

Assessment of existing structures - JCSS workshop – January 28th/29th 2021

Second generation Eurocode 8 Part 3: the European document on seismic assessment and retrofit of existing structures

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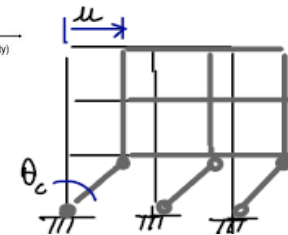
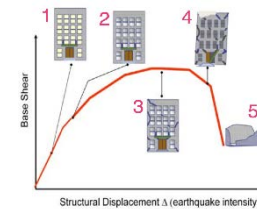
DIPARTIMENTO DI INGEGNERIA
STRUTTURALE E GEOTECNICA

Summary

1st generation Eurocode 8 Part 3 (2005)

- Specificity of assessment wrt design
 - Single knowledge level (KL)
 - Confidence factor
- Forces are not good predictors of performance
 - Displacement-based
- Assessment deals with non-conforming structures
 - Nonlinear analysis and ad hoc deformation criteria

Seismic risk (consequences of damage) mostly associated with existing structures (e.g., Italy, 85% of $E[L]$)



2nd generation Eurocode 8 (2020)

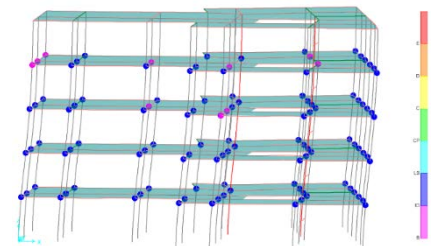
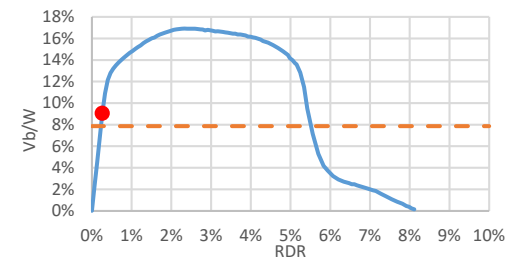
- Displacement-based approach for both assessment and design
- Multiple Knowledge Levels
- Knowledge-dependent partial factors on resistance^(*)
- A probabilistic method of assessment also introduced

Quantitative procedures!
Qualitative assessment based on past performance not really useful for seismic

Eurocode 8 Part 3 2005 (1st generation)

- Primary role of knowledge acquisition (existing \neq new)
 - Information classified into:
 - Geometry
 - (Construction) Details
 - Materials
 - Quantified by Knowledge level (KL)
 - Values: Limited, Normal, Full
 - Controlled by the least amount of information in G, D and M & unique over the structure
 - KL \rightarrow Confidence factor (CF) which divides material strength: 1,35/1,20/1,00
 - CF coexists with γ_m (e.g., γ_C , γ_S) used in traditional verification format

- Inelastic and possibly defective response is the rule.
 - Rules for nonlinear static analysis
 - Novel models for:
 - inelastic deformation capacity (chord rotation)
 - shear strength of members and joints in the inelastic range
 - strength & deformation capacity of retrofitted members



Eurocode 8 Part 3 2005 (1st generation)

- Experimental nature of the document is apparent
 - Most material (models for θ_y and θ_u , or V_R) is in informative annexes
 - KL depends on G, D, M information but it only affects M (through CF)
 - CF values are judgemental
 - Not really streamlined... Four different set of material properties used:
 - Mean (E_{cm}, f_{cm}, f_{ym}) in the model, which provides action effects on ductile modes of failure (θ)
 - Mean divided by CF ($f_{cm}/CF, f_{ym}/CF$) for evaluating the resistance of ductile failure modes (θ_y, θ_u)
 - Mean divided by CF and γ_m ($\frac{f_{cm}}{CF\gamma_c}, \frac{f_{ym}}{CF\gamma_s}$) for the resistance of brittle modes (V_{Rd})
 - Mean times CF, for the demand on brittle modes (V_{Ed}) if analysis model is linear

- Nonetheless, more than 15 years of practical application
 - Increased confidence^(*) in nonlinear analysis methods & displacement-based verifications and associated deformation models
 - Have shown that information should be sought where it is more relevant
 - Thousands of buildings have been assessed and retrofitted

Eurocode 8 Part 3 2020 (2nd generation)

