Abstract—Microalgae have the potential to produce enough biofuels to meet the current US fuel demands. In order to achieve this potential, photobioreactors (PBRs) need to be developed that are efficient, scalable, and affordable. Models are an analytical tool that can be used to evaluate various PBRs. In this article, a dynamic model is developed for growing microalgae in a vertical flat panel photobioreactor (PBR) that may be used to measure PBR efficiency for various architectures independent of scale. The growth model is used to estimate the microalgae growth and byproduct production and consumption as a function of incident light. A feed-forward controller is developed that uses the estimated amount of CO\(_2\) consumed to determine the amount of additional CO\(_2\) to add to the system during photosynthesis. An overall controller structure that uses both feed-forward and feedback control is presented for growing microalgae inside a PBR.

I. INTRODUCTION

Microalgae can convert carbon dioxide (CO\(_2\)) into storage lipids that can be refined into biofuels. More CO\(_2\) is being produced now than in previous years, and there is limited supply of fossil fuels in the world. Under the right conditions, microalgae will utilize the excess CO\(_2\) being produced by human activity to produce lipids that may help supplement the limited fuel supply. There are two control objectives to this process, namely maximizing biomass growth and maximizing storage lipid production (i.e., the lipids that are favorable for biofuel production). The focus of this article is on improving biomass production by regulating key variables (e.g., pH, dissolved CO\(_2\), dissolved O\(_2\), and temperature). While the use of models and controllers to improve lipid production are not discussed here, lipid production was achieved through the use of an appropriate microalgae strain [1].

A program of research sponsored by the National Renewable Energy Laboratory from 1978-1996 estimated that microalgae could produce lipids at the rate of 7,000 - 15,000 gallons/acre/year [2], almost 100X the current productivity of lipids from soy, at roughly 50-100 gallons/acre/year [1]. This means that microalgae could meet 50% of all transport fuel needs of the United States while using only 1.1% to 2.5% of the existing US cropping area [1]. While this is encouraging, there have been numerous problems with scaling up to a large production scale [3]. The primary challenge has been to design a PBR that is able to utilize intense light and maintain appropriate gas concentrations at a commercial scale (c.f., [1], [3], [4], [5], [6], [7], [8], [9]).

Various PBR configurations (e.g., bubble columns, raceway ponds, and flat panel reactors) have been studied in [8]. Each configuration has its advantages and disadvantages. The trade-offs are finding reactors that utilize high light intensities well, can remove produced dissolved oxygen well, and scale well. A variety of linear and nonlinear models have been developed to address this for tubular reactors (c.f., [4], [5], [6], [7], [9], [10], [11], [12], [13], [14], [15]). However, there has been significantly less publications on flat panel reactors, which is the style of reactor addressed in this paper. Model based controls have been developed in [9], [16], [17], [18], [19], [20]. Most of these papers model growth as a function light using a Monod kinetics model. The Monod model describes how bacteria go through an exponential, linear, and decaying growth phases as they consume their nutrients. This idea is extended to how microalgae grow in a light limited closed PBR. This is an entirely empirical model that works well for some situations. In this paper, a scalable model is developed that addresses these phases by considering the physics of microalgae growth inside a vertical flat panel PBR that was developed at Solix Biofuels. The microalgae growth rate is modeled as a function of incident light. Based on the light driven dynamic growth model, an estimate of the amount of CO\(_2\) required for photosynthesis may be delivered as a feed-forward (FF) control input to the PBR. A feedback controller is used to maintain a constant pH, which is also regulated using input CO\(_2\). A photo of the actual PBR used for these experiments is shown in Figure 1.

II. METHOD

In this section, an overall growth model is developed that may be used as a FF controller for pH regulation. The model is primarily physics-based with a few parameters that are fit from data. For the most part, these fitted parameters are efficiency parameters that may be used to compare the performance of different operating conditions and various PBR configurations.

Microalgae Growth Modeling and Control for a Vertical Flat Panel Photobioreactor

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Fig. 1. Photobioreactor Test Bed at Solix Biofuels in Fort Collins, Colorado

A. Photobioreactor Setup

Fig. 1 shows one of the PBR test beds at Solix Biofuels in Fort Collins, Colorado. In the larger PBR bath (on the left), there are four PBRs. Each PBR consists of vertical flat panels submerged in the bath. Sensors are placed throughout the PBR to measure the amount of dissolved O₂ (DO), pH, and optical density (OD). The OD sensor correlates well to dry mass and was used to measure microalgal accumulation. Input gas streams of pure CO₂ and air are continuously delivered through mass flow controllers (MFCs). These gas streams are then mixed and bubbled through the flat panels. This sparging is used to maintain elevated levels of dissolve CO₂ by regulating to a lower pH, remove DO produced by photosynthesis, and to mix the microalgae, which determines the light/dark cycle. The bath provided structure for the vertical flat panels and was used to regulate the temperature of the microalgae inside the vertical flat panels.

