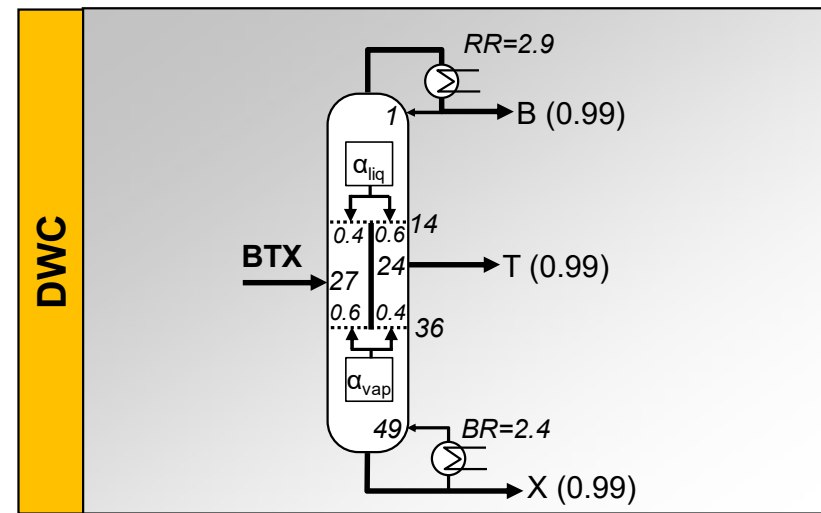
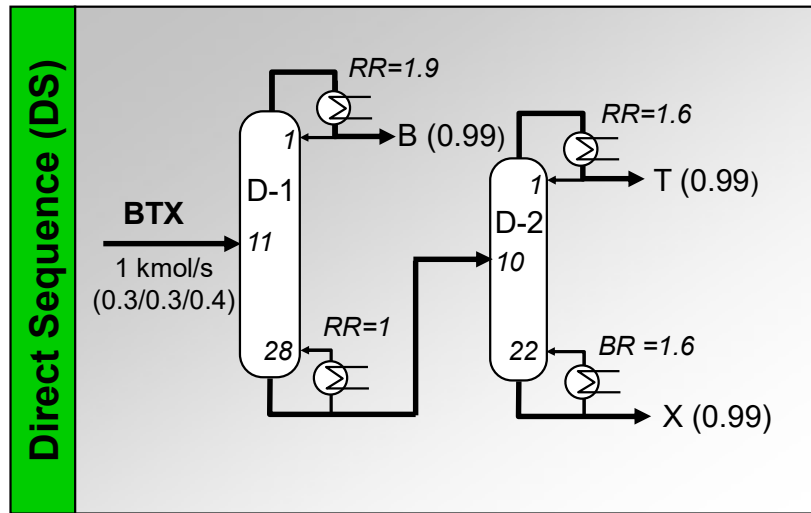
Franke. M.B. (2019), Comp. Chem. Eng.:
Modified Generalized Benders Decomposition (mGBD)



Thermodynamic Efficiency of DWC



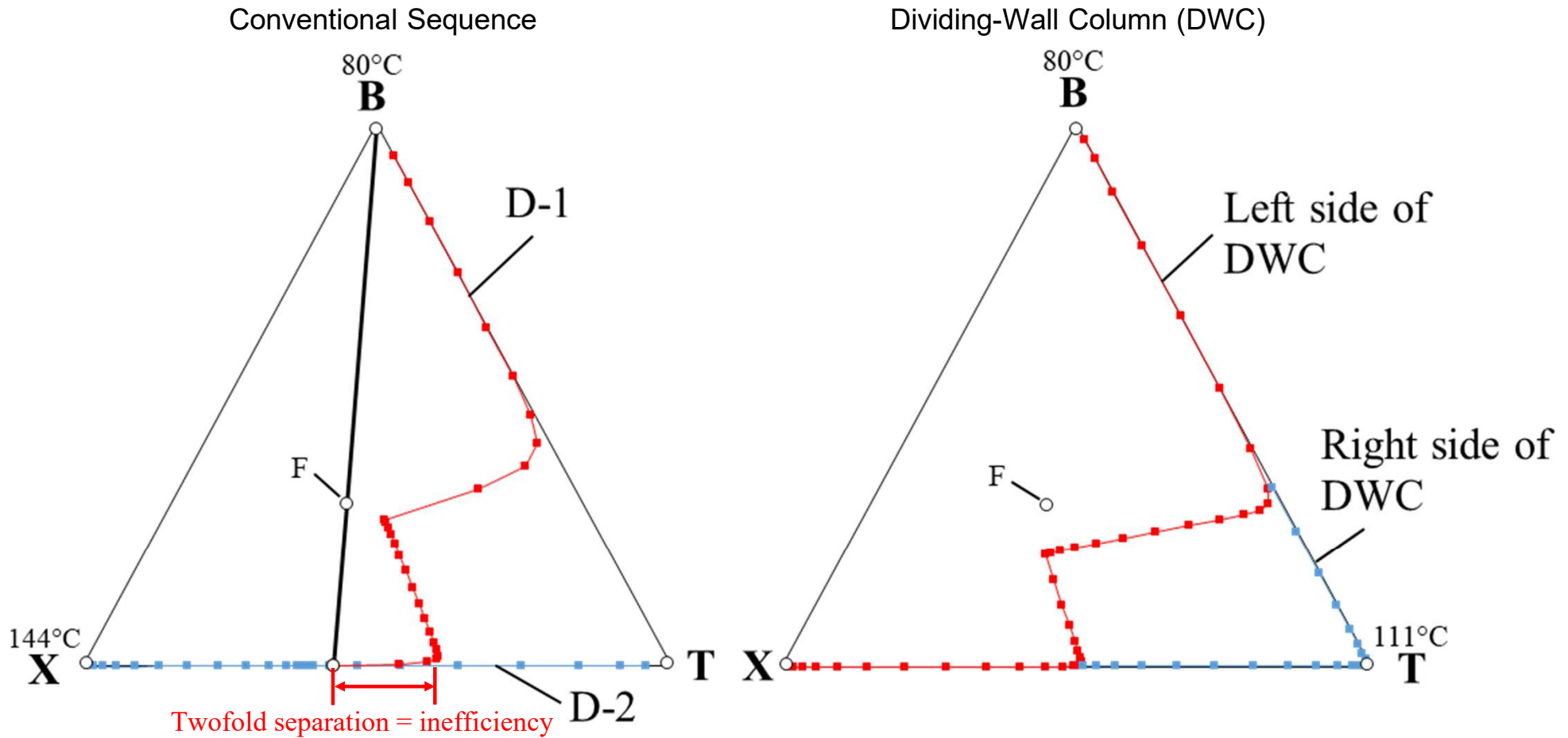
MINLP Results for a Very Prominent Example



	D-1	D-2	DS	DWC	Sav.
Q / MW	24.9	24.6	49.5	35.6	28%
No. of stages	28	22	50	49	2%
Rel. OpEx	0.37	0.36	0.73	0.53	27%
Rel. CapEx	0.13	0.14	0.27	0.22	19%
Rel. TAC	0.5	0.5	1	0.75	25%

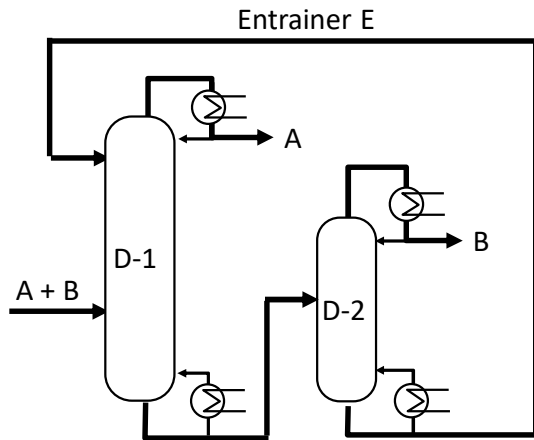
Ling, Luyben (2009), Ind. Eng. Chem. Res.
 Franke (2017), Chem. Ing. Techn.

