Robust Nonlinear Feedback-Feedforward Control of a Coupled Kinetic Monte Carlo-Finite Difference Simulation

E. Rusli, T. O. Drews, D. L. Ma, R. C. Alkire, and R. D. Braatz, Member, IEEE

Abstract—Robust nonlinear feedforward-feedback controllers are designed for a multiscale system that dynamically couples kinetic Monte Carlo (KMC) and finite difference (FD) codes. The coupled codes simulate the copper electrodeposition process for manufacturing on-chip copper interconnects in electronic devices. The control objective is to regulate the current density subject to the condition that the steady-state fluctuation of the overpotential remains bounded within $\pm 0.01$ V. The controller designs incorporate a low-order stochastic model that captures the input-output behavior of the coupled KMC-FD code. The controllers achieve the objectives and the closed-loop responses implemented on the low-order model and the coupled KMC-FD code match well within stochastic variations. The nonlinear feedforward control reduces the rise time of the controller response while the feedback control ensures robustness in the presence of model uncertainty.

I. INTRODUCTION

The vast majority of the literature on controller design is based on continuum models, which are described by systems of algebraic, ordinary differential, and partial differential equations. The continuum modeling approach, however, is inadequate for modeling much of the molecular, nanoscopic, and mesoscale phenomena that occur in the complex chemical processes that constitute the attention of today’s scientists and engineers. This is especially apparent in microelectronics processes, for which the most interesting phenomena occur at the nanometer and smaller length scales. Hence in recent years increasing efforts have been directed towards the development of noncontinuum models, such as kinetic Monte Carlo (KMC) simulation models, for which most controller design techniques are not directly applicable. Actually, it is only recently that the higher level analysis of such stochastic simulators has been possible, and only then applicable to certain classes of simulated processes, such as those with a clear separation of time scales [17].

The design of feedback controllers based on such noncontinuum models is one of the most challenging open research problems in the field of control [12]. For KMC codes, it has been proposed to construct reduced-order models by truncating unlikely configurations and grouping probabilities that evolve together [7], using smaller lattices [10], or applying time-steppers [17] or least-squares systems identification methods [6]. Similar reduced-order models have been defined for dynamically coupled continuum/non-continuum codes [13], [16].

Here a feedforward-feedback controller is designed for a coupled kinetic Monte Carlo-finite difference (KMC-FD) code that simulates the electrochemical deposition of copper into a trench, which is a key process step in manufacturing on-chip interconnects for microelectronic devices [1]. The industrial need is to deposit copper uniformly into trenches and vias of small dimension (less than 100 nm) under galvanostatic (i.e., constant current) conditions. This industrial importance has motivated numerous experimental and simulation studies on the modeling of copper electrodeposition in recent years [12]. The goal of the feedforward-feedback controllers is to maintain the current or current density at a constant specified value, without creating large fluctuations in the applied overpotential. The controllers enable the coupled KMC-FD simulations to operate under experimental operating conditions so that a separate study outside the scope of this paper can be done to compare model predictions from the coupled KMC-FD codes to the collected data.

The paper is organized as follows. First, the coupled KMC-FD copper electrodeposition simulation code is described. This is followed by construction of a low-order stochastic model that is used to design feedforward-feedback controllers and gain-scheduled filters to handle the non-Gaussian stochastic noise produced by the KMC code. Then the closed-loop responses of the controllers are compared in simulations of the low-order stochastic model and the KMC-FD simulation code.
II. COUPLED KINETIC MONTE CARLO-FINITE DIFFERENCE SIMULATION CODE

Kinetic Monte Carlo (KMC) methods are used to simulate structural properties of matter that are not completely describable by a macroscopic continuum description, and are increasingly used for simulating chemical and materials processes. A KMC simulation is a realization of the Master equation [5], [9]:

\[
\frac{\partial P(\sigma, t)}{\partial t} = \sum_{\sigma'} W(\sigma, \sigma')P(\sigma, t) - \sum_{\sigma'} W(\sigma, \sigma')P(\sigma, t)
\] (1)