- CEN/TC250 M515 (Revision of the entire Eurocodes system)
 - Extension of scope
 - EN1998-3:2005 only dealt with buildings in RC and, marginally, steel
 - prEN1998-3:2020 includes buildings and bridges + RC, steel, masonry, timber
 - Technical updating
 - Displacement-based assessment now default, scope for force-based reduced
 - Displacement-based design introduced for new structures in Part 1-1
 - (Updated) deformation and strength models moved from annexes in Part 3 → main body of Part 1-1 (i.e., used for new & existing structures)
 - Only one set of properties used, the mean ones
 - In the (nonlinear analysis) model to determine action effects
 - In the resistance formulas (θ_y , θ_u , V_{Rd} , etc)
 - To evaluate demand on brittle failure modes (V_{Ed} , curved to plastic shear) with linear analysis model

Eurocode 8 Part 3 2020 (2nd generation)

- Technical updating (cont'd)
 - More refined treatment of acquired knowledge
 - Three distinct KLs introduced for G, D and M: KLG, KLD and KLM
 - Each KL need not be uniform over the structure if newly introduced preliminary analysis is carried out^(*)

- Safety
 - On the demand side
 - Near Collapse (NC) verification replaces Significant Damage (= Life safety) as default
 - On the capacity side a unified^(**) partial factors' format to account for
 - Model (epistemic) uncertainty in the resistance formulas
 - Uncertainty (aleatoric and epistemic) in the input variables, classified in the Material properties, Geometric parameters, Construction details categories^(***)

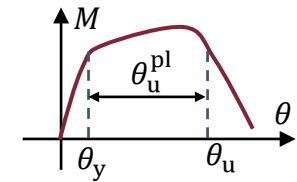
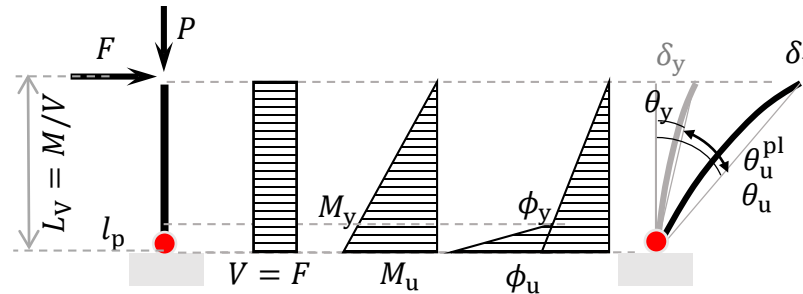
- Reliability differentiation
 - Consequence class (CC), like US risk category, determine return period of seismic action for NC verification
 - Resistance of secondary & non-critical members taken equal to its median (i.e., $\gamma_{Rd} = 1$)

(*) More focussed field investigations, save money and time (**) Consistency across different materials and verifications

(***) Stronger link between information and verifications

Resistance models: inelastic rotation capacity

- Resistance formulas
 - Models are a variable blend of mechanical and empirical

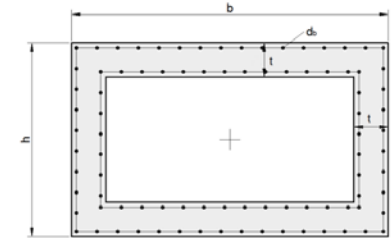


$$\theta_y = \phi_y \frac{\text{flexure } L_V + a_{VZ}}{3} + \frac{\text{slip } \phi_y d_b L f_y}{8\sqrt{f_c}} + 0,0011 \left(1 + \frac{\text{shear } h}{3,0 L_V} \right)$$

$$\theta_u = \theta_y + \theta_u^{\text{pl}}$$

$$\theta_u^{\text{pl}} = (\phi_u - \phi_y) L_{\text{pl}} \left(1 - \frac{2L_{\text{pl}}}{L_V} \right) + \Delta\theta_{u,\text{slip}}$$

RC beam/column
with hollow-core section

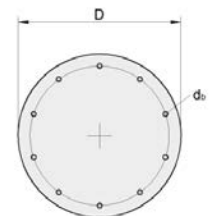


$$\theta_y = \phi_y \frac{L_V + a_{VZ}}{3} + \frac{\phi_y d_b L f_y}{8\sqrt{f_c}} + 0,0025 \left(1 - \min \left(1; \frac{L_V}{8D} \right) \right)$$

$$\theta_u = \theta_y + \theta_u^{\text{pl}}$$

$$\theta_u^{\text{pl}} = (\phi_u - \phi_y) L_{\text{pl}} \left(1 - \frac{2L_{\text{pl}}}{L_V} \right) + \Delta\theta_{u,\text{slip}}$$

