INHERITANCE OF BEHAVIOR IN
OBJECT-ORIENTED DESIGNS FOR
INDUSTRIAL CONTROL SYSTEMS

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Abstract: The paper presents a feasible approach to introduce object-oriented
techniques in the industrial practice of control design. The approach is based on
the use of a domain-specific extension of the modeling language UML and on the
formalization of design models as transition systems for verification purposes. In
particular, the paper shows how to exploit model checking techniques to verify
that object classes, designed as subtypes, correctly inherit the behavior of their
base classes, according to a notion of substitutability specifically defined for the
proposed semantics of object-oriented models. Copyright © IFAC 2005

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1. INTRODUCTION

The emerging technologies for industrial con-
trol systems are putting more and more empha-
sis on concepts like modularity and reusability
of components (both hardware and software),
in order to increase efficiency of manufactur-
ing systems design and reduce time spent dur-
ing the installation of machines and the opera-
tional qualification of production lines. For ex-
ample, the well-known standard for PLC (Pro-
grammable Logic Controllers) programming IEC
61131-3 (I.E.C., 2002) and the newer standard
IEC 61499-1 (I.E.C., 2000) for distributed con-
trol systems, define frameworks for the implemen-
tation of modular software architectures, based
on program organization units called Function
Blocks (FBs). Even though the mentioned tech-
nologies incorporate many high-level concepts de-

gerived from the most recent Software Engineer-
ing principles, practical applications in the manu-
ufacturing domain of methods like object-oriented
modeling or formal verification are quite rare. Se-
veral examples of academic projects that have
attempted to fill this gap can be mentioned, for
example the references in the review (Frey and
Litz, 2000). Nevertheless, there are still important
reasons limiting the appeal of formal methods
from the point of view of industrial control design-
ers, first of which the difficulties in the interpreta-
tion of some theoretical concepts within the pecu-
liarities of the application domain and its day-to-
day practice. These difficulties could be overcome
adopting an “easy to use” modeling language and
customizing it in order to include domain-specific
aspects, making at the same time rigorousness
of formal approaches transparent for technicians
without a background on formal methods. With
these remarks as a basic point, the paper presents
a domain-specific adaptation and formalization
of an object-oriented modeling language, namely
UML (O.M.G., 2001), and how to formalize within
this modeling framework the concept of behavioral
inheritance between classes in a design model.
The rest of the paper describes in Section 2 the modeling language considered, in Section 3 its semantical formalization, with particular regard to inheritance of behavior, and in Section 4 the tools that could support designers for model verification. The paper ends with an illustrative example and some concluding remarks.

2. OBJECT-ORIENTED MODELING AND INDUSTRIAL CONTROLLERS

From a software engineering point of view, the features of IEC 61131-3 and IEC 61499-1 can be defined Object-Based, since FBs have many similarities with objects as defined in modern programming languages: they are defined as types and used as instances, they encapsulate both private algorithms and data and they communicate with other software modules through well-defined interfaces, composed of input and output signals. Even though FBs allow to develop modular control software, neither of the IEC standards can be considered fully Object-Oriented (O-O) in a proper sense, because they do not include the feature of inheritance. However, this lackness should not prevent from the use of O-O design techniques, for example supported by modeling languages like UML and design tools with automatic code generators, provided that a proper interpretation and implementation-level mapping of abstract design concepts is defined. In fact, UML is defined by an extensible meta-model, which means that domain-specific concepts can be added to the language by means of stereotyped elements and well-formedness rules or constraints (i.e. expressed in Object Constraint Language (O.M.G., 2001)).

The rest of the section will describe an extension of UML which can be adopted to design industrial control applications, focusing on a subset of the language that allows to completely specify structure and behavior of a system.