Thermodynamic Efficiency of DWC

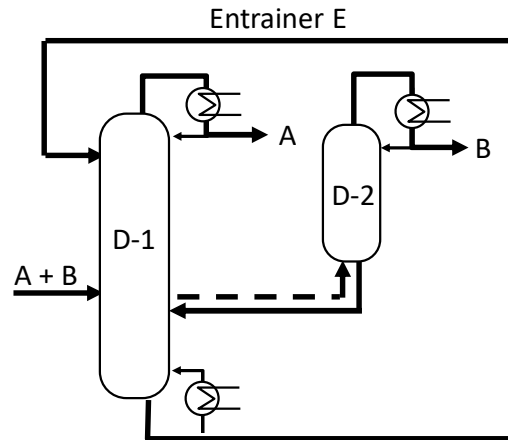


Derivation of Extractive Dividing-Wall Column

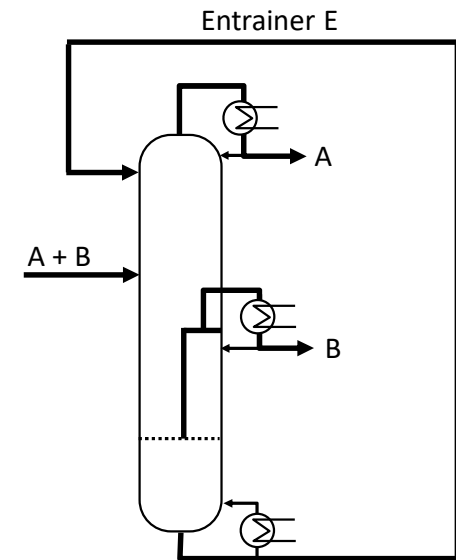
Extractive Distillation



**Extractive Distillation
w/ Side Rectifier**

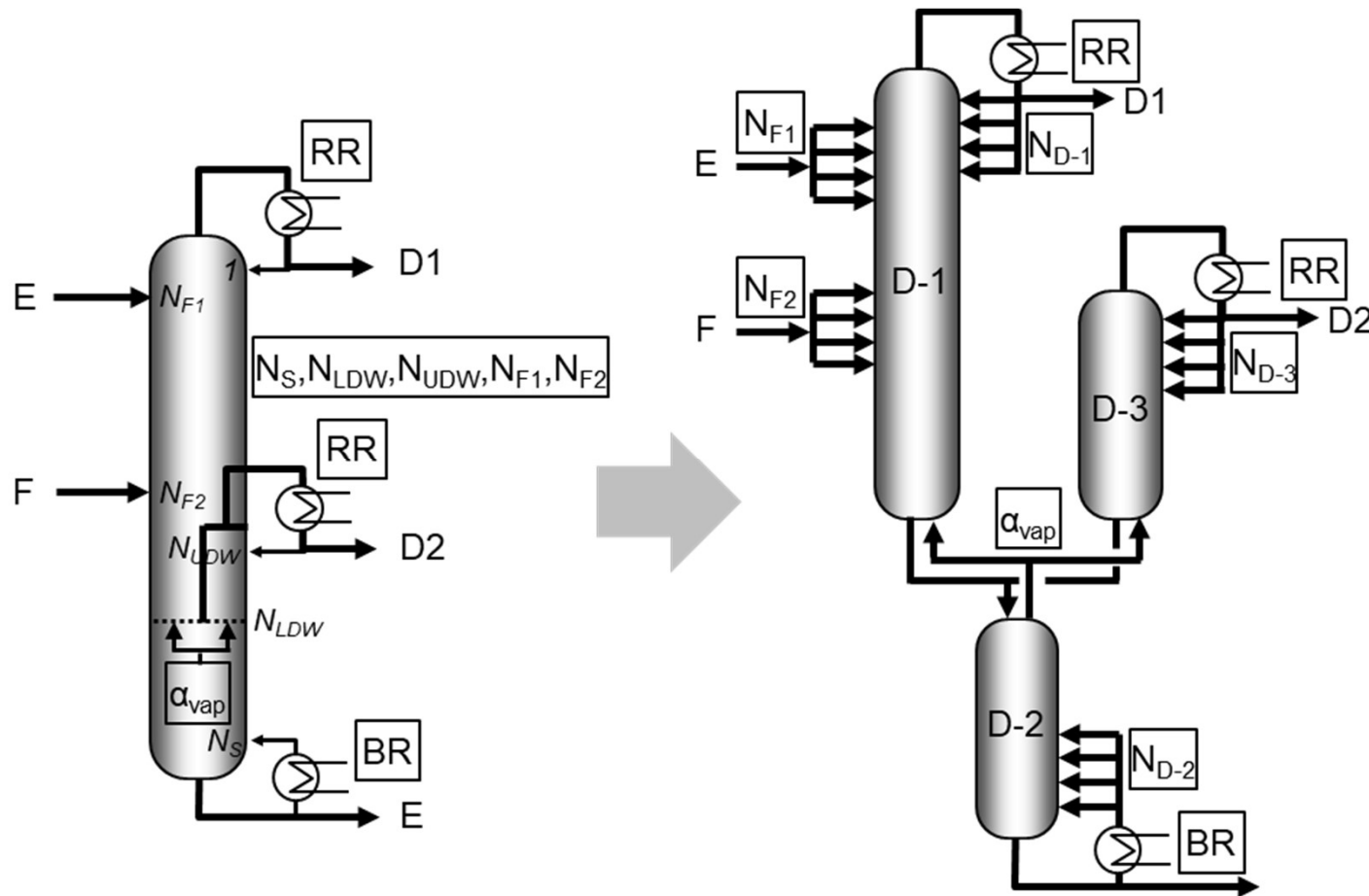


**Extractive Dividing-Wall
Column (Ledge Wall)**

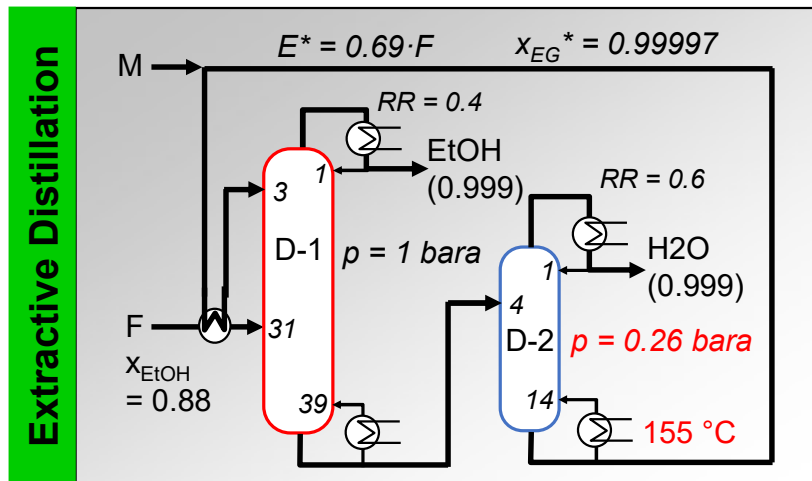


Kiss, Suszwala (2015): Enhanced bioethanol dehydration by extractive and azeotropic distillation in DWC
Czarnecki et al. (2023): Extractive Dividing Wall Column for Separating Azeotropic Systems: A Review