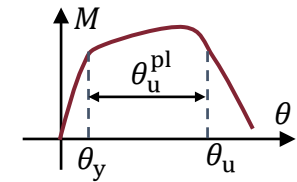
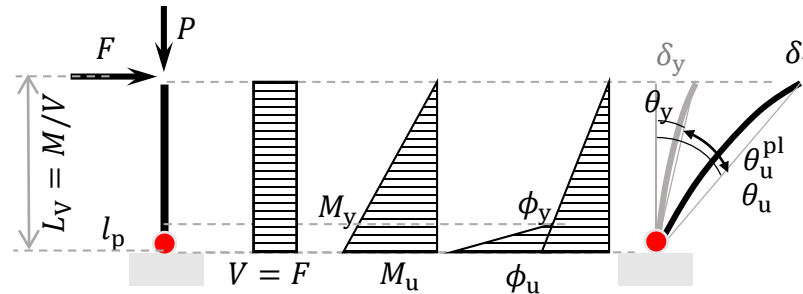
RC beam/column
with circular section



Resistance models: inelastic rotation capacity

Resistance formulas

- Models are a variable blend of mechanical and empirical



$$\theta_y = \phi_y \frac{L_V + a_V z}{3} + \frac{\phi_y d_b L f_y}{8\sqrt{f_c}} + 0,0019 \left(1 + \frac{h}{1,6L_V} \right)$$

$$\theta_u = \theta_y + \theta_u^{pl}$$

$$\theta_u^{pl} = \kappa_{conform} \kappa_{axial} \kappa_{reinf} \kappa_{concrete} \kappa_{shearspan} \kappa_{confinement} \theta_{u0}^{pl}$$

$$\kappa_{axial} = 0,2^v$$

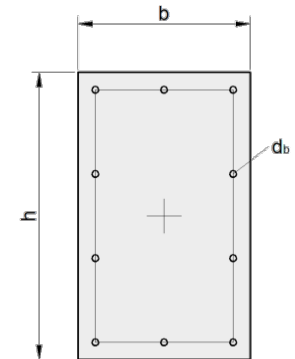
$$\kappa_{shearspan} = \left(\frac{1}{2,5} \min \left(9; \frac{L_V}{h} \right) \right)^{0,35}$$

$$\kappa_{concrete} = \left(\min \left(2; \frac{f_c (MPa)}{25} \right) \right)^{0,1}$$

$$0,039 \text{ rad}$$

$$(f_c = 25 \text{ MPa}, v = 0, \frac{L_V}{h} = 2,5)$$

RC beam/column
with rectangular section



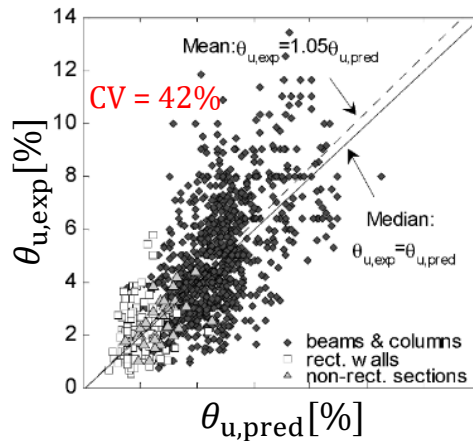
Resistance models: inelastic rotation capacity

- Resistance formulas
 - Variable blend of mechanical and empirical
 - Unbiased, CV of exp/pred ratio (model uncertainty) is available
 - “Design” models usually conservative, CV not documented

Reinforced concrete

$$\theta_y = \phi_y \frac{L_V + a_V z}{3} + \frac{\phi_y d_{bL} f_y}{8\sqrt{f_c}} + 0,0019 \left(1 + \frac{h}{1,6L_V} \right)$$