B. Overall Dynamic Model

There are three main subsystems that interact with each other, namely the incident light to the PBR, the microalgal cells that suspended in the media, and the media itself. The amount of incident light that the microalgae can utilize is a function of sun position and the amount mixing. As the microalgae grow, they interact with the media to remove nutrients and dissolved carbon while releasing dissolved oxygen. A gas mixture of air and CO₂ is bubbled through the media to maintain the appropriate dissolved carbon level and to remove the produced dissolved oxygen through mass transfer. Since the amount of nutrients and dissolved gases in the media will effect the growth rate, these parameters are fed back from the media (water chemistry) model to the microalgal (photosynthesis) model. These phenomenon are captured in the overall PBR model in Fig. 2 that contains the three major subsystems, namely the light subsystem (red), the photosynthesis subsystem (green), and the water chemistry subsystem (blue). The details of each subsystem are described in the remainder of this section.

C. Incident Light Subsystem

About 45% of the full spectrum of light is photosynthetically active radiation (PAR) which is the amount of light (in the 400nm to 700nm range) available for photosynthesis on earth. The incident light subsystem determines the amount of PAR that will reach the microalgae, which is a function of the number of PAR photons that enter the PBR bath, mixing, and PBR geometry. This may be expressed as

\[ I_{\text{PAR}} = f_1(\text{PAR}_{\text{bath}}, \text{mixing}, \text{geometry}) \]  

(1)

The amount of PAR that enters the bath is a function of both the direct and diffuse light that are incident on the PBR bath, which was measured with a PAR sensor. For the model verification presented in this paper, the mixing (i.e., gas flow rate) and geometry were held constant. Therefore, the following simplified model of equation (1) was used.

\[ I_{\text{PAR}} = \eta_{\text{PBR}} \cdot \text{PAR}_{\text{sensor}} \]  

(2)

Here, \( \eta_{\text{PBR}} \) is the efficiency of the PBR for a given mixing and geometry. The variable \( \text{PAR}_{\text{sensor}} \) is the number of PAR photons measured by the PAR sensor. Currently, the term \( \eta_{\text{PBR}} \) is absorbed into the PAR utilization constant \( K_{\text{PAR}} \) in the next section. Therefore, \( I_{\text{PAR}} = \text{PAR}_{\text{sensor}} \) is used for the current growth model. However, as more information becomes available about the effects of mixing and geometry,
it will be incorporated into calculating a more accurate $I_{\text{PAR}}$ term.

**D. Growth Subsystem**

The growth subsystem models the dynamics of the microalgae as they utilize photons from the sun, CO$_2$, and nutrients to produce O$_2$ and more microalgae. The rate at which microalgae grow depends on their ability to utilize the incident light and on the availability of nutrients. Assuming there are ample nutrients available, microalgae growth is primarily a function of input light. When there is an absence of light, the microalgae respire (i.e., utilize O$_2$ and stored carbon as an energy source, which releases CO$_2$). Respiration results in a loss of biomass. In the presence of light, the microalgae will both evolve O$_2$ as they assimilate carbon from dissolved CO$_2$ and respire O$_2$ as they consume stored carbon; however, the growth from carbon assimilation will often dominate the metabolic process$^1$. When the culture is sparse, there are an excess number of PAR photons that are not being utilized. Under this condition, microalgae will grow exponentially, since the produced algal mass will not be limited by available photons. At some point, the algal density will become great enough that all of the incident light will be utilized. At densities greater than this, the microalgae growth rate will be linear. As the density continues to increase, a smaller fraction of the microalgae will be able to receive the amount of light required for photosynthesis and respiration will be the dominant metabolic activity. As this happens, the total microalgae growth in the PBR will cease and eventually begin to decay. In the model, this feature is captured by saturating the density in the growth term. When the density gets above a critical density, labeled $m_{\text{dense}}$, the amount of growth resulting from photosynthesis becomes linear while the density lost due to respiration remains exponential. These effects are described by the following nonlinear differential equation.

