All problems are to be written up clearly and thoroughly, using complete sentences. This assignment is due in discussion at 2pm on Thursday, June 6th.

For all T/F problems on the homework, provide a brief justification for your answer. That may be citing an appropriate theorem or providing a counterexample.

1. Section 6.2 problems 1, 2 a, b, g, i, k, 5, 6, 7, 8, 9, 13, 17, 19

2. Section 6.3 problems 1, 2 a, b, 3a, b, c, 4, 6, 7, 8, 9, 12, 14, 15

   An *isometry* is a linear operator $T : V \to V$ such that $\langle T(x), T(y)\rangle = \langle x, y\rangle$ for all pairs $x, y \in V$.

3. Let $V$ be a finite-dimensional inner product space over $\mathbb{F} = \mathbb{R}$ or $\mathbb{C}$.
   (a) Fix $y \in V$ and suppose $\langle x, y\rangle = 0$ for all $x \in V$. Show that $y = 0$.

   (b) Let $T : V \to V$ be an isometry. Prove that $T$ is an isomorphism.

   (c) Find all isometries $T : \mathbb{R}^2 \to \mathbb{R}^2$ that have $\det T = 1$.