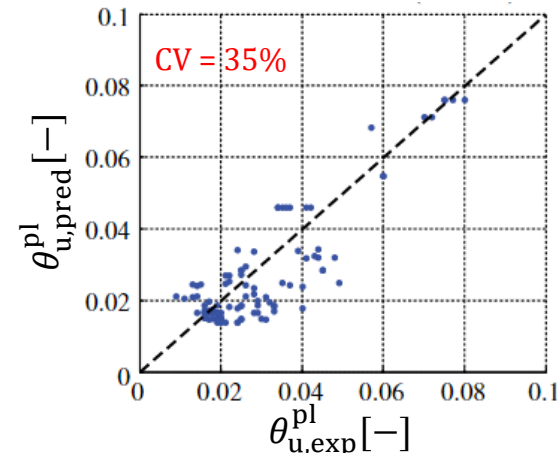
$$\theta_u = \theta_y + \theta_u^{pl}$$



Steel

$$\theta_y = \frac{L(1-n)}{6(\nu_b)EI_x} M_y = \frac{L_V M_y (1-n)}{3 EI_x \nu_b}$$

$$\theta_u^{pl} = 7.37 \left(\frac{h}{t_w} \right)^{-0.95} \left(\frac{L_b}{i_y} \right)^{-0.5} (1 - \nu_G)^{2.4}$$



Resistance models: shear strength in RC

Resistance formulas

- Variable blend of mechanical and empirical
- Unbiased, CV of exp/pred ratio (model uncertainty) is available

EN1992

$$V_{Rc} + V_{Rs} \leq V_{Rmax}$$

prEN1992:2020

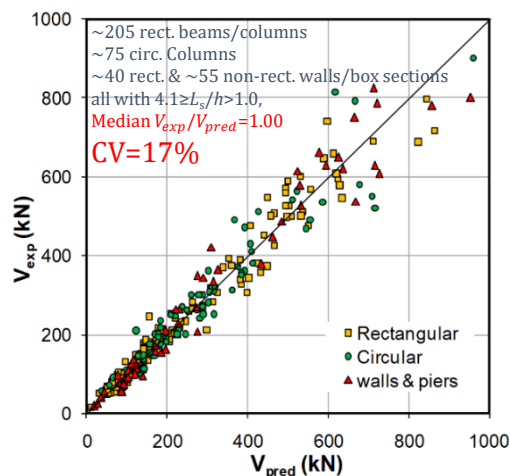
$$V_{Rc}(\epsilon_x) + V_{Rs} \leq V_{Rmax}(\epsilon_x)$$

$$\epsilon_x = \frac{1}{2 A_{s1} E_s} \left(\frac{M}{z} - \frac{N}{2} + \frac{V}{2} \cot(\theta) \right)$$

EN1998-3:2005

$$(V_{Rc}^* + V_{Rs})k(\mu) \leq V_{Rmax}^*$$

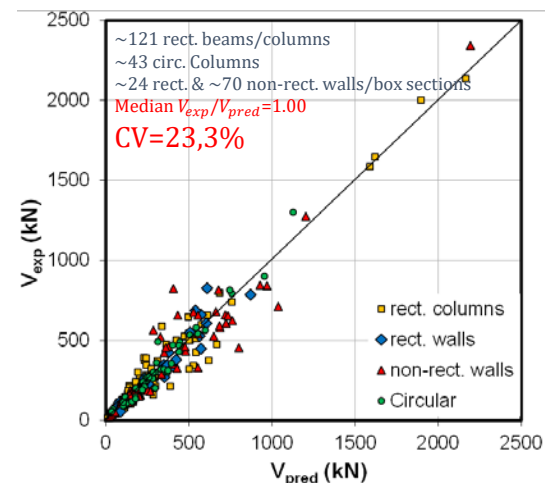
$$(V_{Rc}^* + V_{Rs})k(\mu) + V_{RN} \leq V_{Rmax}^*$$