where \(\sigma\) and \(\sigma'\) are successive states of the system, \(P(\sigma, t)\) is the probability that the system is in state \(\sigma\) at time \(t\), \(W(\sigma', \sigma)\) is the probability per unit time that the system will undergo a transition from \(\sigma'\) to \(\sigma\). The Master equation is a conservation equation for the probability that a system is in state \(\sigma\) at time \(t\), \(W(\sigma', \sigma)\) is the probability per unit time that the system will undergo a transition from \(\sigma'\) to \(\sigma\). Directly integrating the differential equations (1) for all of the states is infeasible, since the total number of differential equations, one for each state, is too large. Instead, only a single realization is computed, in which the KMC code chooses randomly among the possible transitions of the system and accepts particular transitions with appropriate probabilities. After each accepted or attempted transition, the time variable is incremented by one Monte Carlo time step, and the process is repeated. The probabilities are selected to satisfy certain conditions [5] that ensure that the real time variable \(t\) can be computed that corresponds to the number of Monte Carlo time steps.

The electrochemical deposition of copper into a trench is simulated in this application. A KMC method was used to simulate the processes on the surface, which enables the computation of the evolution of the surface roughness, which is an important characteristic of the produced copper deposit. The FD code describes the processes occurring at the surface boundary layer (see references in [3]). While truly molecular-scale simulations are of interest, this coarser mesoscale representation results in an efficient computational method that can predict surface roughness on the same scale as is measured experimentally [3], [4]. The T-shaped Monte Carlo domain consists of a trench with aspect ratio 2:1, with the trench being 40 subdomains wide, 80 subdomains high, and 6 subdomains deep. The top of the simulation domain is 70 subdomains wide.

The Monte Carlo domain has periodic boundary conditions in the \(x\) and \(y\) directions, an impenetrable boundary at the electrode surface (in the \(z\) direction), and receives mass fluxes at the top boundary in the \(z\) direction from the FD code. The KMC code provides the species concentrations to the continuum code. The KMC code also reads an applied overpotential \(\eta\) as input and produces a signal that is the charge passed during deposition. These signals serve as the output and input of the feedback controller (see Fig. 1). This paper considers the case where only pure copper and its charge forms are simulated. It should be noted that the use of solution additives is critically important for achieving a desired time-evolution of the deposit shape, but are not considered in this treatment. The extension of the control technique established here to more sophisticated simulations involving additive effects is straightforward, since tracking additional chemical species does not affect significantly the control problem or design methodology. Almost all of the charge that is passed is associated with reduction of copper.

The KMC code simulates deposition phenomena by considering the likelihood of various actions that each mesoparticle can take at a given time step. These actions are bulk diffusion, adsorption, desorption, and surface diffusion and reaction. All actions are computed as frequencies, with
units of s\(^{-1}\). At a given Monte Carlo time step, a mesoparticle can make a maximum of one move. The moves that each mesoparticle can make are specified in an input file. The possible moves that each species can make are a function of the location of the mesoparticle in the simulation space, as well as the number and type of the six nearest neighbors.

Three time steps are tracked in the KMC simulation code: (1) the time step over which the FD code is called for updated flux information (the linking time step); (2) the sampling interval for the feedback controller; and (3) the Monte Carlo (MC) time step. In order to capture the full dynamics of the system, the MC time step must be small enough to capture the most frequent actions. In this copper electrodeposition application, the Monte Carlo time step was computed to be ~2.8 ns, from (7) of [3]. A complete KMC simulation run typically requires 1.08\times10^8 MC time steps before the copper film reaches its desired thickness. In this particular study, the linking time step and the sampling interval for the controller are set to be 10\(^{-7}\) s and 10\(^{-2}\) s, respectively. The magnitude of linking time step was selected small enough to ensure stability in the interconnected systems [3], while being large enough that the overall computational expense is manageable.

To carry out the galvanostatic (i.e., constant current) simulations associated with industrial plating operations, the controller must manipulate the applied overpotential \(\eta\) to control the current density \(i\), based on the charge transferred as a function of time. There are two main requirements for the controller. First, the controller should have a tracking response as fast as possible, preferably with a settling time of less than 1 s. Second, the manipulated variable should not have overly large fluctuations (within ±0.01 V). The applied overpotential \(\eta\) enters the surface reaction frequencies in a highly nonlinear manner. This suggests that nonlinear control may give better performance than linear control. The next section describes how a low-order stochastic model was constructed from input-output data collected from the KMC-FD code.