Structural views of an O-O system are described with UML by means of Class Diagrams, in which class symbols have compartments to show their properties (i.e. attributes and operations) and graphical links between them represent simple association, aggregation/composition (part-whole relationship) and generalization (a class derives from another), which involves inheritance. An important property that can be associated to a class is represented by its stereotype, which defines its conceptual role in a domain-specific model. For industrial control applications, it is important to specify structural aspects from a mechatronic perspective, which means that software modules must be considered in a tight aggregation with the physical sub-systems that they control. This aggregate, that we call mechatronic object, should have a signal-based interface, in order to exchange events with other mechatronic objects of a machine, and the description of its internal structure should highlight relationships with hardware components (i.e. sensors/actuators). The UML stereotypes that we have defined permit to describe classifiers for mechatronic objects as <<mechatronic>> classes, which have an interface of publicly visible properties, in their turn stereotyped as <<input>> or <<output>>. A <<mechatronic>> class cannot have any public operations, while private operations may be used to model complex data-processing activities. The part of a <<mechatronic>> class related to the connection with physical components is specified with the help of classes stereotyped as <<hardware>>. Classes of this kind are always related by means of a composition link with a <<mechatronic>> class and their <<input>> and <<output>> properties represent the hardware I/O ports as a private part of the <<mechatronic>> class. Figure 1 shows the graphical representation of the proposed stereotypes in a UML Class Diagram. It can be noted that mechatronic objects are quite similar to actors in the ROOM language (Selic et al., 1994), which communicate with each others through the messages exchanged through well-defined ports, consistently with a given protocol. However, the concept of interface for mechatronic objects is simpler and more similar to the one proposed by IEC standards: each <<input>> or <<output>> signal represent a “port” of a given type (including EVENT). A complete structural model for a complex machine would be defined by one or more Class Diagrams, in which part/whole relationships between modules are modeled by composition links between mechatronic classes. The physical interpretation of objects in this framework suggests the definition of well-formedness rules prescribing that there must always be a single “top-level” class (i.e. the machine), that shareable aggregation links cannot be used, and that composition links must be qualified with fixed multiplicity, since dynamic creation of objects is not admissible.

The behavioral specification of the system must be specified describing the internal behavior of each class with a UML State Diagram, a kind of state model strictly derived from Harel’s Statecharts (Harel, 1987). In the proposed UML extension, the Statechart of a <<mechatronic>> class represents

![Fig. 1. UML stereotypes for mechatronic models](image-url)
the behavior of the controller, while the Statechart of a «hardware» class models the plant’s behavior. With regard to textual expressions in Statecharts (i.e. transition labels and state actions), their specification with an IEC 61131-3 compatible syntax would ease automatic code generation for industrial controllers. In particular, we propose to label transitions with strings having the format:

\[
\text{trigger}[\text{guard}] / \text{actions}
\]

where events in the trigger can be inputs of the stereotyped class or outputs of its contained instances, explicitly typed as EVENT. The guard must also be a valid boolean expression, and actions will follow the same rules of the similar string included in a state action, which is specified by a textual expression like:

\[
\text{when} / \text{actions IF}[\text{guard}]
\]

Here, when is a qualifier that can be entry or exit, guard is an optional boolean expression that may prevent the action from being executed, if it evaluates to false, and actions is an ordered list of operations that can: set or reset a boolean variable, assign the value of an expression to a variable of a non-boolean data-type, or emit an attribute typed as EVENT.

3. FORMALIZATION OF MECHATRONIC MODELS

The underlying semantics of the modeling language described in previous section must be formalized taking into account the peculiarities of the application domain which make adequate some parts of the UML semantics. In particular, the semantics of Statecharts is defined in UML by a Run-To-Completion execution algorithm, based on an event-queue for each object, in which events are processed one at a time. This interpretation is counter-intuitive for the implementation on synchronous devices like PLCs, for which the “original” Statecharts semantics of (Harel and Naamad, 1996) is more suitable. Moreover, the common O-O definitions of inheritance in terms of structural conformity (e.g. name consistency of public operations) are not appropriate for the domain of industrial control and for a design methodology in which components behavior is specified with state models. The correct interpretation of the inheritance concept must consider behavioral conformity and substitutability of state-based behaviors, with definitions similar to those reported in (Harel and Kupferman, 2002). Therefore, we define the instantiation of the top-level class in a UML mechatronic model as a mechatronic system

\[
M_S = (M, t, \Gamma)
\]

where \( M \) is a set of instances of mechatronic classes, \( t \in M \) is the top-level one and \( \Gamma : M \rightarrow 2^M \) is a function that retrieves for each instance the ordered set of its components. The composition of \( M_S \) is univocally determined by multiplicity of aggregation links in the UML model and each \( M_i \in M \) is an univocally referable instance of a mechatronic class \( C_j \). A mechatronic class is defined as

\[
C = (S, T, P, r, \gamma)
\]