$$
\dot{m}_{\text{algae}} = P\bar{m}_{\text{algae}} - Rm_{\text{algae}}
$$

where

$$
P = K_{\text{PAR}}I_{\text{PAR}}
$$

$$
\bar{m}_{\text{algae}} = \min(m_{\text{algae}}, m_{\text{dense}})
$$

$$
m_{\text{dense}} = f(m_{\text{algae}}, \text{mixing, geometry})
$$

The state variable $m_{\text{algae}}$ is the amount of microalgae inside the PBR and its derivative, namely $\dot{m}_{\text{algae}}$, is the growth rate of microalgae inside the PBR. The productivity parameter $P$ is the specific growth rate at a given sun intensity. The term $K_{\text{PAR}}$ is the *sun utilization* parameter that converts incident light, namely $I_{\text{PAR}}$, into microalgae growth rate, and the constant $R$ is the rate of biomass loss due to respiration in the dark. The microalgae also respire while exposed to sunlight, so the respiration term is still appropriate during growing times. However, the rate of respiration is known to be greater during sunlight exposure. This discrepancy is hard to measure directly. Instead, it is wrapped into the $K_{\text{PAR}}$ parameter (i.e., photorespiration results in a smaller sun utilization parameter). Finally, the parameter $m_{\text{dense}}$ is critical density above which the growth becomes linear.

As microalgae grow, they consume carbon, which they get from dissolved CO$_2$ and other nutrients from their surroundings while releasing O$_2$. In general, microalgae biomass is 50% carbon by dry weight [1]. A mole of CO$_2$ has a mass of 44 grams and 12 of these grams come from carbon. Based on these premises, the expression that 1 gram of microalgae can fix 1.83 grams of CO$_2$ may be derived as follows

$$
\frac{44g\text{CO}_2/mol}{12g/mol} \times \frac{0.5gC}{g\text{algae}} = \frac{11}{6} \frac{g\text{CO}_2}{g\text{algae}} = 1.83 \frac{g\text{CO}_2}{g\text{algae}}
$$

A simplified equation for photosynthesis is given by

$$
12\text{H}_2\text{O} + 6\text{CO}_2 + \text{light} \rightarrow \text{C}_6\text{H}_{12}\text{O}_6 + 6\text{O}_2 + 6\text{H}_2\text{O}
$$

This equation states that for every gram of CO$_2$ consumed, there is a gram of O$_2$ produced. While this is true, it does not account for all of the O$_2$ that is produced. This results from the fact that O$_2$ molecules come from splitting water, which provide energy for all of the metabolic processes inside the microalgae. Therefore, there is not a one-to-one correspondence of O$_2$ molecules produced to CO$_2$ molecules fixed. The excess energy that is not used to fix CO$_2$ is used for other metabolic processes such as fixing nutrients from the surrounding media and cell repair. This is often echoed in the literature by the fact that it takes 8 photons of light to produce one O$_2$ molecule, but that it takes 8-12 photons of light to assimilate a CO$_2$ molecule (c.f., [21]). Assuming that 10 photons of light are required to fix one CO$_2$ molecule, the amount of O$_2$ produced will be

$$
\frac{32g\text{O}_2/mol\text{O}_2}{44g\text{CO}_2/mol\text{CO}_2} \times \frac{8\text{mol}\text{O}_2}{10\text{mol}\text{CO}_2} \times \frac{11g\text{CO}_2}{6g\text{algae}} = 1.07 \frac{g\text{O}_2}{g\text{algae}}
$$

Based on these assumptions, the CO$_2$ consumption rate and O$_2$ produced rate may be expressed in terms of the growth rate. In particular, the mass production and consumption rates of CO$_2$ and O$_2$, respectively, are

$$
\dot{m}_{\text{CO}_2}(g/L/h) = 1.83\dot{m}_{\text{algae}}(g/L/h)
$$

$$
\dot{m}_{\text{O}_2}(g/L/h) = 1.07\dot{m}_{\text{algae}}(g/L/h)
$$

In general, the relationships may be expressed as

$$
\dot{m}_{\text{CO}_2}(\text{mass/time}) = K_{\text{CO}_2}\dot{m}_{\text{algae}}(g/L/h)
$$

$$
\dot{m}_{\text{O}_2}(\text{mass/time}) = K_{\text{O}_2}\dot{m}_{\text{algae}}(g/L/h)
$$

where, $K_{\text{CO}_2}$ and $K_{\text{O}_2}$ are the amount of gas consumed/produced per mass of microalgae growth and may be in units other than grams gas per gram microalgae. An example of this is when the amount of CO$_2$ is measured in standard liters per minute (SLPM). Let $V_{\text{total}}$ be the volume of the PBR in liters and using the fact that there are 1.808 grams of CO$_2$ ($g\text{CO}_2$) per standard liter (SL), then $K_{\text{CO}_2}$