III. IDENTIFICATION OF LOW-ORDER STOCHASTIC AND DETERMINISTIC MODELS

The KMC-FD code is computationally expensive, highly stochastic, and nonlinear. To design low-order controllers, a low-order stochastic model was constructed that captured the most essential input-output behavior of the coupled KMC-FD code. This low-order model was incorporated into model-based controller design and used for filter and controller tuning.

The output of the KMC-FD code was the cumulative charge passed from the beginning of the simulation up to the current simulation time. To emulate the real physical system as closely as possible, the charge signal was converted to a current density signal. The current density was computed as the total charge passed in every 0.01 s per cm\(^2\) of surface area. A larger time step interval could be used to compute the current from the charge, but this would lead to a more sluggish response, causing an inherent performance limitation in the controller. On the other hand, decreasing the time step leads to a more highly noise-corrupted signal.

The manipulated variable is the applied overpotential, which affects the kinetics of the mechanisms simulated in the KMC-FD code and hence directly affects the current generation.

The model identification stage consisted of applying a series of step input overpotentials to the KMC-FD code within the operation conditions of the code and observing the current responses. Sample results are plotted in Figure 2. Comparison of the probability mass function of different time segments suggests that each step response reaches steady state immediately. This is not surprising since the simulation time step for the KMC-FD code is much smaller than the time step of the control action. The KMC and FD codes are linked dynamically and communicate to each other by passing boundary conditions every 10\(^{-3}\) s, which is five orders of magnitude smaller than the time step of the control action.

The stochastic fluctuations displayed in the output response are non-Gaussian and asymmetric, and can be modeled by a discrete Poisson distribution for all normal operating conditions. To ensure consistency and accuracy, the identification procedure was repeated with different seed numbers. These sets of input-output data were used in the parameter estimation of a low-order stochastic model:

\[
P(i(k) = \kappa | \eta(k-1)) = \frac{\lambda^{\kappa} e^{-\lambda}}{(-400\kappa)!} \quad (3)
\]

\[
\lambda = 2.5285 e^{1.9167 \eta(k-1)} - 1.3622 \quad (4)
\]

where \(k\) is the time index (\(k \in Z\), where \(Z\) is the set of non-negative integers), \(\kappa \in \{-0.0025n, n \in Z\}\), \(\eta\) is the overpotential, and \(i(k)\) is the observed current density. The incremental value of \(\kappa\) is affected by the amount of charges involved in the reduction of copper species contained in one cubic lattice (subdomain). The form of the nonlinearity was motivated by the expression for the surface kinetics [3]. Figure 3 compares the stochastic current density produced by the low-order model (3)-(4) and the KMC-FD code for a range of applied overpotential.

IV. CONTROLLER AND FILTER DESIGNS

A linear controller was designed based on the low-order stochastic model (3)-(4). The controller incorporates a first-order filter to attenuate excessive simulation output noise (see Figure 4):

\[
F(z) = \frac{\alpha}{1-(1-\alpha)z^{-1}} \quad (5)
\]
with filter coefficient $\alpha$. The linear feedback controller was
initially designed based on the deterministic part of the
low-order model (3)-(4) and then detuned using the filter (5)
to meet the performance specifications. The deterministic
model of the plant, which is the expected value of the current
density as a function of the overpotential, was calculated
from (3)-(4):

$$i(k) = -6.3213 \times 10^{-3} e^{-6.5962 \eta(k-1)} + 3.4055 \times 10^{-3}$$

(6)

An alternative deterministic model, which schedules the
mean process gain as a function of the input variable $\eta$,
$$i(k) = K\eta(k-1),$$
(7a)
can be derived from the step response data. The mean
process gain was computed with respect to the steady-state
condition at $\eta = 0$. The minimum least-squares fit to a
quadratic function of the scheduled gain was:

$$K = 4.6058\eta^2 + 0.22074\eta + 0.061912$$

(7b)

The two deterministic models (6) and (7) give almost the
same output prediction error over the full range of operating
conditions.