Extractive DWC: 3-Column Substitution Model

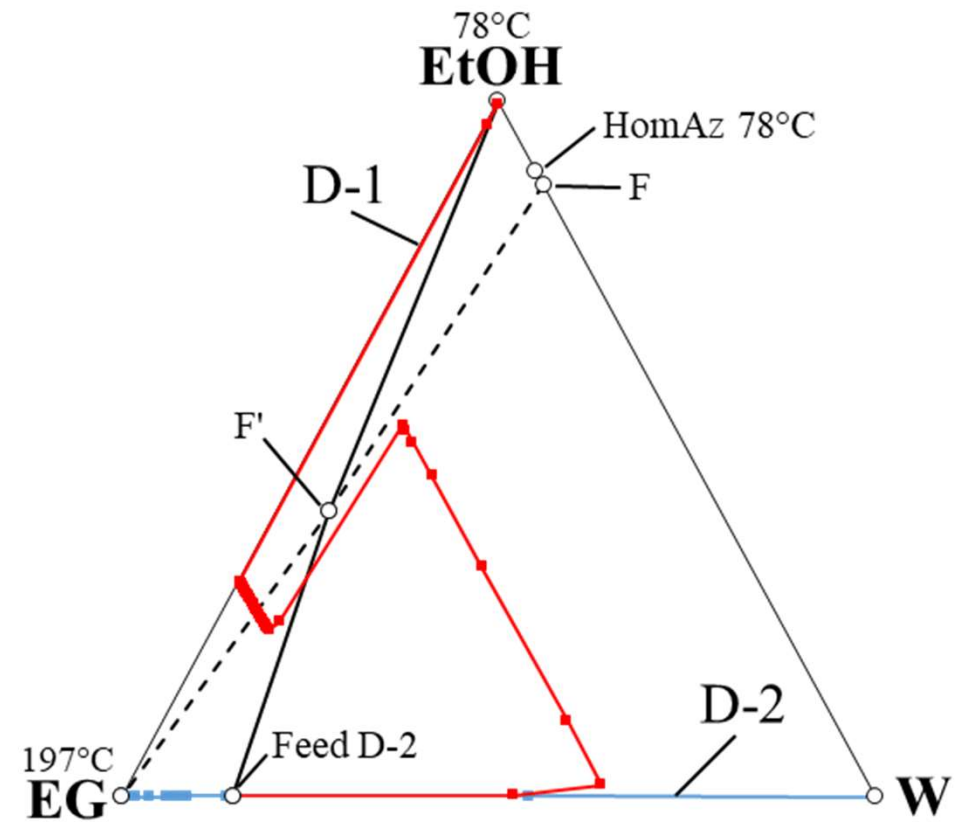


Extractive Distillation in a Dividing-Wall Column (EDWC)

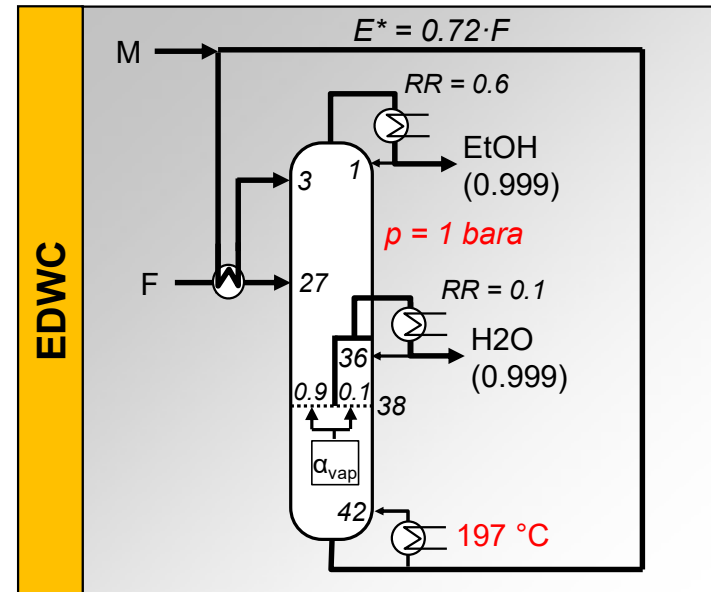
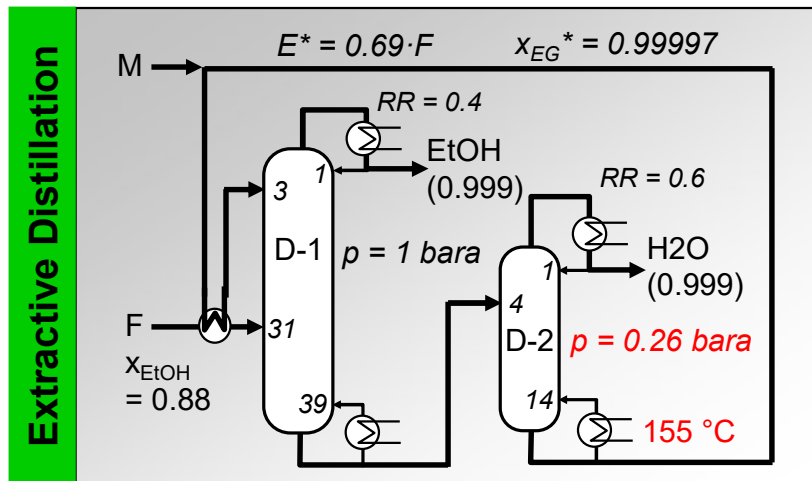


*Flowsheet optimization variables

	D-1	D-2	ED
Q / kJ/kg EtOH	1401	188	1589
No. of stages	39	14	53
Rel. OpEx	0.71	0.1	0.81
Rel. CapEx	0.16	0.03	0.19
Relative TAC	0.87	0.13	1