---

$^1$Microalgae contain the enzyme Rubisco that will utilize both CO$_2$ and O$_2$ as substrates.
may be expressed as
\[
m_{\text{CO}_2}(\text{SLPM}) = \frac{1h}{60\text{min}} \frac{\text{SL}}{1.808 g\text{CO}_2 \text{VPBR(L)}} m_{\text{algae}}
\]
\[
= \frac{1.83 V_{\text{PBR(L)}}}{1.808 \cdot 60} m_{\text{algae}}(g/L/h)
\]  (12)

E. Water Chemistry Subsystem

The water chemistry subsystem models both the dissolved gases and nutrients available to the microalgae in the media. The dissolved gases are a function of both the gases being delivered in by the MFCs and the internal gases being consumed and generated by the microalgae. The main purpose of sparging is to regulate the concentrations of dissolved O2 and dissolved CO2 through mass transfer. In general, the gas transfer rates may be modeled locally as a first order dynamic system. Due to the distributed nature of the system, the model would require many cascaded first order systems. This phenomenon may be essentially captured by using a first order plus dead time model [22], which is the method used here.

When the media in the PBR is at equilibrium with air, there is about 7mg/mL of dissolved O2 in the media, which is maintained through sparging when there is no growth. During high growth periods, dissolved O2 will build up in the system and is eventually purged at night. This is described by the following dynamic model.

\[
m_{\text{DO}}(t) = \frac{w_{\text{sparge}}}{\tau_{\text{DO}}} (m_{\text{DO, gas}}(t - \tau_{\text{d, gas}}) - m_{\text{DO}}(t)) + m_{\text{O}_2}(t)
\]  (13)

Here, \(w_{\text{sparge}}\) is the flow rate of gas into the PBR, \(\tau_{\text{DO}}\) is the lag time for mass transfer of DO between the media and sparging bubbles, \(m_{\text{DO, gas}}\) is the DO level that the media will equilibrate to, and \(m_{\text{O}_2}\) is the rate of oxygen produced through photosynthesis. When sparging is turned off (i.e., \(w_{\text{sparge}} = 0\)), then DO will build up in the system at the rate that it produced by photosynthesis. Once sparging is turned back on, the DO levels will equilibrate back to \(m_{\text{DO, gas}}\) with a lag time of \(\tau_{\text{DO}}/w_{\text{sparge}}\). The input gas stream is an air plus CO2 gas stream where the amount of added CO2 varies. This variation may change the equilibrium valve \(m_{\text{DO, gas}}\). There is a delay from when the CO2 concentration changes and when the new gas mixture arrives at the media, which is captured by the delay \(\tau_{\text{d, gas}}\). For the model presented in this paper, it was assumed that \(m_{\text{DO, gas}} = 7\) mg/mL independent of the CO2 concentration.

An analogous method may be used to model the dissolved inorganic carbon (DIC), which is given in eqn (14).

\[
m_{\text{DIC}}(t) = \frac{w_{\text{sparge}}}{\tau_{\text{DIC}}} (m_{\text{DIC, gas}}(t - \tau_{\text{d, gas}}) - m_{\text{DIC}}(t)) - m_{\text{CO}_2}(t)
\]  (14)

Here, \(m_{\text{DIC, gas}}\) is the CO2 gas concentration required for a specific pH. As CO2 is removed from the media through photosynthesis (i.e., \(m_{\text{CO}_2}\)), the value of \(m_{\text{DIC, gas}}\) will be increased to help replace the consumed CO2. Therefore, this value is always changing during active growth to maintain a constant pH. Due to the distributed nature of the system, there is a delay of \(\tau_{\text{d, gas}}\) between when the commanded CO2 concentration changes and when the CO2 reaches the media.