prEN1998-1-1:2020

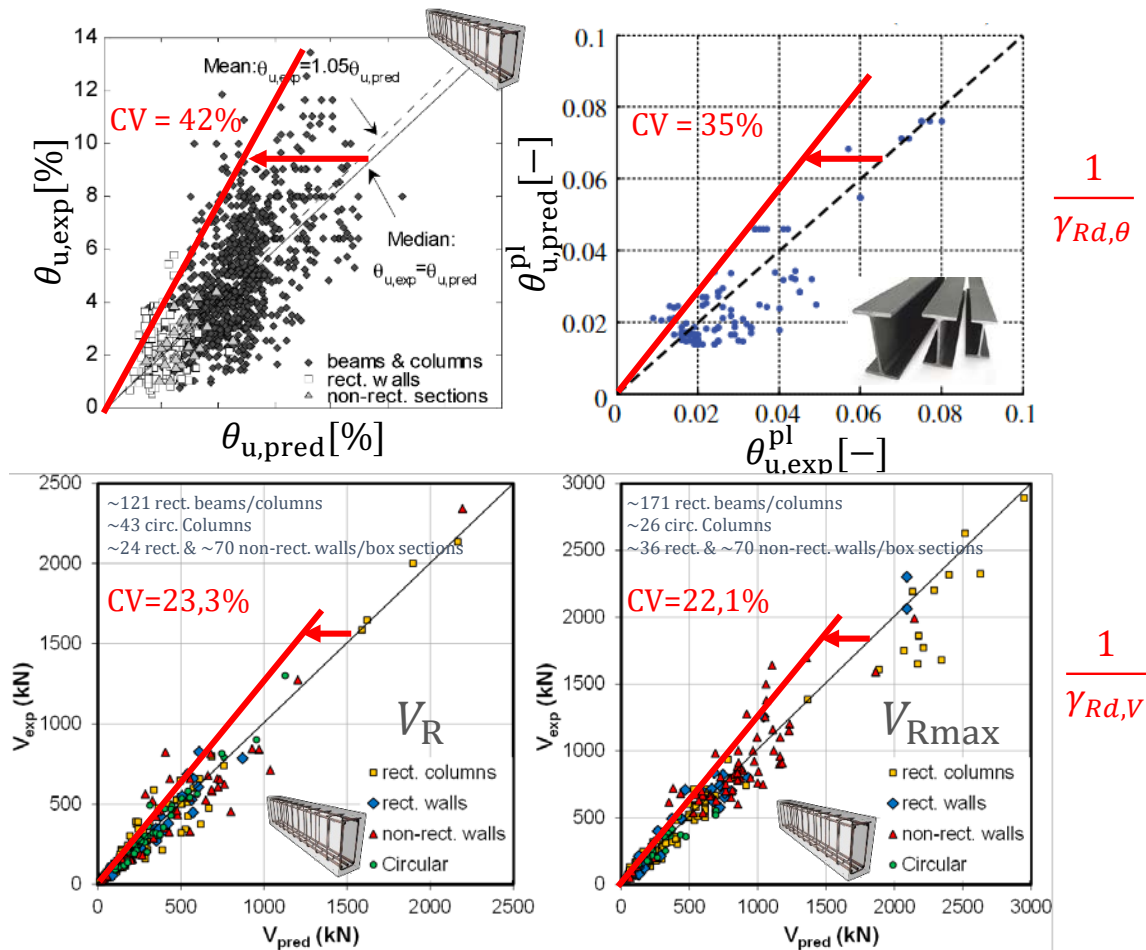
$$V_{Rc}(\epsilon_x) + V_{Rs} + V_{RN} \leq V_{Rmax}(\epsilon_x)$$

$$\epsilon_x = \frac{1}{2 A_{s1} E_s} \left(\mu \frac{M}{z} - \frac{N}{2} + \frac{V}{2} \cot(\theta) \right)$$



Partial factors on resistance

- Evaluation of median of resistance with best estimate properties
- Lower fractile for verification through a single member-level partial factor

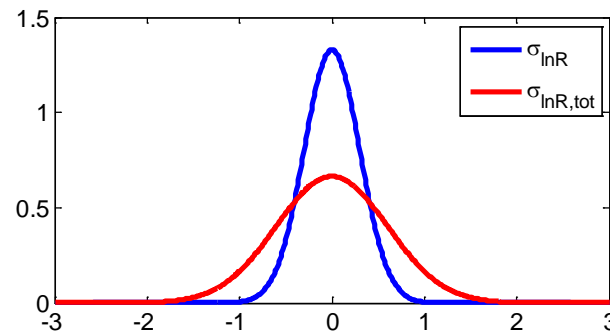


Partial factors on resistance: formulation

- Fractile k can be obtained from median, if $\sigma_{\ln R, \text{tot}}$ is known

$$R_k = e^{\mu_{\ln R} + k\sigma_{\ln R, \text{tot}}} = \hat{R} e^{k\sigma_{\ln R, \text{tot}}} \rightarrow \gamma_{Rd} = \frac{\hat{R}}{R_k} = e^{-k\sigma_{\ln R, \text{tot}}}$$