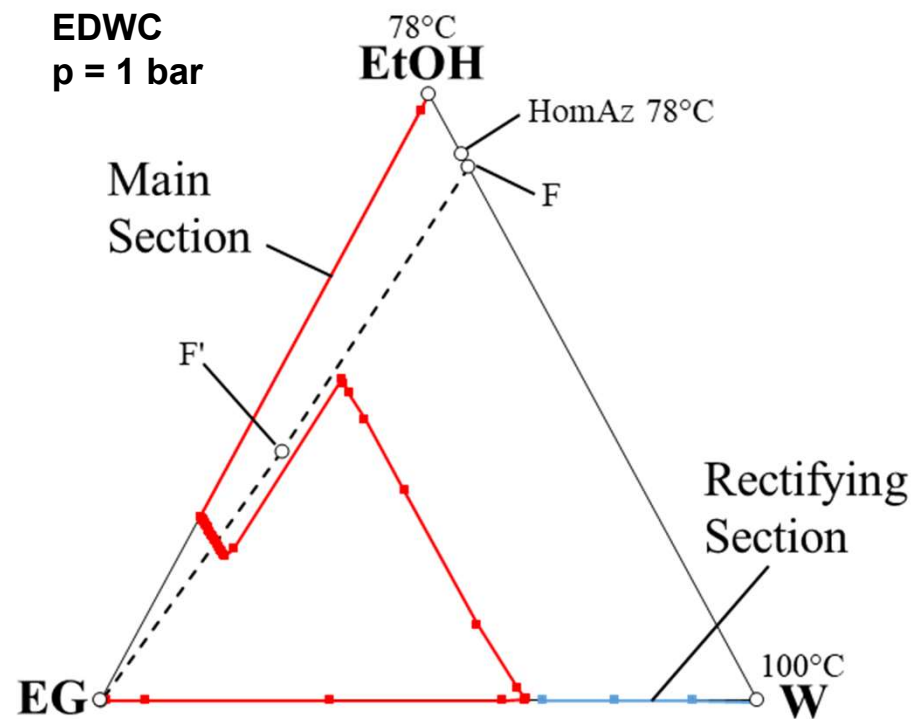
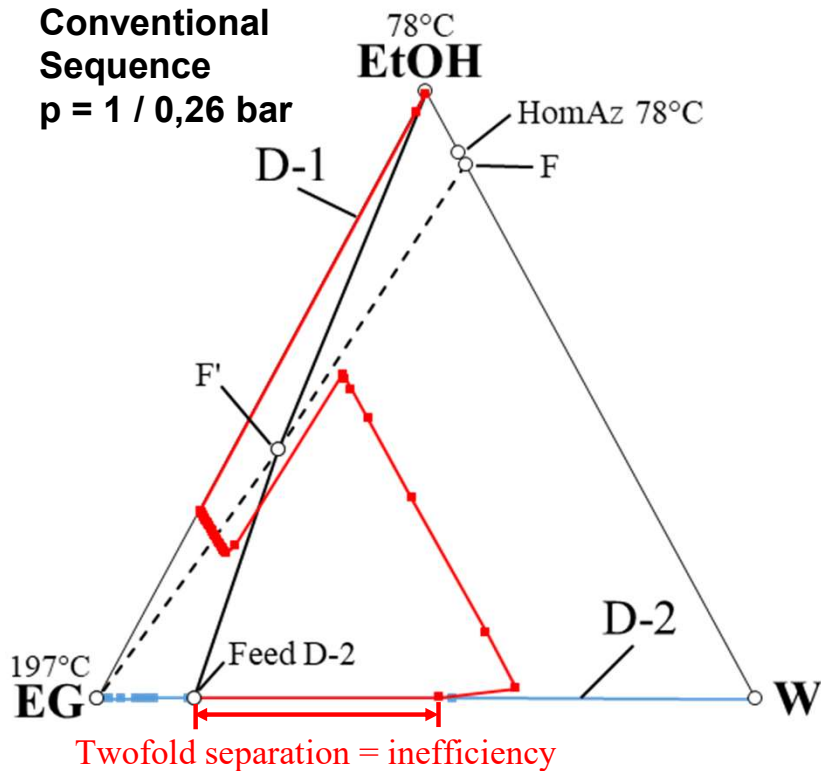


Extractive Distillation in a Dividing-Wall Column (EDWC)



	D-1	D-2	ED	EDWC	Sav.
Q / kJ/kg EtOH	1401	188	1589	1664	-5%
No. of stages	39	14	53	42	21%
Rel. OpEx	0.71	0.1	0.81	0.94	-16%
Rel. CapEx	0.16	0.03	0.19	0.2	-5%
Relative TAC	0.87	0.13	1	1.14	-14%

Thermodynamic Efficiency of EDWC



Although double separation is avoided, the extractive dividing-wall column is **not** a viable option for separating near-azeotropic ethanol/water mixtures because the pressures cannot be selected independently.

Alternative: Side-stream Column

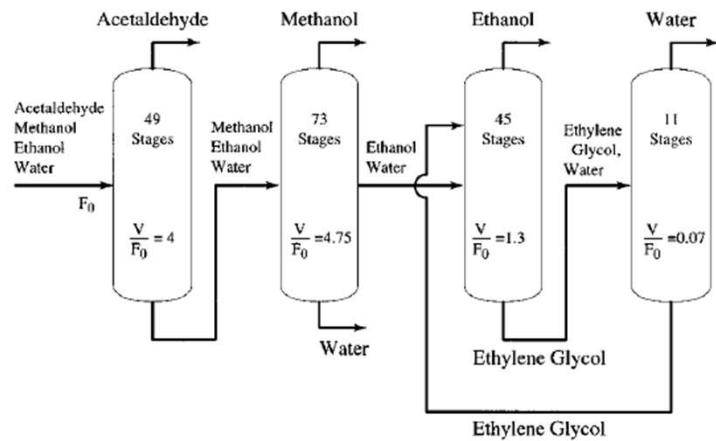


Figure 14. Second sequence to separate acetaldehyde, methanol, ethanol, and water. This sequence has a total of 4 columns, 8 heat exchangers, 178 stages, and a normalized vapor flow of 10.12.

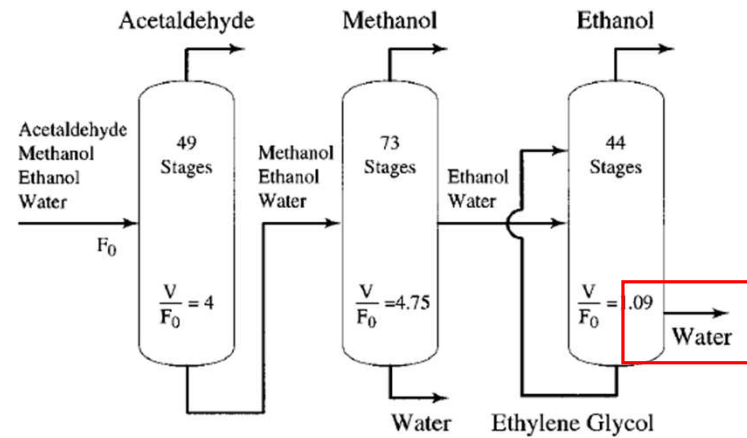


Figure 15. Third sequence to separate acetaldehyde, methanol, ethanol, and water. This sequence has a total of 3 columns, 6 heat exchangers, 166 stages, and a normalized vapor flow of 9.84.

Table 4. Summary of Design Results for the Four-Component Separation Sequences

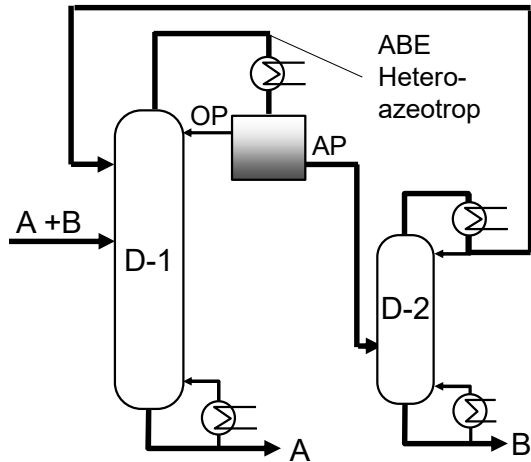
	sequence		
	first	second	third
stages	178	178	166
shells	5	4	3
heat exchangers	10	8	6
vapor flows $\sum V/F_0$	12.19	10.12	9.84

For low-purity specifications of water stream, side-stream columns can be a viable option.

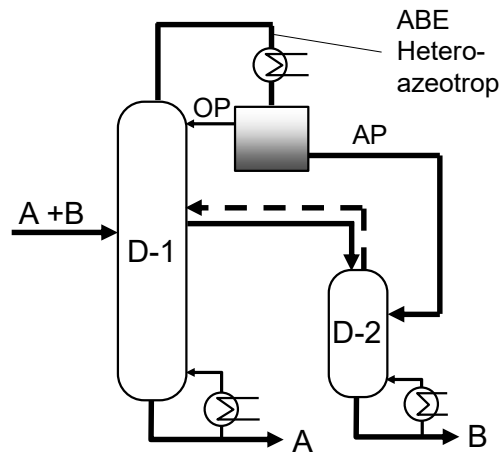
Rooks, Malone, Doherty (1996): Ind. Eng. Chem. Res., 35, 3653-3664