As CO2 dissolves in the media, it breaks down into different species, namely aqueous CO2 (\(\text{CO}_2(aq)\)), carbonic acid (\(\text{H}_2\text{CO}_3\)), bicarbonate (\(\text{HCO}_3^-\)), and carbonate (\(\text{CO}_3^{2-}\)). The combination of all of these species make up the total DIC. The amount of aqueous CO2, namely \(\text{CO}_2(aq)\), is a function of temperature and pressure, which is governed by Henry’s Law. Based on the DIC and Henry’s law, the following chemical equilibrium is reached.

\[
\text{CO}_2(aq) + \text{H}_2\text{O} \leftrightarrow \text{H}_2\text{CO}_3 \leftrightarrow \text{H}^+ + \text{HCO}_3^- \leftrightarrow 2\text{H}^+ + \text{CO}_3^{2-}
\]  (15)

The amount of each of carbonic acid, bicarbonate, and carbonate species determines the pH. As pH increases the equilibrium shifts to the left and to the right as the pH decreases. As microalgae grow, \(\text{CO}_2(aq)\) is removed from the surrounding media, which causes the equilibrium to shift to the left and the pH to rise. Some strains of microalgae will also utilize bicarbonate as a carbon source. The microalgae still require CO2, which they get by splitting bicarbonate into \(\text{H}^+ + \text{HCO}_3^- \rightarrow \text{CO}_2 + \text{OH}^-\). The release of the OH- also causes the pH to increase. It is unclear which method of carbon assimilation dominates the pH increase.

The addition of dissolved CO2 decreases the pH of the media. Since it can take 2-3 seconds for carbon to completely dissolve and only a fraction of the input CO2 dissolves before leaving the vent, there are some dynamics associated with the pH in the media, which are captured by the first order dynamics (transfer function) in eqn (16). The pH model is linearized about a pH of 7.3.

\[
\text{pH}(t) = \frac{1}{\tau_{\text{PH}}}(K_{\text{pH}} m_{\text{DIC}}(t) - \text{pH}(t))
\]  (16)

Here, \(\tau_{\text{PH}}\) is the lag time associated with the DIC settling into the appropriate species and \(K_{\text{pH}}\) is the conversion factor from DIC to pH units.

CO2 is not the only factor affecting pH. Others have found that pH is also affected by calcium carbonate precipitation in the media and nitrogen assimilation, excess cation influx, excess anion flux, and organic assimilation and excretion by the microalgae [23]. However, CO2 input is the main controllable and measurable variable which has the most significant effect on pH. This characteristic creates some challenges involving the separate control of CO2 and pH, which is a topic of ongoing research.

F. Feed-forward Controller

One of the applications of the model is to determine the amount of CO2 that is required by the microalgae and to supply it via FF CO2 control. Recall that the rate of CO2 consumption is directly related to growth rate. This was given in eqn 10. This CO2 consumption rate may be used as a FF input CO2 flow rate to the PBR. In practice, there is a nominal CO2 flow rate that is required to maintain pH, which is labeled \(m_{\text{CO}_2}\text{(media)}\). The overall FF controller input is given by

\[
u_{\text{FF}}^{\text{CO}_2} = m_{\text{CO}_2}\text{(growth)} + m_{\text{CO}_2}\text{(media)}
\]  (17)
As with most FF control, a feedback controller is used to correct for model differences and to reject system disturbances. For the setup here, a PI controller was used to provide the feedback correction based on the desired and measured pH. An overall block diagram of the controller is shown in Fig. 3.

![Controller Diagram](image)

**Fig. 3.** pH Regulation using a Feed-forward plus Feedback Controller

### III. EXPERIMENT

The 644 L PBR used for the following experiment is shown in Fig. 1. The PBR had four panels that were 17m long, 0.33m high, and 0.03m thick. For the experiment described here, the microalgae strain *Nannochloropsis oculata* was used. The goal was to grow the microalgae culture up to maximum density in the shortest amount of time. Enough nutrients were provided at the beginning of the batch to make sure that the microalgae were not substrate limited. A combination of FF and feedback controller was used to regulate the CO$_2$ delivery as described in Section II-F.

#### A. Model Parameters

A PAR sensor was used to measure the sun intensity at the bath. The methods outlined in Section II-C were used to determine the amount of light that entered the PBR bath in units of m$_{mol}$/hour. Since the mixing and orientation were held constant, the term $\eta_{PBR}$ in eqn 2 was grouped into the growth parameter $K_{PAR}$.