A. Feedback-Feedforward Controller Designs

The gain in (7) varies by nearly a factor of three depending
on the operating condition: $K \in [0.05, 0.1417]$ (8)
where the upper bound was selected to exceed slightly the
steady-state value for regulating the current density at
$-0.015 \text{ A/cm}^2$. The linear feedback controller was designed
using direct synthesis. The desired closed-loop response was
first-order-plus-time-delay:

$$\frac{i}{i_c} = G_{CB}(1+FGC_{FB})^{-1} = \frac{(1-e^{-\Delta t/\tau})z^{-1}}{1-e^{-\Delta t/\tau}z^{-1}}$$

(9)

where $G$ is the process model, $C_{FB}$ is the feedback controller,
$\tau$ is the desired closed-loop time constant, $i_c$ is the desired
current density, and $\Delta t$ is the controller sampling time. For
the low-order model, $G = Kz^{-1}$, Equation (9) was
rearranged to derive the feedback controller

$$C_{FB} = \frac{(1-\phi)-(1-\alpha)(1-\phi)z^{-1}}{1-(1+\phi(1-\alpha))z^{-1} + \phi(1-\alpha)z^{-2}} \cdot K$$

(10)

where $\phi = e^{-\Delta t/\tau}$ and $\alpha$ is the filter coefficient. The model
gain $K$ was chosen to be 0.1417 to obtain optimal performance for the operating conditions simulated in the paper while ensuring robust stability to the model gain variation in (8), using the sufficient condition for nonlinear time-varying perturbations in [2]. The values $\Delta t = 0.01 \text{ s}$ and $\tau = 10^{-5} \text{ s}$ ensure fast response yet not faster than the dynamics of the KMC-FD simulation which is on the order of $10^{-5} \text{ s}$. The tuning of the filter coefficient $\alpha$ to satisfy closed-loop objectives is discussed in the next section.

The feedback controller is designed based on the plant
model in (6):

$$\eta = -\frac{1}{6.5962} \ln \left( \frac{3.4055 \times 10^{-3} - i_c}{6.3213 \times 10^{-3}} \right)$$

(11)

The feedforward term acts an inverter to cancel the static
nonlinearity in the low-order model. As a result, the model
combined with the inverter is a pure time delay with a unit
gain. The fact that the nonlinearity is static for the nominal
model causes the nonlinear robustness analysis to be
straightforward and identical to the analysis reported by [14]
for single-input single-output processes with linear
dynamics and static nonlinearities.

Gain-scheduled and nonlinear inversion-based feedback
controllers were also designed, but the closed-loop per-
formances were very similar to that obtained by the linear
feedback controller, and so for brevity those controller
designs and closed-loop simulation results are not reported
here. Interested readers are directed to [15].

B. Gain-scheduled Filter Designs

The filter coefficient $\alpha$ was tuned to ensure that at least
90% of the fluctuations in the applied overpotential were
within $\pm 0.01 \text{ V}$ over the entire operating regime, while
avoiding too much filtering which leads to unnecessarily
sluggish response. If a fixed filter coefficient were used,
then it would have to be designed based on the probability
density distribution of the applied overpotential at the final
time, that is, the time required to fill up the trench with
copper. The reason for this is that the applied overpotential
is the most negative at the final time, and the stochastic
fluctuations are largest when the applied overpotential is the
most negative. A filter coefficient that adequately filters the
stochastic fluctuations at the final time would also provide
adequate filtering at earlier times, but would provide much
more filtering than needed at the earlier times. This
motivated the use of a gain-scheduled filter coefficient
designed so that 90% of the fluctuations in the applied
overpotential are within $\pm 0.01 \text{ V}$ regardless of the operating
conditions.

A primary goal of this study was to create a filter and
controller design procedure that can be quickly repeated
when physicochemical parameters in the KMC-FD code are
changed. Due to the high computational cost of running the
KMC-FD code, its use in filter and controller design is
limited to the creation of data for constructing the low-order
stochastic model (3)-(4). The low-order stochastic model is
then used to design the filter and controller. The
approximate probability density distribution of the applied
overpotential at the final time was obtained by running the
closed-loop simulation using the low-order stochastic model
with the selected feedback controller 10,000 times for
several $\alpha$ values. The implementation of this Monte Carlo
technique was fast. It took less than 4 minutes to complete
10,000 runs for one $\alpha$ value when the code is written in Microsoft Fortran and run on a Personal Computer with a 900 MHz Athlon processor. From this probability density distribution, the mean and 90% confidence interval were estimated. As discussed above, the values for the filter coefficient were determined which resulted in 90% of the fluctuations being within ±0.01 V for all values of the applied overpotential (which is directly related to the current density, through (6)). The least-square fit mapping for a linear controller is given by:

$$\alpha = 0.083919e^{336.61r} + 376.64$$  \hspace{1cm} (12)

where $i_r$ is the desired current density. Equation (12) implies that within the normal operating regime, more filtering is required for larger current density. This result agrees with physical intuition as the variance of the process output variable increases with its mean value as shown in Figure 2.

V. RESULTS AND DISCUSSION

Fig. 5 shows agreement between the closed-loop responses obtained by applying the feedforward-feedback controllers to the KMC-FD code and the low-order stochastic model (3)-(4), where the reference current density was –0.015 A/cm². The close agreement indicates that the stochastic model (3)-(4), where the reference current density controllers to the KMC-FD code and the low-order responses obtained by applying the feedforward-feedback controller, due to the limit on the allowed fluctuations in the manipulated variable (the applied overpotential). The speed of response of the feedforward controller is not limited by these stochastic fluctuations. The integral action in the feedback controller makes small corrections in the manipulated variable so that zero bias in the current density occurs at long time, under model uncertainty.

Fig. 5b shows that the feedforward-feedback controller successfully regulates the filtered current density to the desired setpoint. Again, a good agreement is observed for the closed-loop response of the filtered current density for the controller implemented on the low-order model (3)-(4) and the coupled KMC-FD code, indicating that the low-order model was sufficiently accurate to be used in controller design. Fig. 5c focuses on the initial time response of the filtered current density. The filtered current density reaches the desired set-point in less than 1 second for both the low-order model and the coupled KMC-FD codes.

Replacing the linear feedback controller with inversion-based nonlinear or gain-scheduled controllers [15] resulted in very similar closed-loop responses. This result is not surprising because the response at very short times is specified by the nonlinear feedforward controller, which was the same in all feedback-feedforward control designs, and the response at longer times is primarily specified by the dynamics of the filter $F$, which was the same in all feedback-feedforward control designs.

VI. CONCLUSIONS

A low-order feedforward-feedback controller was designed for a coupled kinetic Monte Carlo finite difference code that simulates the infill of a trench during copper electrodeposition. The feedforward-feedback controller and associated gain-scheduled filter were constructed from a low-order stochastic model constructed from data collected from the KMC-FD code. The controller enables the KMC-FD code to operate under constant current conditions, which is typically done in industrial practice. The controller was also designed to keep the steady-state fluctuations of the overpotential bounded within ±0.01 V. Differences between the closed-loop simulations obtained with the low-order stochastic model and the KMC-FD code were within the stochastic variations in the responses, which justified the use of the low-order stochastic model for filter and controller design.

REFERENCES


Fig. 1. Simulation coupling of the KMC-FD codes with a controller. FD denotes finite difference code, KMC denotes kinetic Monte Carlo code, and C is the controller. The KMC domain is illustrated on the left. At each linking time step, the KMC code passes the species concentration ci at the interface to the FD code and in return, the FD code passes the species flux Ni at the interface to the KMC code. The control output is current density i, the manipulated variable is the overpotential η, and ir is the controller set point.

Fig. 2. Incremental step input implemented on the KMC-FD code and the resulting step response. The step response was constructed by plotting the current density computed for every 0.01 second. As shown, the step response is stochastic.

Fig. 3. Current density distributions on four overpotential η values for the low order stochastic model (3)-(4) (solid line) and the coupled KMC-FD simulation.

Fig. 4. Block diagram for the closed-loop system: G is the plant (either the coupled KMC-FD codes or the low-order stochastic model), CFB and CFF are the feedback and feedforward controllers, F is the filter, η is the applied overpotential, i is the current density, and ir is the desired current density.

Fig. 5. Closed-loop responses of the overpotential (a) and the filtered current density (b and c) for the feedforward-feedback controller implemented on the low-order stochastic model (3)-(4) and the KMC-FD simulation code.