Derivation of Azeotropic Dividing-Wall Column

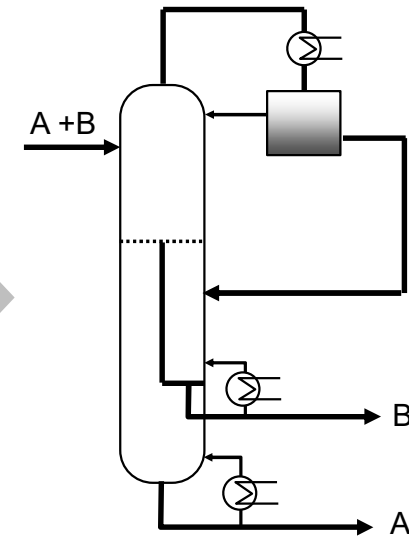
Heteroazeotropic Distillation



Heteroazeotropic Distillation /w Side Stripper



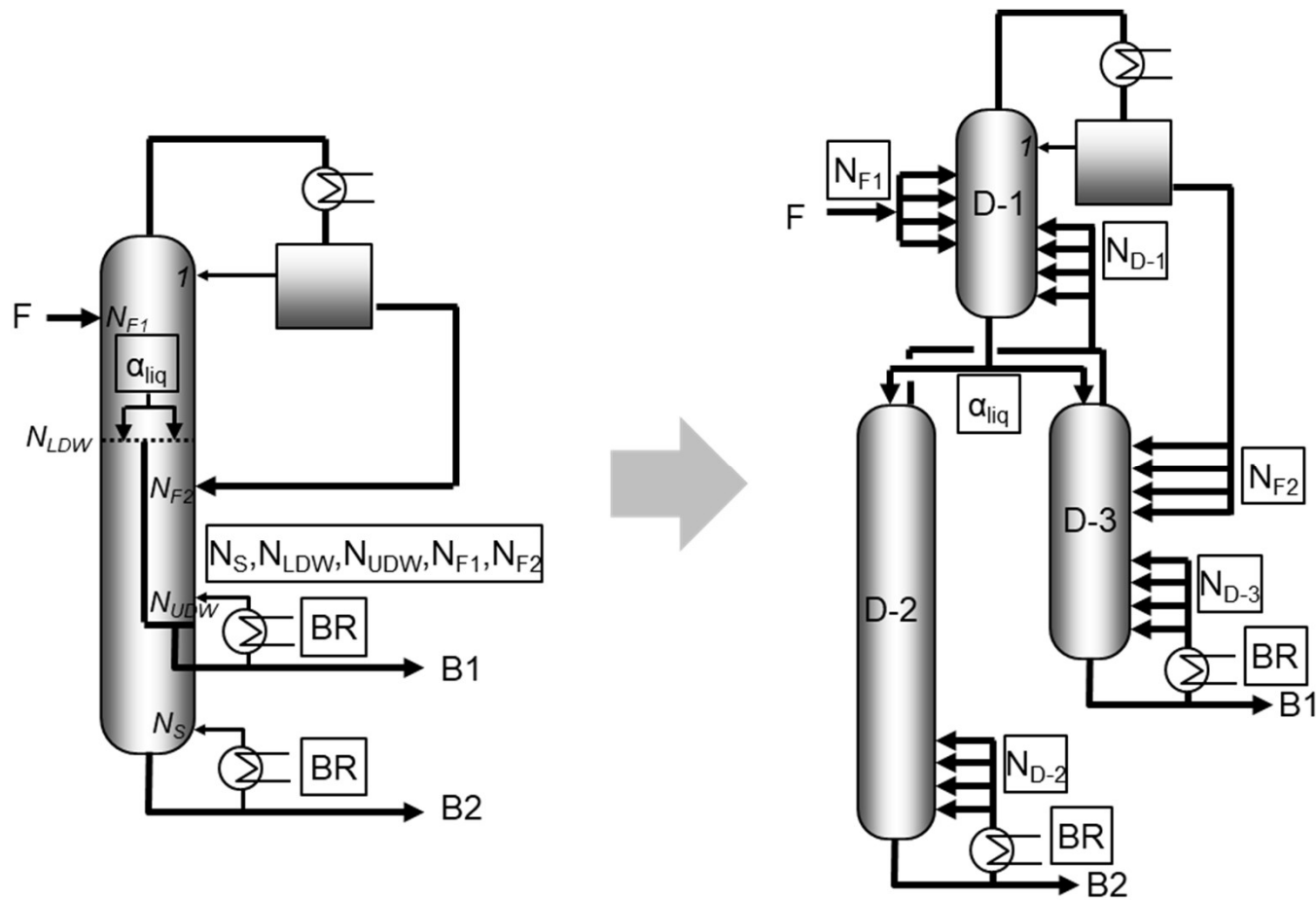
Heteroazeotropic Dividing-Wall Column



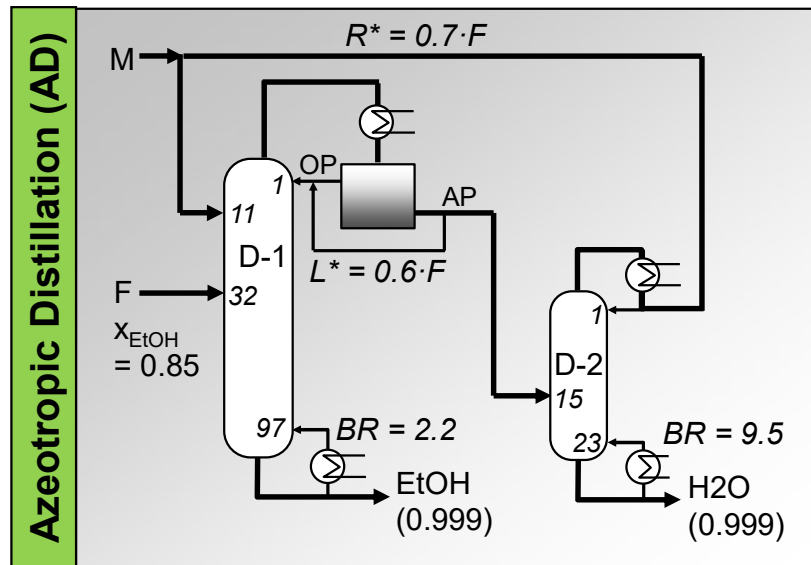
Examples:

Sun et al. (2011): Implementation of Ethanol Dehydration Using Dividing-Wall Heterogeneous Azeotropic Distillation Column
 Le, Halvorsen, Pajalic, Skogestad (2015): Dividing wall columns for heterogeneous azeotropic distillation

Azeotropic Distillation: 3-Column Substitution Model

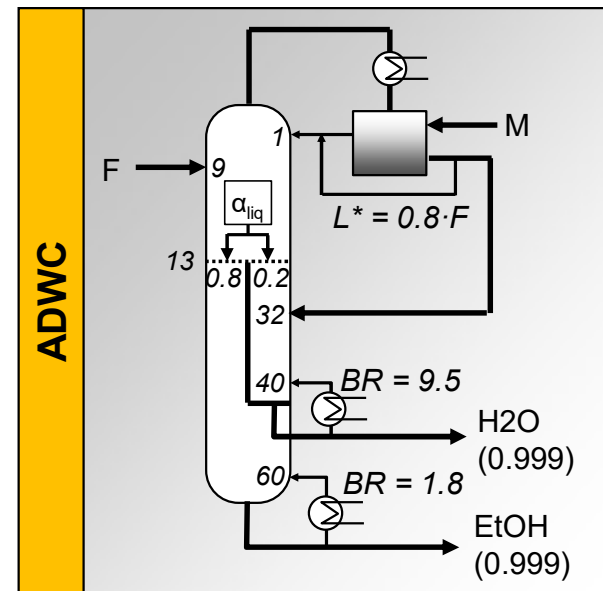


Azeotropic Dividing-Wall Column (ADWC)