where \( S \) is a set of states, \( T \) is a set of transitions, \( P = P^I \cup P^O \) is a set of “port” variables, each one of a given data type (including event), \( r \in S \) is the root state and \( \gamma \) is an ordered set of contained instances of other mechatronic classes. The hierarchical aspects of the Statechart of a class \( C \) are defined by typing each \( s \in S \) as an AND-state, OR-state or basic, and by the functions \( def(s) \), which retrieves the default state of each OR-state, \( chldn(s) \), which retrieves the set of immediate substates of \( s \), and \( chldn^*(s) \), the reflexive-transitive closure of \( chldn(s) \). A configuration is a subset of \( S \) which is maximally consistent (i.e. all of its elements can be simultaneously active) and \( compl(X) \) retrieves a configuration which is the default completion of a consistent set \( X \). We also define as \( B \) the set of boolean expressions over variables in \( P^I \cup \bigcup_{M_i \in \gamma} P^O_i \), as \( A \) the set of assignments over variables in \( P^O \cup \bigcup_{M_i \in \gamma} P^I_i \) and as \( E \) the set of event expressions over variables \( P^I \cup \bigcup_{M_i \in \gamma} P^O_i \), which consists of boolean expressions that contain only variables typed as events. These definitions permit to associate with each transition \( tr \in T \) the following attributes:

\[
\text{src}(tr) \in S, \text{trig}(tr) \in E, \text{actor}(tr) \in A,
\]

\[
\text{compl}(X) \text{ retrieves a configuration which is the default completion of a consistent set } X.
\]

\[
\text{trig}(tr) \text{ is the trigger expression, } \text{grd}(tr) \in B, \text{ the guard expression, } \text{act}(tr) \in 2^A, \text{ a set of assignment actions, and } \text{targ}(tr) \in S, \text{ the target state. The scope of a transition } tr \text{ is the smallest OR-state containing both } \text{src}(tr) \text{ and } \text{targ}(tr), \text{ while } \text{maxsrc}(tr) \text{ is the unique child of the scope of } tr \text{ such that } \text{src}(tr) \in chldn^*(\text{maxsrc}(tr)). According to these definitions, when } tr \text{ is fired the state } \text{maxsrc}(tr) \text{ and all of its descendents } (chldn^*(\text{maxsrc}(tr))) \text{ are de-activated, while } \text{targ}(tr) \text{ and the states in its default completion are activated. A transition is enabled if the predicate}
\]

\[
en(tr) = \text{in}((\text{src}(tr))) \land \text{trig}(tr) \land \text{grd}(tr)
\]

is true (\( \text{in}(\text{src}(tr)) \) means that the source state is active), but is firable only if an additional predicate \( \text{conflict}(tr) \) is false, which happens if no other transition with a priority higher than that of \( tr \) is enabled. The priority rules we have adopted enforce an explicit order, fixed at design time, between transitions with the same source state and give higher priority to transitions exiting states at a higher level in the hierarchy. To conclude, we assume that states \( s \in S \) have an associated list of actions, each defined as a tuple \((w, a, t, g)\), where
$w \in \{\text{entry}, \text{exit}\}$, $a \in 2^A$ is a set of assignments and $g \in B$ is a guard expression.

The reaction of a mechatronic class instance to external stimuli is defined as a step, in which the next state configuration and the next value of each variable are computed. Each instance in a mechatronic system $M_S$ performs its step when it is marked as active, instead of idle by a scheduling function, whose formal detail are not specified here. The most simple scheduling function would cyclically mark active each $M_i \in M$ according to a fixed sequential order (i.e. the typical PLC scan cycle). Whatever is the scheduling function, we assume that input ports of an instance $M_i \in M$ typed as events retain their truth value until $M_i$ becomes active and are immediately set false when $M_i$ has terminated to compute its step, which means that no event can remain undetected. Each instance of a generic mechatronic class $C$ is initialized in the configuration $Sc_0 = \text{compl}(r)$, with given initial assignments to variables in $P \cup \bigcup_{M_i \in C} P_i$, and each one of its steps is performed as follows:

1. compute the set of firable transitions $F_i = (tr | T_i | \text{en}(tr) \wedge \neg \text{conflict}(tr))$;
2. compute the next configuration $Sc_i' = \text{compl}((Sc_i - \bigcup_{tr \in F_i} \text{chldn}^*(\text{maxsrc}(tr))) \cup \bigcup_{tr \in F_i} \text{targ}(tr))$;
3. execute exit actions related to exited states, actions associated with each $tr \in F_i$ and entry actions related to entered states.