- The total logarithmic standard deviation is a function of
 - Model uncertainty (CV of exp/pred) $\sigma_{\ln R}$
 - Variability (aleatoric+statistical) of input variables (e.g., f_c, L_V, ρ_w)



- All formulas in Eurocode 8 can be put in the form

$$R(\mathbf{x}) = \hat{R}(\mathbf{x})\epsilon_R \rightarrow \ln R(\mathbf{x}) = \ln \hat{R}(\mathbf{x}) + \tilde{\epsilon}_R$$

← Input variables
← Model error

Partial factors on resistance: formulation

- Linearization of $\ln \hat{R}(\mathbf{x})$ around $\hat{\mathbf{x}}$ leads to an expression for $\sigma_{\ln R, \text{tot}}$

$$\ln R(\mathbf{x}) = \ln \hat{R}(\hat{\mathbf{x}}) + \sum \left. \frac{\partial \ln \hat{R}}{\partial \ln x_i} \right|_{\hat{\mathbf{x}}} (\ln x_i - \mu_{\ln x_i}) + \tilde{\epsilon}_R =$$

$$= \ln \hat{R}(\hat{\mathbf{x}}) + \sum \left[\frac{\hat{x}_i}{\hat{R}(\hat{\mathbf{x}})} \left. \frac{\partial \hat{R}}{\partial x_i} \right|_{\hat{\mathbf{x}}} \right] (\ln x_i - \mu_{\ln x_i}) + \tilde{\epsilon}_R =$$

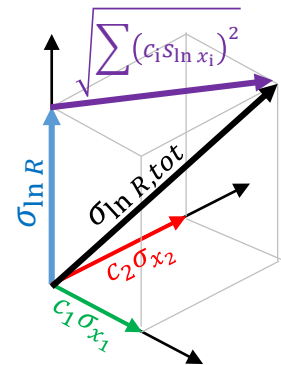
Median @ median

Correction for the log

Sensitivity to x_i

$$= \ln \hat{R}(\hat{\mathbf{x}}) + \sum c_i \tilde{\epsilon}_i + \tilde{\epsilon}_R$$

Tangent/Secant



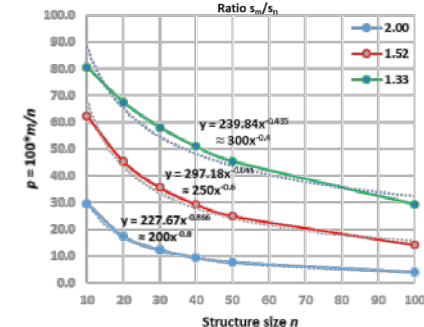
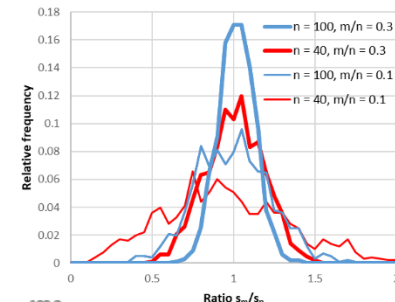
- Total logarithmic standard deviation is then

$$\sigma_{\ln R, \text{tot}} = \sqrt{\sigma_{\ln R}^2 + \sum (c_i \sigma_{\ln x_i})^2}$$

- The $\sigma_{\ln x_i}$ is only imperfectly known (limited testing)

$$\sigma_{\ln R, \text{tot}}(KL) = \sqrt{\sigma_{\ln R}^2 + \sum (c_i s_{\ln x_i})^2}$$

$r_i \sigma_{\ln x_i}$



Partial factors on resistance: formulation

Table 5.1 — KLG on Geometry as a function of collected information

| Original design documents (outline or detailed construction drawings) | Extent of survey* | | |
|--|-------------------|------|------|
| | L | E | C |
| Not available | KLG1 | KLG2 | KLG3 |
| Incomplete set | KLG2 | KLG3 | |
| Complete set | KLG3 | | |

* L: limited; E: extended; C: comprehensive (see 3.1.3)

(2) If **discrepancies** between the structural drawings and the survey results are significant, a more extensive dimensional survey should be performed (e.g., from limited to extended), or a lower KLG should be adopted.