*Flowsheet Optimization Variables

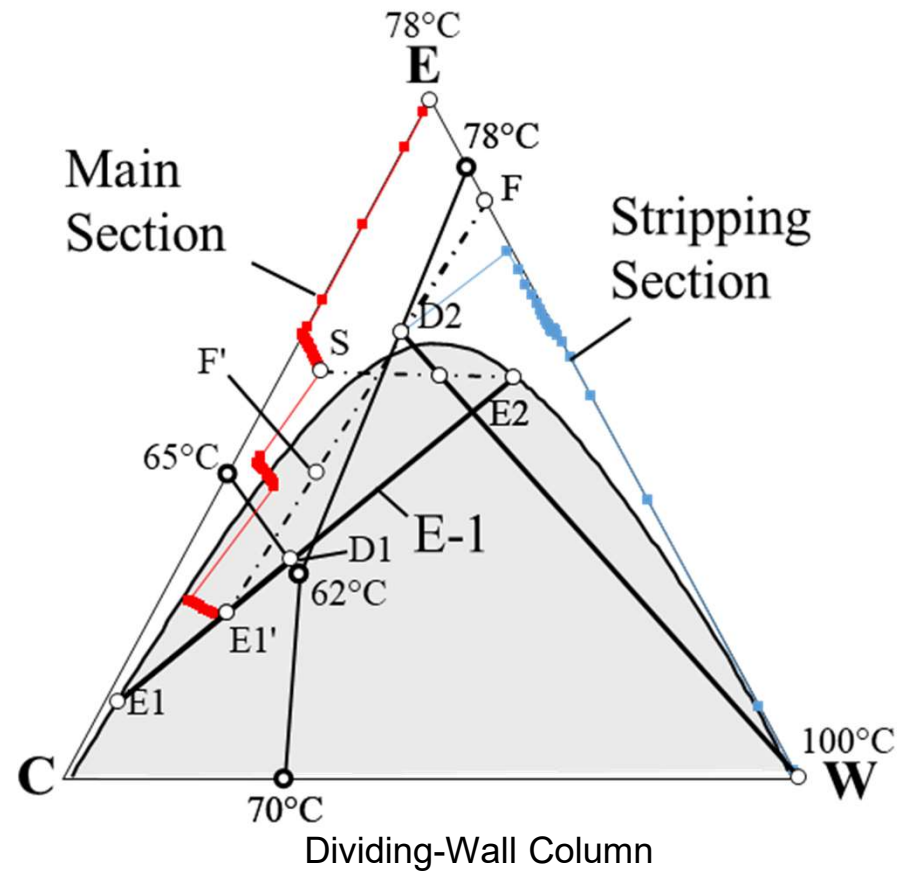
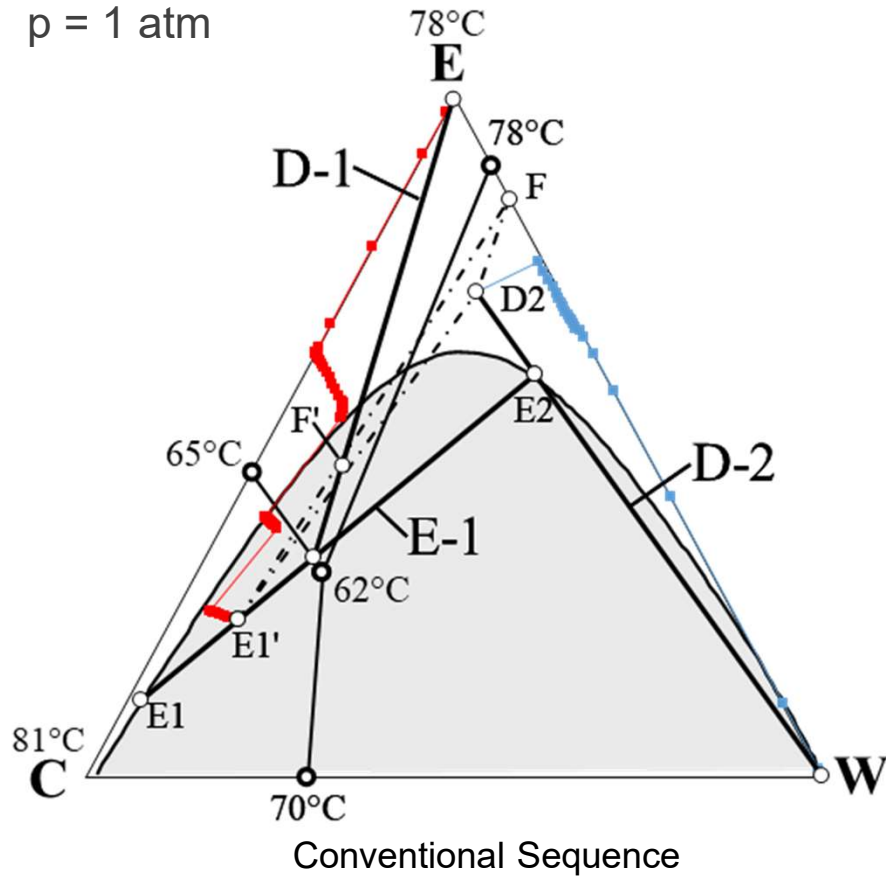
	D-1	D-2	AD	ADWC	Sav.
Q / kJ/kg EtOH	2020	1483	3503	3197	9%
No. of stages	97	23	120	60	50%
Rel. OpEx	0.38	0.28	0.66	0.59	11%
Rel. CapEx	0.25	0.09	0.34	0.29	15%
Rel. TAC	0.63	0.37	1	0.88	12%



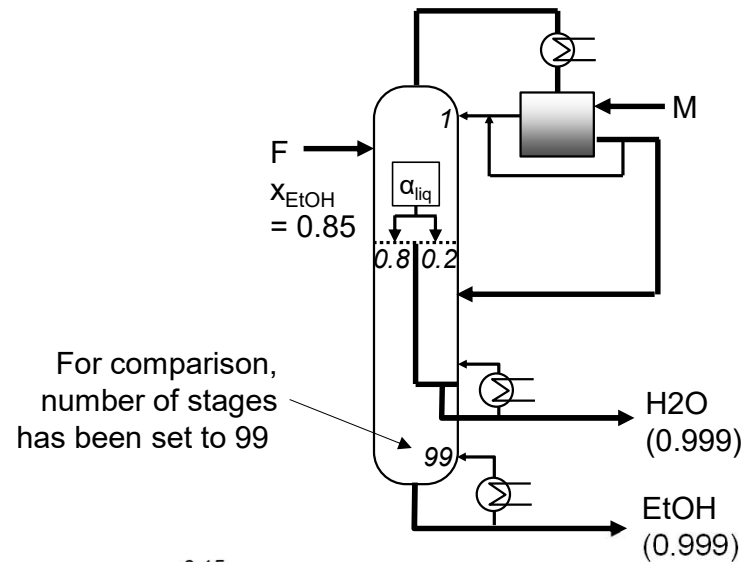
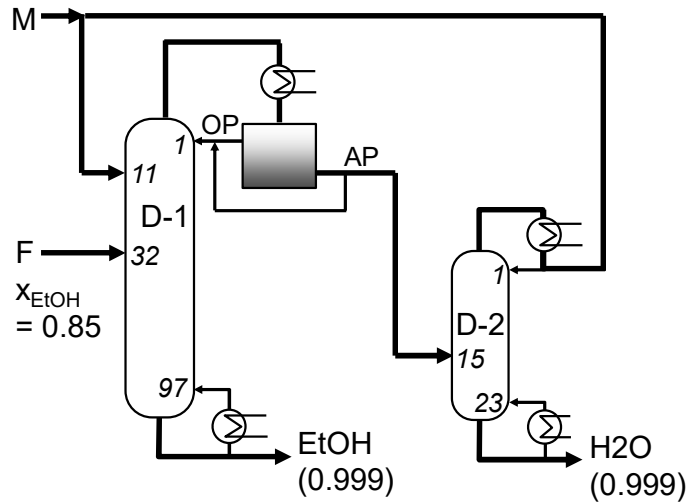
The ADWC is an economically attractive option for separating near-azeotropic ethanol/water mixtures.

