

FORMELLISTE

Annenderiverttesten:.

$$\Delta = AC - B^2 \quad \text{der} \quad A = f_{xx}, \quad B = f_{xy}, \quad C = f_{yy}$$

Koordinatsystemer:.

Sylinderkoordinater: $x = r \cos \theta, \quad y = r \sin \theta, \quad z = z,$

$$r^2 = x^2 + y^2, \quad dV = r dz dr d\theta$$

Kulekoordinater: $x = \rho \sin \varphi \cos \theta, \quad y = \rho \sin \varphi \sin \theta, \quad z = \rho \cos \varphi,$

$$\rho^2 = x^2 + y^2 + z^2, \quad dV = \rho^2 \sin \varphi d\rho d\varphi d\theta$$

Flateintegral:.

$$dS = |\vec{N}(u, v)| du dv = \left| \frac{\partial \vec{r}}{\partial u} \times \frac{\partial \vec{r}}{\partial v} \right| du dv$$

Tyngdepunkt for romlige legemer:.

$$\bar{x} = \frac{1}{m} \iiint_T x dm, \quad \bar{y} = \frac{1}{m} \iiint_T y dm, \quad \bar{z} = \frac{1}{m} \iiint_T z dm$$

Vektoranalyse:.

Greens teorem: $\oint_C P dx + Q dy = \iint_R \left(\frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y} \right) dA$

Divergensteoremet: $\iint_S \vec{F} \cdot \vec{n} dS = \iiint_T \nabla \cdot \vec{F} dV = \iiint_T \text{div} \vec{F} dV$

Stokes teorem: $\oint_C \vec{F} \cdot \vec{T} ds = \iint_S (\nabla \times \vec{F}) \cdot \vec{n} dS = \iint_S (\text{curl} \vec{F}) \cdot \vec{n} dS$

der $\nabla = \left\langle \frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z} \right\rangle$