The execution of a step transforms the status of an instance $M_i$ from $\sigma_i = (Sc_i, V_i)$ to $\sigma'_i = (Sc'_i, V'_i)$, in which $V_i$ and $V'_i$ are current and next values of each variable in $P_i \cup \bigcup_{M_j \in C} P_j$. The observable status of an instance is defined as $\text{obs}V_i$ and is the value of the variables in $P_i$. The global status of a mechatronic system $M_S$ is given by $\sigma_S = (\sigma_1, ..., \sigma_n)$, where $n$ is the cardinality of $M$, and its behavior, given a scheduling function, is determined by the set $\mathcal{L}_{M_S}$ of all the possible finite and infinite sequences $\sigma^0, \sigma^1, \sigma^2, ..., \sigma^k$, in which the change between $\sigma^i$ and $\sigma^{i+1}$ is determined by the step of one instance.

In order to formalize the concept of behavioral conformity between mechatronic classes, we follow the so-called Liskov Substitution Principle (Liskov, 1988), which states that a class can be considered a subtype of another one if the behavior of an object-oriented system, defined in terms of the base class, is not affected by the substitution of all the instances of the base class with instances of the derived class. In our interpretation, since the instances of a class can influence the global behavior of a mechatronic system only by means of their input/output ports, we analyze the computational sequences of the system focusing on the value of that kind of variables. Therefore, we define as the observable behavior of a mechatronic class $C$ in a mechatronic system $M_S$, which contains $r$ instances of $C$ with indexes between $l$ and $l + r$, the set $\mathcal{L}_C$ of all the sequences $\sigma^0_C, \sigma^1_C, \sigma^2_C, ..., \sigma^K_C$ that can be extrapolated from $\mathcal{L}_{M_S}$, in which $\sigma^K_C$ is composed by the observable status of all the instances of $C$, that is $(\text{obs}V_{1l}, ..., \text{obs}V_{1l+r})$. Consistently with the previous definitions, we can define that a class $C_1$ is substitutable with another class $C_2$ having the same interface (i.e. $P_1 = P_2$), if for any mechatronic system $M_S$, with the same scheduling function,

$$\mathcal{L}_{M_S}^{C_1} \subseteq \mathcal{L}_{M_S}^{C_2} \quad (4)$$

that is the observable behavior of $C_2$ can extend the observable behavior of $C_1$, without deleting any observable sequence.

4. CHECKING SUBSTITUTABILITY

The substitutability of mechatronic classes as defined in previous section can be checked with the help of specific tools supporting formal verification techniques for finite state systems. In particular, the Cadence version of the tool SMV (McMillan, 1999), originally developed at Carnegie Mellon University, adopts Symbolic Model Checking (McMillan, 1993) to verify refinement of components in modular transition systems. Here, we will briefly describe how to translate in the SMV language the behavioral specification of mechatronic classes and how to exploit the tool’s feature for refinement verification as a way to prove their substitutability. The SMV language allows to describe a finite state system with constructs to declare modules and data-types, supports both boolean and integer arithmetic and has specific constructs to initialize state variables and to assign them the next value in a computational path. A mechatronic class can be translated as an SMV module as follows:

```module MechClass(Active, I1, I2, O1, O2)
{ input Active, I1, I2 : boolean;
 output O1, O2 : boolean;
 Instantel : MechClass1(...);
 ... }
```