Conventional Sequence vs. Dividing-Wall Column

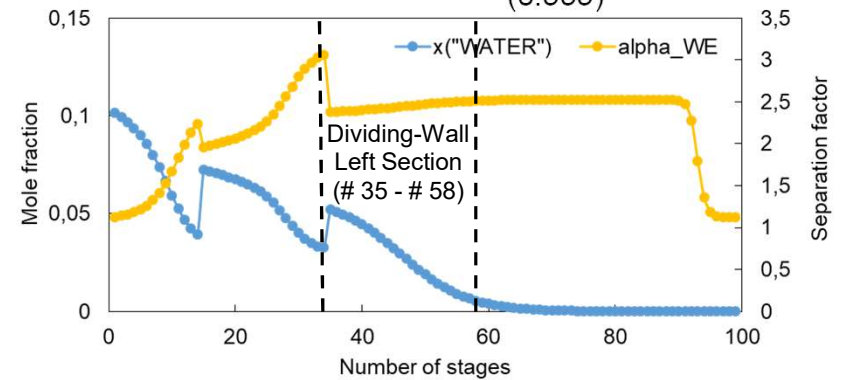
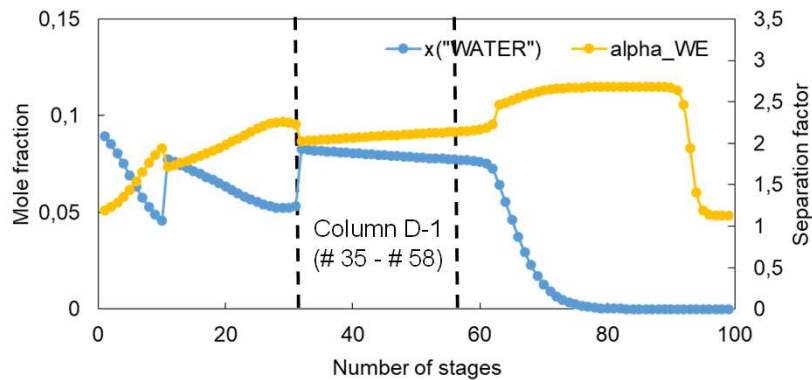
$p = 1 \text{ atm}$



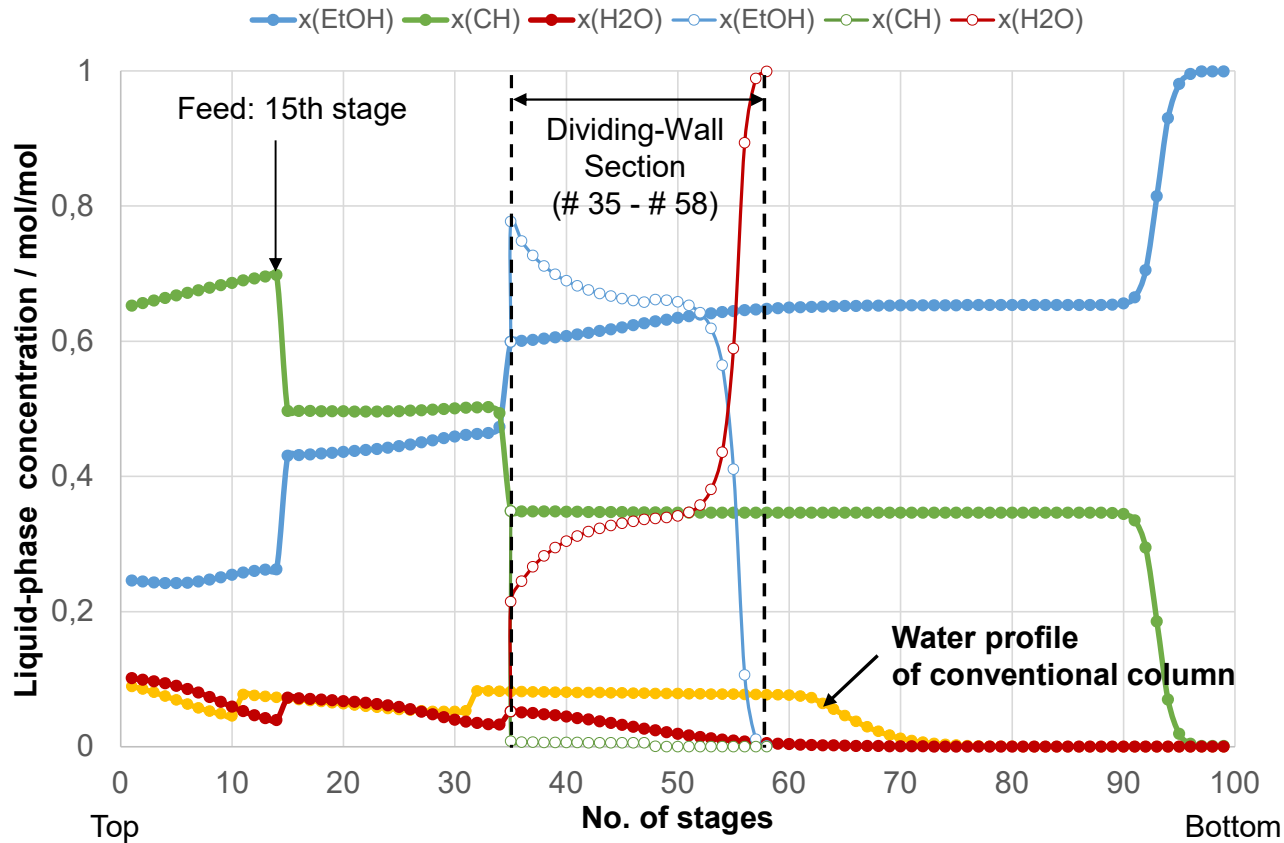
Why does the ADWC perform better?