(3) For each type of element (column, wall, beam, floor diaphragm, etc.), the minimum percentage of structural elements (reinforced concrete or steel) that should be surveyed for dimensions is given by Formula (5.1), depending on the required extend of survey.

$$p = p_1 n^{-c} \leq 100 \quad (5.1)$$

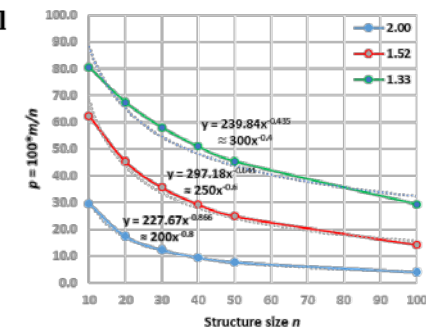
where:

n is the total number n of elements of this type in the structure, determined according to (5);

p_1 and c are coefficients which should be taken from Table 5.2 for each level of survey.

Table 5.2 — Minimum requirements for different levels of survey (vertical elements*)

| Level of survey | Limited (L) | Extended (E) | Comprehensive (C) |
|-----------------|-------------|--------------|-------------------|
| p_1 | 200 | 250 | 300 |
| c | 0,8 | 0,6 | 0,5 |



Partial factors on resistance: calibration

- $\sigma_{\ln R, \text{tot}}(\mathbf{x}, \mathbf{KL}) \rightarrow \gamma_{\text{Rd}}(\mathbf{x}, \mathbf{KL})$ depends on the structural member, i.e. \mathbf{x}

$$\gamma_{\text{Rd}}(\mathbf{x}, \mathbf{KL}) = e^{-\kappa \sqrt{\sigma_{\ln R}^2 + \sum (c_i(\mathbf{x}) s_{\ln x_i})^2}} \quad \mathbf{KL} = \{\text{KLG} \quad \text{KLD} \quad \text{KLM}\}$$

- Luckily $\gamma_{\text{Rd}}(\mathbf{x})$ is reasonably stable with \mathbf{x}

└─→ Min., Average, High

- Further, KLG, KLD, KLM each has 3 values
 - This leads to $3^3 = 27$ values of $\gamma_{\text{Rd}}(\mathbf{x})$

- One KL, however, normally dominates each formula

$$\text{„} \frac{\partial \sigma_{\ln R, \text{tot}}}{\partial \text{KL}} \text{“} = \frac{\sqrt{\sum_{j \in \text{KL}} (c_j s_{\ln x_j})^2}}{\sigma_{\ln R, \text{tot}}}$$

Sum only over x_i belonging to KLj (e.g., f_c is KLM)

- It is possible to evaluate on a large parameters' space the factor for each formula and then tabulate an average value as a function of the dominant KL

Partial factors on resistance: calibration

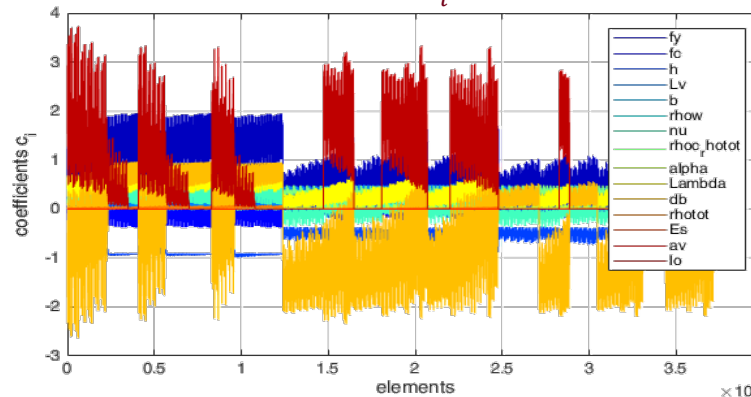
- For each formula a parameter space has been defined
- 27 values of $\gamma_{Rd,KL}(\mathbf{x})$ have been computed, then simplified to 3 wrt to dominant KL
- For now, «calibration» = matching the resistance implied by the previous code (2005)