where Active is a boolean input set true according to the scheduling function, the other parameters represent the observable interface and Instantel is one of the contained instances of other modules. The Statechart specification will be translated encoding the hierarchy of states into variables with enumerated values:

```Root : {State1, State2, ..., StateN};
SUBState1 : {State11, ..., State1B};```
and evaluating the configuration and the set of enabled and actually firable transitions with predicates defined as follows:

\[
\begin{align*}
\text{INState1} & := (\text{Root} = \text{State1}); \\
\text{INState11} & := \text{INState1} \& (\text{SUBState1} = \text{State11}); \\
\text{ENTrans1} & := \text{INStateXX} \& \text{Trigger} \& \text{Guard}; \\
\text{CONFLTrans1} & := \text{ENTrans2} | \text{ENTrans3} | \ldots; \\
\text{FIRABLETrans1} & := \text{ENTrans1} \& \neg \text{CONFLTrans1};
\end{align*}
\]

Finally, initialization and execution of a step can be translated as follows:

\[
\begin{align*}
\text{init}(\text{Root}) & := \text{State1}; \quad \text{-- default state} \\
\text{init}(\text{SUBState1}) & := \text{State11}; \quad \text{-- default state} \\
\text{default} \{ \text{next}(\text{Root}) := \text{Root}; \quad \text{-- no state change} \\
\quad \text{next}(\text{O1}) := \text{O1}; \ldots \} \\
\text{in case} \{ \text{Active} \& \text{FIRABLETrans1} : \\
\quad \text{next}(\text{Root}) := \text{State2}; \quad \ldots \}
\end{align*}
\]

which states that if no transition is firable the status of the module remains unchanged (default statements), otherwise it is opportually changed.

An SMV program is completed by the declaration of a main module (i.e. the top-level) and by the specification of desired properties of the system, to be proved by model checking, expressed with CTL and LTL (Allen Emerson, 1996) temporal logics or in terms of refinement maps. In the latter case, SMV will explore the computational paths of the system to prove that the assignments to a given set of variables are compatible with those specified in a so-called abstract layer. In practice, SMV can prove that every possible behavior of a system implementation is also a possible behavior of the system specification. In our case, in order to check that two classes are substitutable, we have to define the base class as the implementation layer and the derived class as the abstract layer. This is translated in SMV as follows:

\[
\text{module main(){} }
\begin{align*}
\text{I1, I2, \ldots} & : \text{boolean}; \\
\text{O1, O2, \ldots} & : \text{boolean}; \\
\text{C1} & : \text{BaseClass}(1, \text{I1, I2, \ldots, O1, O2, \ldots}); \\
\text{layer derived :{} } \\
\quad \text{C2} & : \text{DerivedClass}(1, \text{I1, I2, \ldots, O1, O2, \ldots});
\end{align*}
\]

Notice that the instances C1 and C2 are always active. When SMV opens a similar program, it automatically defines as properties to check formulas written as Oi//derived, where Oi is an output signal in both C1 and C2. Each one of these properties is verified if the values taken by Oi along any computational path of the instance C1 are compatible with those taken along the paths of the instance C2, declared in the layer derived. The inputs of both instances are assumed free variables, which means that are allowed to range over any possible value of their types. If these properties are all proved, then the observable behavior of any instance of the base class is contained in the observable behavior of any instance of the derived class, for any possible stimulus that they can receive, which proves substitutability of the base class with the derived class in any mechatronic system.

5. EXAMPLE

An example of a manufacturing machine quite common in the packaging industry is schematized in Fig. 2. This kind of machine is called horizontal packer and has the following processing principle: products are inserted in an horizontal “tube”, which is made wrapping around the film and sealing it along the longitudinal direction, then the film is sealed transversally and cut, in order to release the packed product.

![Fig. 2. Packaging machine with horizontal flow](image)

A structural model of this machine, from the perspective of control design, can be described with UML as shown in Fig. 3. The diagram shows that the class Longitudinal sealer has a derived version named Enhanced Longitudinal Sealer, which has implicitly (because of structural inheritance) the same interface and contained instances (i.e. Heater and Temperature Sensor) of the base class, plus an additional instance of Heater, referred as ExtraHeater (name of the composition link).

![Fig. 3. Class Diagram of the horizontal packer](image)
substitutability, following the heuristics suggested by some object-oriented methodologists, like those in (Douglass, 1999). In particular, Fig. 4 shows a possible (simplified) Statechart for the base behavior and Fig. 5 an extended Statechart in which the state Increase Temp. has been refined in order to include a substate in which the extra heater is powered, to speed up the rise of the measured temperature, and another in which it is switched off, with a transition between them that may be triggered, for example, by a timer.

Fig. 4. Basic Statechart for a longitudinal sealer

Fig. 5. Refined Statechart for a longitudinal sealer

This refinement do not change the behavior observed from the top-level class Horizontal Packer, which sends to the longitudinal sealer Start and Stop events and reads a high value on the boolean signal SealingOK when the measured temperature is above 400° C. The behavioral conformity of the two classes can be verified writing an SMV program as described in previous section and, in case of positive answer from the model checking tool, the two Statecharts can be translated into the internal behavior of two software components (i.e. FBs) for PLC applications. Of course, both operations can be done automatically with the help of a CASE tool supporting UML and customizable code generation.

6. CONCLUSION AND FUTURE WORK

The paper has described a domain-specific extension of the modeling language UML which can be easily adopted by industrial control engineers to design programs for PLC-based systems. The concept of inheritance, characterizing the object-oriented approach to software and systems design, has been formalized in a definition specifically studied for the application domain. In the future, the definitions contained in the present paper will be extended to consider more complex cases of refinement (i.e. extension of the interface). Moreover, the authors aim to integrate the proposed concepts into a CASE tools that can support industrial control engineers in their design practice.

REFERENCES