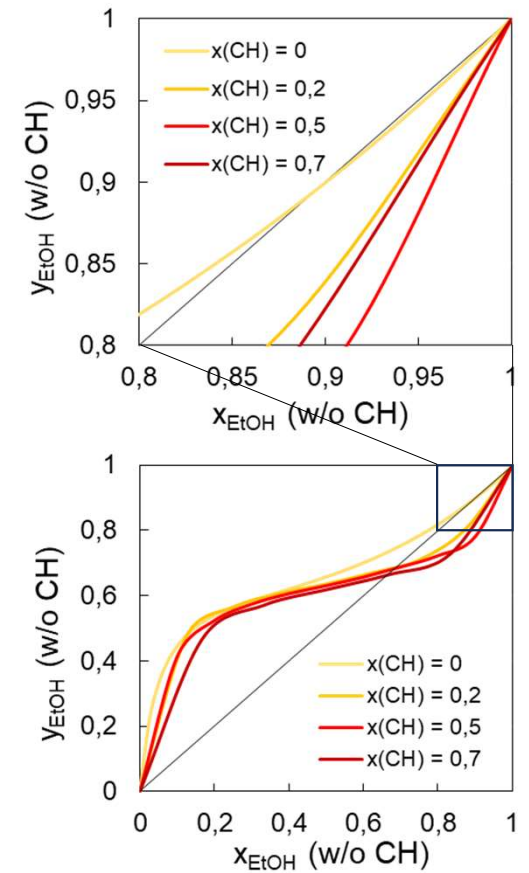
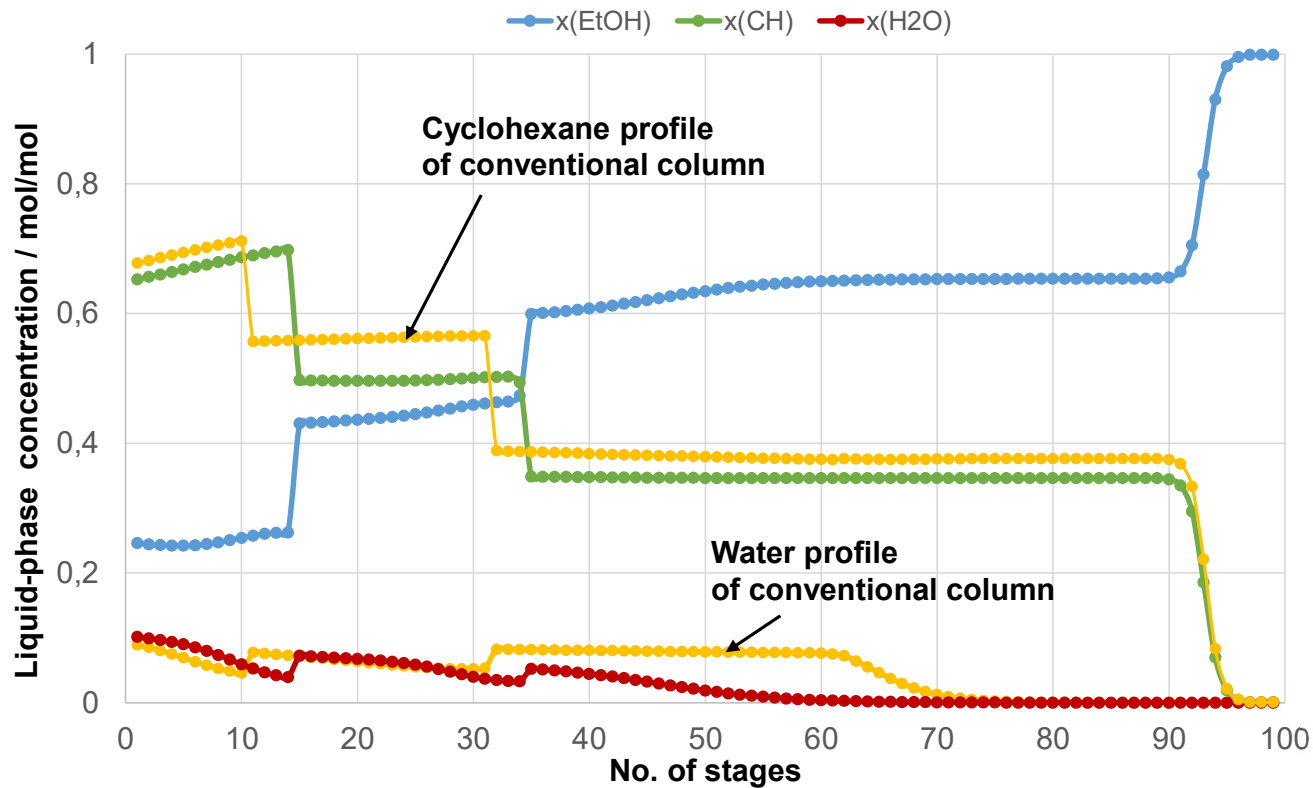
For comparison, number of stages has been set to 99



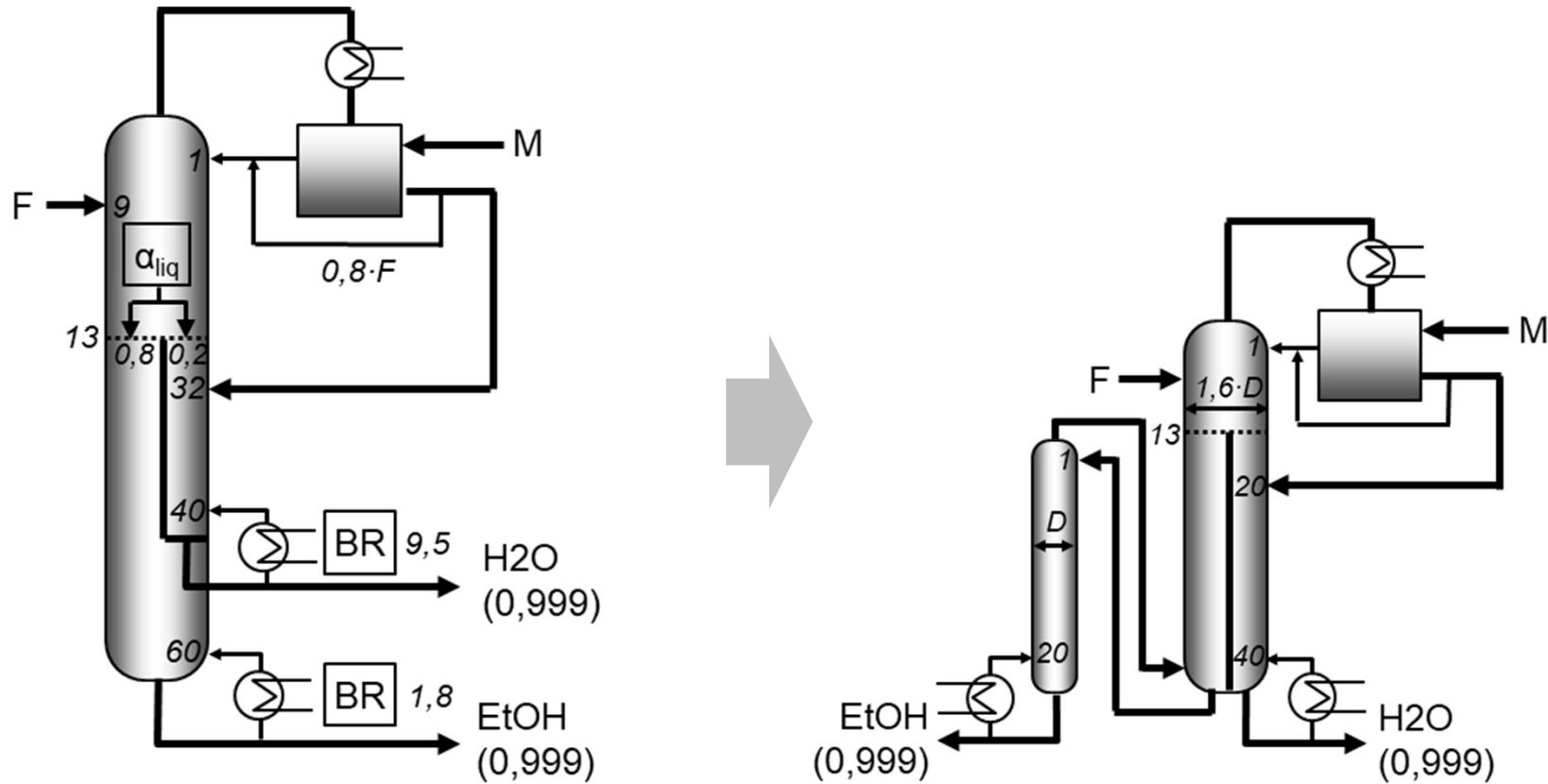
Why does the ADWC perform better? – cont'd



Why does the ADWC perform better? – cont'd



DWC Gives Rise to Alternative Designs



Conclusions

- DWC is not always the best choice
- Fair (optimization-based) comparison needed
- Visual inspection of concentration profiles not sufficient
- Pressure is an important (but often neglected) optimization variable (degree of freedom)