Assumed $\sigma_{ln x_i}$

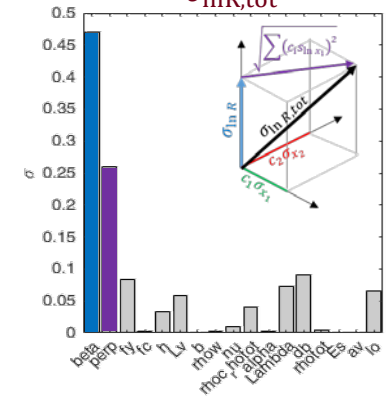
| | | type | $\sigma_{ln x_i}$ (existing) |
|--------------|-----------------------------|------|------------------------------|
| f_y | steel yielding stress | KLM | 0.10 |
| f_c | concrete resistance | KLM | 0.15 |
| d_b | long.rebar diameter | KLD | 0.20 |
| v | normalized axial load | KLG | 0.10 |
| ρ_{tot} | total long.geom.ratio | KLD | 0.20 |
| ρ_w | trasversal geom.ratio | KLD | 0.20 |
| E_s | steel elastic module | KLM | 0.00 |
| a_v | boolean variable | KLG | 0.00 |
| Λ | overlapping ratio | KLD | 0.20 |
| l_o | long.reinf. sovrapp. length | KLD | 0.10 |
| μ | ductility parameter | KLG | 0.20 |

Table 1: Variability in the shared parameters.

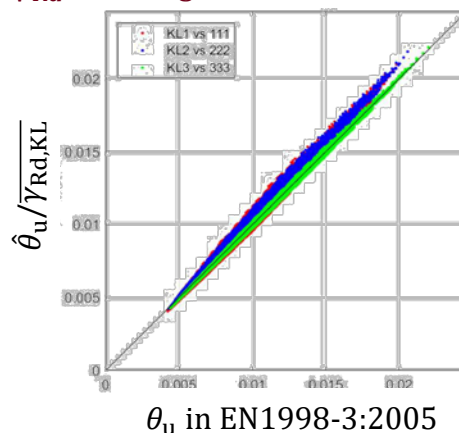
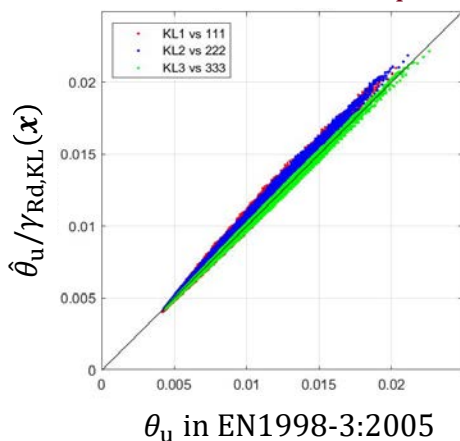
Coefficients c_i



$\sigma_{ln R,tot}$



Member-dependent $\gamma_{Rd} \cong$ average one



$3^3 = 27 \gamma_{Rd}$ values and dominant KL (Details in this case)

| | | | | | | | | | |
|-------------|------|------|------|------|------|------|------|------|------|
| KLG: | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 3 |
| KLD: | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 |
| KLM:1 | 1.66 | 1.61 | 1.60 | 1.65 | 1.60 | 1.58 | 1.64 | 1.59 | 1.58 |
| KLM:2 | 1.66 | 1.61 | 1.60 | 1.65 | 1.60 | 1.58 | 1.64 | 1.59 | 1.58 |
| KLM:3 | 1.66 | 1.61 | 1.59 | 1.64 | 1.60 | 1.58 | 1.64 | 1.59 | 1.57 |

(b) γ_{Ra,θ_u} (G) M sens. = 0.058 **0.190** 0.008

Simplified table with 3 γ_{Rd} values (dominant KL only)

| KLD | 1 | 2 | 3 |
|---------------|------|------|------|
| γ_{Rd} | 1,67 | 1,62 | 1,57 |

Conclusions

- Seismic assessment and retrofit design in Eurocode 8 is
 - Quantitative
 - Displacement-based
 - Employs nonlinear analysis and inelastic deformation criteria
- Safety on the resistance side is ensured by using γ_{Rd} , member-level partial factors on resistance that
 - Divide the median resistance evaluated with best-estimate properties
 - The same properties that enter into the (nonlinear) model
 - Are consistently derived across all materials and failure modes
 - Account for model uncertainty and uncertainty on input variables
 - Are tabulated vs the dominant KL
 - Each formula is most sensitive to one between Geometry, Details and Materials
 - Can be changed at national level with a single formula (*)