The microalgae were able to utilize most of the light at low cell densities; however, as the density increased, the growth rate became linear. This is described by the saturation of $m_{algae}$ in eqn 4. For the experiments here, the biomass units have been normalized so that $m_{dense} = 1$.

For the growth model used here, the temperature, nutrients, pH, O$_2$ concentration, and CO$_2$ concentration were regulated externally. O$_2$ removal was regulated by air sparging and the CO$_2$ concentration was maintained by regulating the pH. Therefore, the primary factor that affected growth was the PAR from eqn 2. The model parameter $K_{PAR}$ in eqn 4 captures the light utilization in units of m$_{mol}$/m$_{mol}$. This parameter contains the effects of all of the variables that were held constant like mixing, orientation, temperature, nutrients, pH, and dissolved O$_2$ and CO$_2$. This parameter along with the FF controller parameter $K_{CO2}$ were fit using a nonlinear least squares optimization.

The rate of respiration in the dark was calculated by examining the rate of respiration over multiple nights. This was accomplished take two points during the night and assuming exponential decay. For example, if $m_{algae}(0)$ is the dry mass at 11pm at night (assuming that sunset is well before 11pm) and $m_{algae}(5)$ is the dry mass at 4am the next day (assuming that sunrise is well after 4am), then the following holds

$$m_{algae}(5) = m_{algae}(0)e^{-5R},$$

and $R$ may be calculated directly. By repeating this process over many days and averaging the results, a nominal $R$ value was obtained. The FF controller parameters are given in Table I.

A feedback PI controller was used to maintain the pH at 7.3. The controller gains were empirically tuned. An anti-windup digital PI controller was implemented to both prevent windup and to limit the controller actuation to the limits of the MFCs.

### IV. RESULTS AND DISCUSSION

Due to some software issues, only a feedback controller was implemented on the actual PBR shown in Fig. 1. For comparison, an estimate of what the FF controller would have predicted is plotted over the amount of CO$_2$ required for pH regulation. The results of this controller are shown in Fig. 4.

![Model Verification](image)

**Fig. 4.** Dynamic Model Verification.
modeled and OD sensor measurement of microalgae mass. The third plot shows the amount of CO₂ required to maintain a pH of 7.3 and a plot of what the FF controller would have commanded. The FF controller was able to capture the CO₂ profile. During the day, the feedback controller was only able to regulate the pH to within 0.05 of 7.3. At night, the pH was within 0.01 of 7.3. It is assumed that the addition of the FF controller will provide tighter regulation during the day. The bottom graph shows the DO sensor reading and the DO model. All three models are able to capture the dynamics of the system using first order models.

For a given strain of microalgae, the rate of dark respiration, namely $R$, will be fixed. The only two parameters that will change with different operating conditions are $m_{dense}$ and $K_{PAR}$. The only parameter that will affect $m_{dense}$ is mixing since it will determine both the fraction of microalgae exposed to PAR photons and the duration of the exposure. Since there is an optimal light/dark cycle for microalgae [5], there is an optimal mixing with an associated maximal $m_{dense}$. Maximizing $m_{dense}$ will maximize that amount of time that the microalgae spend in the exponential growth phase. All of the other operating conditions will affect the sun utilization parameter, namely $K_{PAR}$. A larger $K_{PAR}$ means better sun utilization and hence more growth for a given amount of sun. Since the objective is to maximize growth, it is desirable to operate the PBR at the optimal temperature, nutrient level, dissolve oxygen level, dissolve carbon level, and pH level that will result in the largest $K_{PAR}$. Maximizing $m_{dense}$ and $K_{PAR}$ are topics of ongoing research.

V. CONCLUSIONS AND FUTURE WORK

A model for a vertical flat panel PBR was presented along with an example of how the model could be used for FF control. The model was developed independent of the actual PBR size or microalgae strain (i.e., it was built around densities and concentrations with parameters based on known theoretical relationships or fit from data). This allows for the same model to be used to evaluate the performance of a variety of PBR sizes, orientations, architectures, and various microalgae strains. It should be noted that different microalgae strains require different mixing, pH levels, temperatures, and nutrient levels. Ongoing modeling efforts will continue to develop methods for determining model parameters from first principles and experience with the physical PBRs.

As a part of the development process, a better understanding is needed of how the parameters held constant in eqns (1) and (4) affect the growth. Determining these effects and utilizing the model to test various operating conditions and PBR designs is crucial for commercial success. These are topics of ongoing research.

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